

## How Many Bursts Does it Take to Form a Core at the Center of a Galaxy?

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### ABSTRACT

We present a novel method for systematically assessing the impact of central potential fluctuations associated with bursty outflows on the structure of dark matter halos for dwarf and ultra-faint galaxies. Specifically, we use dark-matter-only simulations augmented with a manually-added massive particle that modifies the central potential and approximately accounts for a centrally-concentrated baryon component. This approach enables precise control over the magnitude, frequency, and timing of when rapid outflow events occur. We demonstrate that this method can reproduce the established result of core formation for systems that undergo multiple episodes of bursty outflows. In contrast, we also find that equivalent models that undergo only a single (or small number of) burst episodes do not form cores with the same efficacy. This is important because many UFDs in the local universe are observed to have tightly constrained star formation histories that are best described by a single, early burst of star formation. Using a suite of cosmological, zoom-in simulations, we identify the regimes in which single bursts can and cannot form a cored density profile. Our results suggest that it may be difficult to form cores in UFD-mass systems with a single, early burst regardless of its magnitude.

*Keywords:* Galaxy dark matter halos(1880) — Galaxy structure(622) — Cold dark matter(265)

### 1. INTRODUCTION

The current paradigm of cold, collisionless dark matter plus dark energy ( $\Lambda$ CDM) has had a number of successes reproducing observations on the largest scales. For example, the distribution of galaxy clusters seen from large sky surveys are consistent with the predictions of cosmological N-body simulations which evolve the primordial fluctuations measured from the Cosmic Microwave Background to present-day using a  $\Lambda$ CDM framework (e.g., Springel et al. 2005; Reid et al. 2010). Yet, on smaller scales (i.e., the scales of individual galaxies), key tensions persist that bring into question whether a cold and collisionless dark matter (DM) species is indeed the best descriptor (Bullock & Boylan-Kolchin 2017; Sales et al. 2022).

The small-scale tensions in Cold Dark Matter (CDM) generally arise from inconsistencies in the predicted structure, abundance, or distribution of galaxies as compared to observations—especially for low-mass systems (Moore 1994; Sales et al. 2022). In the absence of baryons, CDM galactic halos are expected to follow Navarro-Frenk-White (NFW) profiles (Navarro et al.

1996b), which feature a continuously rising central DM density (i.e., a DM cusp) with an inner log-slope  $\frac{d \log(\rho)}{d \log(r)}$  that approaches  $-1$  at small radii. By contrast, it is observationally inferred that some nearby low-mass galaxies have a flattened inner DM density (i.e., a DM core) (e.g., Walker & Peñarrubia 2011; Oh et al. 2015; Almeida et al. 2024; Vitral et al. 2024). This discrepancy between predictions and observations is referred to as the “core-cusp problem.” It is related to the “diversity problem” (Oman et al. 2015), which refers to the fact that the circular velocity profiles of simulated CDM galaxies exhibit less variation compared to the observed profiles of dwarf galaxies. This inconsistency may be an indication that the CDM model that underpins our current cosmological paradigm needs revisiting. Indeed, alternative DM models, such as those which include self-interactions (e.g., Spergel & Steinhardt 2000; Tulin & Yu 2018), can potentially alleviate these discrepancies by introducing new mechanisms that alter a halo’s inner structure.

However, it is worth noting that the core-cusp problem was initially identified and studied through N-body

simulations, which lack a direct treatment of the baryonic component of galaxies. Modern cosmological simulations include not only gravity acting upon DM, but also hydrodynamics coupled to comprehensive models of galaxy formation. These simulations incorporate the physics of gas cooling, stellar feedback, AGN feedback, star formation, black holes, and the ISM (see, e.g., Somerville & Davé 2015; Vogelsberger et al. 2020, for reviews). The inclusion of baryons is not just an improvement allowing for more direct modeling of the emergent galaxy population, but is also critical for the evaluation of the CDM tensions as the baryons can impact the DM particles by modifying the overall halo potential.

In fact, it has been demonstrated that the interaction of DM and baryons through gravity alone may be sufficient to alleviate the core-cusp problem (Navarro et al. 1996a; Read & Gilmore 2005; Governato et al. 2012). Episodic mass ejection from the galactic center can inject heat into the central DM by rapidly fluctuating the central potential (Governato et al. 2010; Pontzen & Governato 2012, 2014). Physically, these episodic mass ejections can be thought of as strong, or “bursty”, stellar feedback events. Fully cosmological simulations employing the more bursty feedback models have shown core formation beginning in the classical dwarf ( $M_* = 10^5\text{--}10^7 M_\odot$ ) regime and peaking in strength for bright dwarf ( $M_* = 10^7\text{--}10^9 M_\odot$ ) galaxies (Chan et al. 2015; Tollet et al. 2016; Bullock & Boylan-Kolchin 2017; Lazar et al. 2020; Di Cintio et al. 2014; Azartash-Namin et al. 2024). Thus, if star formation occurs in stochastic bursts (e.g., Governato et al. 2010; Hayward & Hopkins 2017; Faucher-Giguère 2018), as opposed to the stellar mass growing smoothly over time, the resulting gaseous outflows naturally perturb the orbits of the DM particles in the inner region and sufficiently flatten the density profile (e.g., Oñorbe et al. 2015; Jahn et al. 2023). There are, however, limits where stellar feedback is incapable of DM core formation. Fitts et al. (2017) found  $M_* \approx 2 \times 10^6 M_\odot$  to be the threshold mass for bursty feedback to significantly modify the DM density profile. This limit is primarily, if not entirely, an energetic one: galaxies that are too low in mass simply do not have enough stellar feedback energy present to convert the core into a cusp.

Regardless of the details, it is clear that the small-scale tensions may arise either owing to our lack of knowledge of galaxy formation physics or a fundamental flaw in our currently favored DM paradigm. Studying both (i) the regimes when, where, and how bursty feedback is able to operate and, separately, (ii) the regimes where bursty feedback is able to convert DM cusps into cores is therefore critical to our understanding of the extent

to which our DM prescription needs to be modified. In this work, we take a new approach of using fully cosmological, dark-matter-only (DMO) simulations coupled to analytically-modulated central potential contributions. We are able to capture the fully cosmological development of the DM halo, while also considering how *systematically varied* time-dependent central potentials impact the DM halo structure. As we demonstrate within this paper, we can systematically vary the total number of bursts, as well as the total mass ejected in each burst. Our approach allows us to fill in an important void that sits between previous idealized studies (e.g., those of Pontzen & Governato 2012 and Ogiya & Mori 2014) and the fully cosmological studies where the bursty nature of feedback naturally arises in a way that cannot be directly modulated (e.g., Hopkins et al. (2014); Oñorbe et al. (2015); Lazar et al. (2020); Chan et al. (2015)).

In addition to introducing this flexible framework, we also aim to address the questions: “Could galaxies convert a DM cusp into a core via a single episode of star formation?” It has been suggested that some UFD satellite galaxies have implied cored DM density profiles (Almeida et al. 2024). However, the stellar populations within these systems are fairly tightly constrained to be consistent with approximately single-age stellar populations that are also very old (i.e., having formed  $> 80\%$  of their stellar mass before the midpoint of reionization ( $z = 7.7 \pm 0.7$ ; Sacchi et al. 2021)). In other words, if these systems formed most of their stellar mass in a single burst long ago, could that be sufficient to convert a DM cusp into a core, or are multiple, episodic bursts required?

In this paper, we test the ability of bursty feedback to convert cusps into cores using modified cosmological simulations where we can manually prescribe the number and magnitude of the bursts to address this question. The structure of this paper is as follows. In §2, we outline our methods, including descriptions of: our simulations (§2.1), the employed galaxy growth/burst/outflow models (§2.2, §2.3), and the method of characterizing inner DM density profiles (§2.4). In §3, we present our results, split into the classical dwarf (§3.1) and UFD (§3.2) regimes. In §4, we discuss our results and in §5, we present our conclusions.

## 2. METHODS

### 2.1. Simulations

We study the mechanism of core formation via bursty feedback using modified cosmological simulations. The foundation of our cosmological simulations are standard DMO zoom-in simulations. We create zoom-in initial conditions using MUSIC (Hahn & Abel 2011), with a

parent box of 36 Mpc. We adopt cosmological parameters  $\Omega_0 = 0.301712$ ,  $\Omega_\Lambda = 0.6983$ ,  $\Omega_b = 0.0$ , and  $H_0 = 100 \text{ h km s}^{-1}$  where  $h = 0.6909$  consistent with Planck Collaboration XI (Planck Collaboration et al. 2016). Our simulations have a DM mass resolution of  $3.44 \times 10^3 M_\odot$  and a gravitational softening of 0.038 kpc. We then evolve these initial conditions from redshift  $z = 127$  down to  $z = 0$  using the simulation code AREPO (Springel 2010; Weinberger et al. 2020). Prior to the addition of any changes to the central potential (as described below), the setup described here is a standard CDM cosmological zoom-in simulation.

Our goal in this paper is to probe the impact of a set of successive mass expulsion events on the resulting DM halo structure. To achieve this, we follow the approach used in Rose et al. (2023) whereby the gravitational impact of the central baryon component (i.e., galactic gas and stars) is represented by a single massive simulation particle. Unlike the DM simulation particles, which move freely under the force of gravity through the simulation domain and have a constant mass with time, the tracer particle is pinned to the potential minimum of the halo and given a manually prescribed mass that evolves with time. As with all other simulation particles, the tracer particle is assigned a gravitational softening. While this is strictly to avoid two-body interactions for DM particles, a larger softening is employed for the massive tracer particle to emulate the effect of having a spatially distributed (i.e., not point-like) mass distribution. We note that a different potential modification profile could have been selected, however, Rose et al. (2023) showed this was sufficient to produce realistic galaxy properties when compared with baryonic simulations.

We note three points about this setup. First, because we manually vary the tracer particle’s mass, the total mass in the simulation is not conserved. This variation in the particle’s mass can capture the impact of baryons condensing into the central region and subsequently being expelled. In other words, this particle is the mechanism that we use to impose specific time variability in the central potential. We do not expect the fact that the global mass budget changes slightly with time to impact our findings. While local fluctuations to the mass (i.e., bursty outflows) can change the distribution of matter in the central halo, these fluctuations amount to a change in the total mass globally that is of order  $10^{-6}\%$ . Second, even though we are using a very simplistic method for modifying the central potential, the approach does capture the impact of the central baryon component on the DM halo structure, as demonstrated in Rose et al. (2023). And, third, because we are manually prescrib-

ing the tracer particle’s mass, we can systematically explore varied mass growth histories including an array of smooth and bursty growth histories.

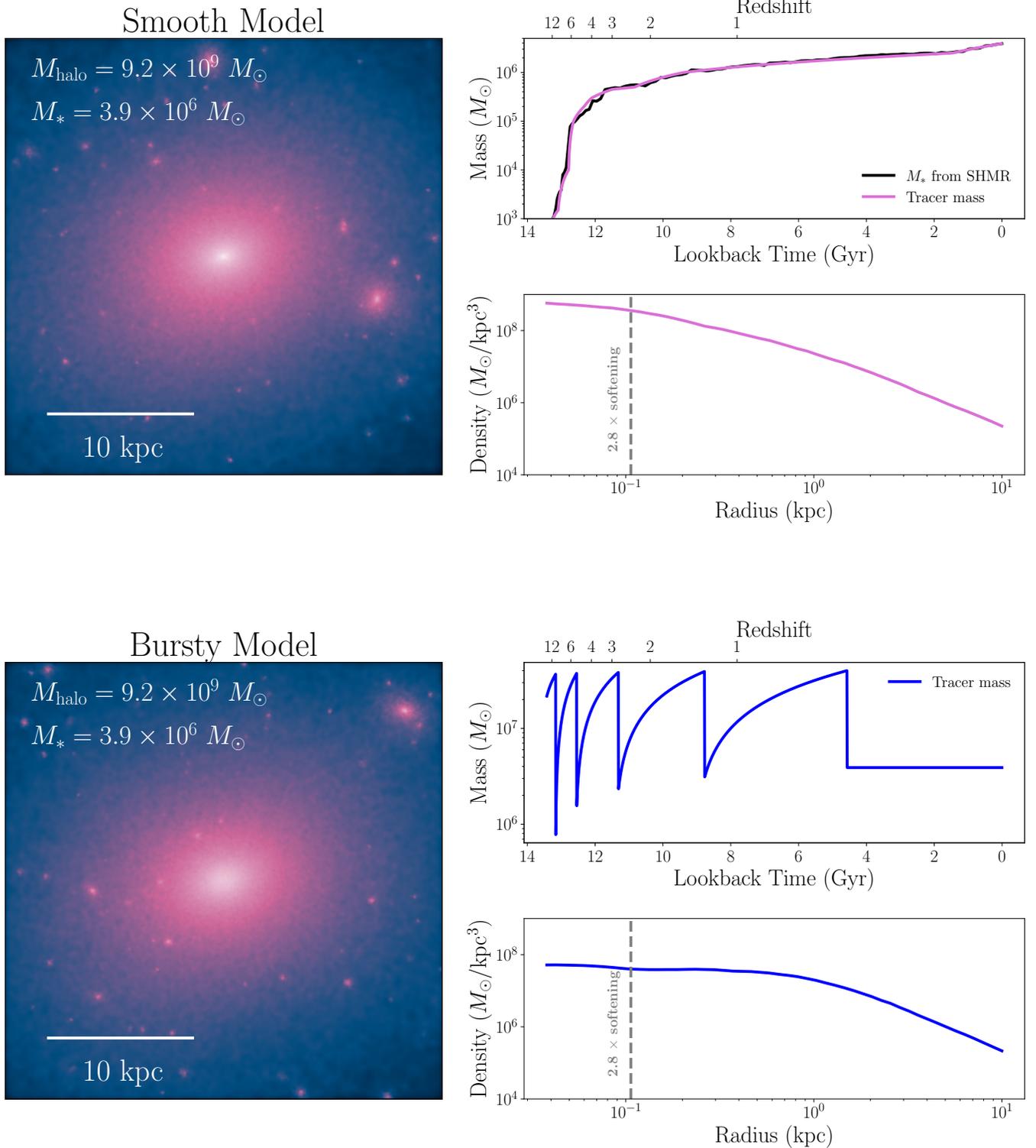
We first explore the classical dwarf regime in order to ensure the model can reproduce previous results for the central DM halo properties in the presence and absence of bursty feedback. We first model the smoothly forming classical dwarf galaxy (i.e., without bursty feedback) to verify cusp formation. We then model the same system with the stellar mass forming over multiple episodic bursts of star formation. Finally, we compare the resulting DM density profiles to verify that the tracer particle emulating bursty outflows can turn the cusp to a core. Once this is established, we apply this method to the specific case of UFDs that undergo just one outflow.

## 2.2. Galaxy Growth/Outflow Models

The unique feature of our simulations is that we impose specific mass evolution histories on the tracer particle. Specifically, its mass is updated at each timestep during the simulation following some pre-prescribed pattern. We employ three growth patterns: a smooth model, an episodically bursty model, and a single-burst model—each of which are described here.

The first class of model is a smooth star formation history, henceforth referred to as smooth models, which describes a galaxy whose central mass smoothly grows with time (i.e., does not experience any significant mass blowouts). The tracer mass growth over time for this model is shown in the top-right panel of Figure 1. The primary purpose of these models is to provide a standard of comparison against which we can understand how the bursts have (or have not) impacted the density profile.

The second class of model is the episodically bursty model, where the galaxy is assumed to accrete gas mass smoothly for some period of time, followed by a rapid/instantaneous drop in the tracer particle mass mimicking a feedback-driven blowout event. The tracer mass growth over time for one such model is shown in the lower-right panel of Figure 1. We keep the final stellar mass fixed at the same value as in the smooth model (described in further detail for each of the two galaxy models in §2.3). We prescribe a mass evolution for the tracer particle that is meant to mimic the fluctuating mass of a galaxy with bursty outflows and captures the impact that bursty feedback has on the orbits of the inner DM particles. The fluctuation of the central mass changes the gravitational potential, and if this happens sufficiently quickly (not adiabatically), it boosts the DM particles to a higher orbit. The net effect is that this process irreversibly transfers energy to the DM particles. We model this process by allowing



**Figure 1.** Comparison of DM density for the smooth (top panels) and bursty (bottom panels) models implemented using the modified-DMO approach for a halo with mass  $9.2 \times 10^9 M_{\odot}$ . *Left:* Dark matter mass projection made from a  $30 \times 30 \times 30$  pc box surrounding the central halo. The halos look similar, save for their central regions. The smooth model produces a clear peak in density at the very center, while the bursty model reaches a constant density (forms a core) up to  $\sim 2.0$  kpc from the center. *Right:* Tracer mass versus time as well as density profile for the smooth and bursty model. In both cases, the final stellar mass is  $3.9 \times 10^6 M_{\odot}$ . The tracer mass in the upper panel represents a galaxy with a smooth history, which follows the SHMR shown in black. The tracer mass evolution in the lower panel represents a galaxy that undergoes five bursts of star formation, expelling  $3.6 \times 10^7 M_{\odot}$  of gas in each burst. The  $z = 0$  DM density profiles produced from each of these models are also shown. The grey dashed line marks  $2.8 \times$  the DM particle softening, the point below which numerical effects begin to be important. The smooth model has an inner log-slope  $\alpha = -1.40$  when averaged over 1–2% of the virial radius, consistent with an NFW profile. By contrast, when there are episodic bursts, we find a log-slope  $\alpha = -0.63$ .

the tracer particle mass to increase at a constant rate in scale factor, then instantaneously decreasing it. The height of this drop physically corresponds to the gas mass expelled from the central region of the galaxy due to supernova energy. The mass that remains after this sharp decrease corresponds to the stellar mass formed in the burst (which is simply the final stellar mass divided by the number of bursts). After the last burst, the tracer particle’s mass remains constant. This is not necessarily physical in the sense that the galaxy’s mass can continue to increase, but is motivated by the fact that star formation is less bursty at lower redshifts (Faucher-Giguère 2018). We vary both the number of bursts and the amount of mass expelled in §3.1 to understand the impact of both of these parameters. Rather than making physical assumptions, the range of values we tested for the amount of mass expelled was determined by starting with extremely large values, and decreasing it until core formation ceased.

We assign the burst times by assuming that the time separating bursts is proportional to the dynamical time of the halo (Ogiya & Mori 2014). Episodically bursty models with more (fewer) bursts simply assume that the burst timing is a smaller (larger) multiple of the Hubble time. In the model shown in the lower-right panel of Figure 1, we assume that the stellar mass forms over five bursts (at  $z = 9.9, 5.3, 2.8, 1.3$  and  $0.4$ ) and each burst causes  $3.6 \times 10^7 M_\odot$  to be expelled from the inner region of the galaxy.<sup>1</sup> The number of bursts that takes place in hydrodynamic simulations which model these processes explicitly can vary based on many factors, but is generally of order 10 bursts. As one example, galaxies in a sample taken from the FIRE simulations underwent  $\sim 1$ – $2$  bursts every 200 Myr at  $z = 2$  (Sparre et al. 2017). Approximating this as the rate across a galaxy’s entire formation history, and assuming that star formation ceases to be bursty at  $z \sim 1.3$  (Faucher-Giguère 2018), this yields a typical value of between 20 and 50 bursts.

The third and final growth model we employ is the single-burst model. Inspired by stellar age distributions in UFDs (e.g., Sand et al. 2010; Okamoto et al. 2012; Weisz et al. 2014; Brown et al. 2014; Simon 2019; Gallart et al. 2021; Sacchi et al. 2021), these models increase their mass steadily with time (attributed to gas accretion) followed by a single outflow event. The subsequent

mass is then held constant until the present day. This model can be considered a limit of the bursty model that is constrained to a single burst.

### 2.3. Galaxy Models: Classical and Ultra-faint Dwarf

We simulate both classical dwarf and UFD galaxies to study the mechanism of core formation via bursty feedback. The classical dwarf has a  $z = 0$  halo mass of  $9.2 \times 10^9 M_\odot$ . To model a galaxy of this mass with a smooth growth history, we employ the redshift-dependent stellar-to-halo-mass relation (SHMR) described in Moster et al. (2013). To achieve this, we first run a DMO simulation to calculate the halo mass as a function of time. We then use the SHMR to evaluate the corresponding stellar mass and prescribe the growth of the massive particle to match this growth history. The tracer mass enters the simulation at  $z = 11$  with a mass of  $10^3 M_\odot$  and has a final mass of  $3.9 \times 10^6 M_\odot$ , as shown in the top-right panel of Figure 1.<sup>2</sup> We place the tracer particle in the simulation no earlier than  $z = 11$  because it will be pinned to the potential minimum of the most massive halo within a manually defined sub-volume. At very early times, the individual halos are closer together and more similar in mass, making it difficult to identify the most massive halo at  $z = 0$ , which is where we want to place the tracer mass. We do not expect this choice to significantly impact our results because the halo is a small fraction of its  $z = 0$  mass. We use a gravitational softening of 0.36 kpc for the massive particle representing the baryon mass of the galaxy, meaning that the majority of the mass is concentrated within 1.1 kpc.

The UFD has a  $z = 0$  halo mass of  $7.8 \times 10^7 M_\odot$ . We adhere to observational constraints on the star formation histories of these systems to determine their stellar mass as a function of time. We prescribe a growth history consistent with the cumulative mass fraction over time of Milky Way (MW) satellites that have a similar present-day halo mass. Specifically, we set the final stellar mass to  $1.4 \times 10^3 M_\odot$ —consistent with the observed stellar mass of these systems, which ranges from  $(0.54$ – $7.46) \times 10^3 M_\odot$  (Sales et al. 2017) and within  $2\sigma$  of both the predictions of semi-analytic models (Ahvazi et al. 2024) and forward modeling of MW satellites (Nadler et al. 2020). In our smooth model, the particle mass grows such that 80% of the stellar mass has formed by  $z = 7$  and 90% by  $z = 5$ . To model a single burst for

<sup>1</sup> One can easily see that the minimum mass after the burst is gradually increasing with time. In fact, the upper mass immediately before the burst is also increasing with time, but this is not so easily seen with the log-scale of the plot. This makes it seem like the amount of mass being expelled varies with time even though it is constant.

<sup>2</sup> The tracer particle is initialized at the same time of  $z = 11$  but at a higher mass ( $2.3 \times 10^7 M_\odot$ ) for the bursty model, shown in the bottom-right panel of Figure 1. This is because the first of the five bursts in this model is set to occur at  $z = 10$ . In order for this to happen, the tracer mass must be quite large prior to the outflow at this time.

363 this galaxy, rather than making physical assumptions  
 364 about when the burst occurs, we manually vary its tim-  
 365 ing across a wide range of values ( $z = 1$  to  $z = 8$ ) to  
 366 understand how this changes the impact of the outflow  
 367 on the DM density. The amount of mass expelled is ini-  
 368 tially set at  $1.4 \times 10^4 M_\odot$  by making assumptions about  
 369 the gas mass available to be expelled in these systems,  
 370 the details of which are discussed in §3.2, but it is also a  
 371 parameter that we vary. We also employ a smaller grav-  
 372 itational softening of 0.06 kpc for the massive particle  
 373 to account for the difference in size as compared with  
 374 the classical dwarf system.

#### 2.4. Characterization of Density Profiles

375 We use two independent metrics to characterize the  
 376 density profiles of the galaxies and assess whether they  
 377 are cuspy or cored. We calculate the inner log-slope,  
 378 commonly referred to as  $\alpha$  (where  $\rho \propto r^\alpha$ ), over 1–2%  
 379 of the virial radius (Di Cintio et al. 2014; Tollet et al.  
 380 2016). This is a reliable metric for cores that are a few  
 381 percent of the virial radius, but is not sensitive to the  
 382 presence of smaller cores (given the radius range where  
 383  $\alpha$  is determined). For this reason, we use a complemen-  
 384 tary approach of fitting to the core-Einasto model and  
 385 finding the best-fit core radius  $r_c$  (Lazar et al. 2020).  
 386 This addresses the issue of not detecting smaller cores,  
 387 but there can still be instances in which the model fit is  
 388 sufficiently poor that we do not get a reliable estimate  
 389 of the core radius. Density profiles with slightly irreg-  
 390 ular shapes will not be well-characterized by a three-  
 391 parameter model, and in these cases, the core radius  
 392 estimate will also be an imperfect metric. Using both of  
 393 these measures decreases the bias associated with  $\alpha$  or  
 394  $r_c$  alone.

### 3. RESULTS

396 In this section, we present results employing the pre-  
 397 scriptive approach described in §2. We split our re-  
 398 sults into the classical dwarf regime (§3.1), where DM  
 399 cores are often observed (e.g., Kleyna et al. 2003; Walker  
 400 & Peñarrubia 2011; Amorisco & Evans 2012; Amorisco  
 401 et al. 2013), and the UFD regime (§3.2) where the DM  
 402 density may be cored (Amorisco 2017; Contenta et al.  
 403 2018; Simon et al. 2021) or cusped (Hayashi et al. 2020;  
 404 Vitral et al. 2024), and there are often large uncertain-  
 405 ties associated with these measurements (Hayashi et al.  
 406 2023). In the UFD regime, star formation is restricted to  
 407 a small number of bursts (e.g., Brown et al. 2014; Simon  
 408 2019; Gallart et al. 2021; Sand et al. 2010; Okamoto et al.  
 409 2012; Sacchi et al. 2021; Weisz et al. 2014). Therein,  
 410 we study how varying the amount of mass expelled per  
 411 burst, the number of bursts, and the effective size of the

413 galaxy impacts the efficacy of bursty feedback at form-  
 414 ing cores.

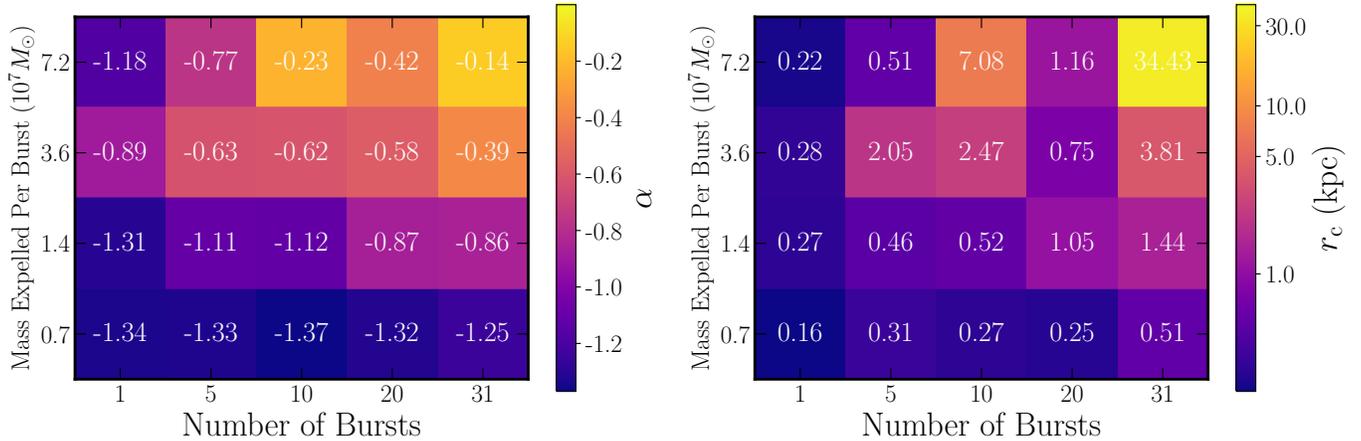
#### 3.1. Classical Dwarfs

415 Figure 1 provides a visual overview of the smooth  
 416 (top row) and bursty (bottom row) growth models for  
 417 the classical dwarf. For each model, we show the mass  
 418 growth of the tracer particle over time. For the smooth  
 419 model, the tracer particle mass is shown in magenta  
 420 against the stellar mass inferred from the SHMR re-  
 421 lation in black (Moster et al. 2013). As described in  
 422 §2.2, the episodically bursty model has a tracer mass  
 423 that increases smoothly, then instantaneously decreases  
 424 a specified number of times. In the model shown, there  
 425 are five such outflow events. Also shown for each model  
 426 are the corresponding present-day DM density profiles.  
 427 The vertical grey dashed line marks  $2.8 \times$  the DM par-  
 428 ticle softening, the point below which numerical effects  
 429 begin to be important. Looking at the region to the right  
 430 of this dashed line, we see that the central density profile  
 431 is cusped for the smooth model and cored for the episod-  
 432 ically bursty model—both consistent with expectations.  
 433 The smooth model has inner log-slope  $\alpha = -1.40$  when  
 434 averaged over 1–2% of the virial radius, consistent with  
 435 an NFW profile. By contrast, the episodically bursty  
 436 model forms a core 2.05 kpc in size and has  $\alpha = -0.63$ .  
 437 For illustration, we also show the present-day DM  
 438 mass projection, produced from a  $30 \times 30 \times 30$  kpc box  
 439 centered on each galaxy.

##### 3.1.1. Variable Total Mass Outflow Models

441 As a first variation on the episodically bursty model,  
 442 we consider how the number and amplitude of poten-  
 443 tial variations impact core formation. Specifically, we  
 444 manually change the strength and frequency of the cen-  
 445 tral potential variations by altering (i) the total num-  
 446 ber of bursts ranging from 1 to 31, spaced proportion-  
 447 ally to the dynamical time of the halo and (ii) the to-  
 448 tal mass expelled per burst ranging from  $0.7 \times 10^7 M_\odot$   
 449 to  $7.2 \times 10^7 M_\odot$ . Taken together, this changes the to-  
 450 tal integrated mass expelled for the tracer particle from  
 451  $0.7 \times 10^7 M_\odot$  (for a single burst with the smallest mass  
 452 expulsion) to  $2.2 \times 10^9 M_\odot$  (for 31 of the most massive  
 453 bursts). In other words, this tests the impact of chang-  
 454 ing the total mass ejected from the central region by  
 455 several orders of magnitude—hence, we refer to these  
 456 scenarios as variable total mass outflow models.

457 Our results show significant variations in core for-  
 458 mation based on our outflow model. For each model,  
 459 we have calculated both the inner log-slopes and best-  
 460 fit core radii  $r_c$  (Lazar et al. 2020) of the resulting  
 461 present-day DM density profiles. We show the results  
 462 in terms of both metrics as a function of the amount of  
 463



**Figure 2.** Summary of the inner log-slopes ( $\alpha = \frac{d \log \rho}{d \log r}$ ) best-fit core radii  $r_c$  for a classical dwarf galaxy as a function of number of bursts and burst mass.

464 mass expelled per burst and number of bursts in Figure  
 465 figure 2. Several clear trends emerge: galaxies generally  
 466 have more cored density profiles when they either expe-  
 467 rience a larger number of bursts (i.e., moving to the  
 468 right in Figure 2) or more massive bursts (i.e., moving  
 469 up). As the mass expelled per burst increases, the inner  
 470 log-slope for the 10, 20, and 31 burst simulations in-  
 471 creases from  $\sim -(1.37-1.25)$  to  $-(0.42-0.14)$  mono-  
 472 tonically. Similarly, the core radius for these simulations  
 473 increases from  $\sim 0.25-0.51$  kpc to  $\sim 1.2-34$  kpc. We note  
 474 that there is also some non-monotonicity, but that this  
 475 can be mostly attributed to the density profile associ-  
 476 ated with these models having irregular inner shapes  
 477 that are not fully described or well-characterized by the  
 478 three-parameter core-Einasto model. This trend contin-  
 479 ues to some extent for one and five bursts. In these  
 480 regimes, there is still a trend where more massive bursts  
 481 lead to larger core radii, but the trend is somewhat less  
 482 pronounced. While the 10, 20, and 31 burst simulations  
 483 each increase the core radius by a factor of five or more,  
 484 the single-burst model increases the core radius from  
 485  $\sim 0.16-0.28$  kpc—less than a factor of two. This result  
 486 is unsurprising given that increasing the mass-per-burst  
 487 directly increases the amplitude of the potential fluctu-  
 488 ations. Notably, the core radii we obtain for models  
 489 with 10 bursts and varying mass expelled per burst of  
 490 0.27 to 7.08 kpc are comparable to those found in the  
 491 FIRE-2 (Hopkins et al. 2018) halos of similar mass in  
 492 Lazar et al. 2020 of 0.28 and 5.09 kpc which also con-  
 493 tain bursty feedback (in which the stellar-to-halo mass  
 494 ratio is increasing between the two rather than the size  
 495 of the fluctuations directly as we model here). For any  
 496 fixed value of the mass expelled per burst, the largest  
 497 cores form for the greatest number of bursts. When the  
 498 mass expelled is held constant at  $3.6 \times 10^6 M_\odot$ , for ex-  
 499 ample, the core radius increases from 0.28 to 3.81 kpc as

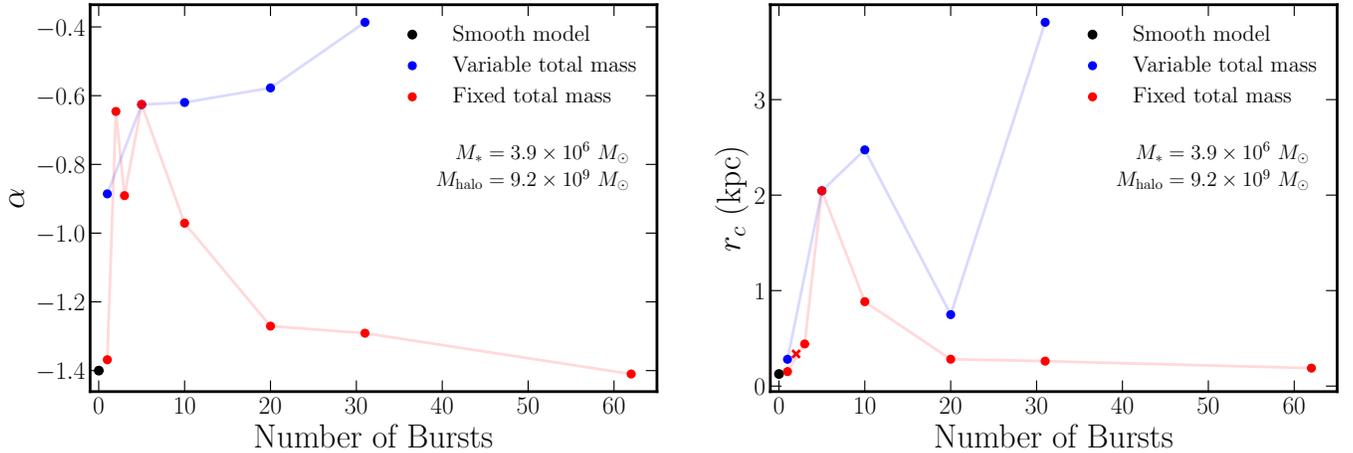
500 the number of bursts increases from 1 to 31. Similarly,  
 501  $\alpha$  increases from  $-0.89$  to  $-0.39$ .

### 502 3.1.2. Constant Total Mass Outflow Models

503 In contrast to the variable total mass outflow models  
 504 considered in the previous subsection, here we hold the  
 505 total mass ejected constant at  $1.8 \times 10^8 M_\odot$  while varying  
 506 the number of bursts between 1–62 and mass-per-burst  
 507 accordingly. The total mass ejected is set to the value  
 508 for the five-burst model shown in Figure 1 because that  
 509 model has a cored present-day density profile. However,  
 510 we note that there is no other reason to choose this  
 511 particular value.

512 In Figure 3, we compare the trends in core radii and  
 513 inner log-slope for these constant total mass models with  
 514 the variable total mass models of the previous section as  
 515 a function of the number of bursts. The blue line depicts  
 516 the results when the total outflow mass varies with the  
 517 number of outflows. Viewing the results in terms of the  
 518 inner log-slope, we observe a monotonic upward trend  
 519 from  $-0.89$  to  $-0.39$  as the number of bursts increases  
 520 from 1 to 31. Viewing the results in terms of the core  
 521 radius, we find a similar trend where the size of the  
 522 core increases from 0.28 to 3.81 kpc. The exception  
 523 to this trend is the twenty-burst model, which has a  
 524 smaller core radius than the ten-burst model. In this  
 525 case, the density profile (not pictured) begins to flatten  
 526 around 2 kpc, but the density increases again at smaller  
 527 radii. As a result, the shape of this profile is not well-fit  
 528 by the three-parameter core-Einasto profile. The trends  
 529 observed with this line are simple to understand: more  
 530 bursts of equal magnitude simply means more potential  
 531 fluctuations capable of impacting the DM particle orbits.

532 The red line depicts the results when the total mass  
 533 expelled is constant. The core radius begins at 0.15 kpc  
 534 for one burst, increases to 2.05 kpc for five bursts, then



**Figure 3.** Comparison of the relationship between number of bursts and both the core size (right) and inner log-slope (left) for variable (blue) versus fixed (red) total energy transferred to the DM particles via bursty feedback for the classical dwarf galaxy. When the amount of mass expelled in each burst is constant, we find that the profile simply becomes more cored as we increase the number of bursts (increasing the total energy transferred). If instead the mass expelled in each burst is varied such that the total mass expelled is constant, we find a more complex relationship. As the number of bursts is decreased, initially this leads to an increase in the core size. However, if there are fewer than five bursts, this trend reverses. The point marked with an “x” indicates that for this model, the core-Einasto fit is poor.

monotonically decreases to 0.19 kpc. The “x” indicates the one point for which a good fit is not obtained. We observe a similar trend in  $\alpha$  for these models:  $\alpha = -1.37$  for one burst, which increases to and peaks at  $-0.63$  for five bursts, then decreases to  $-1.41$  for 62 bursts. The non-monotonicity in this trend from two to three bursts can be explained by looking at the density profiles shown in Figure 4. The two burst model has an inner log-slope and core radius of  $\alpha = -0.65$  and  $r_c = 0.37$  kpc, but these values are more difficult to interpret due to the shape of the density profile. From Figure 4, we can see that the density profile plateaus from 0.5 to 2 kpc, which overlaps with the range where the slope is calculated, but it begins to rise again for smaller radii. This means the calculated value of  $\alpha$  does not completely characterize this density profile and explains the decrease in  $\alpha$  from 2 to 3 bursts we see in Figure 3. In general, though, Figure 3 shows that the dependence of core formation on number of bursts is more complex for the fixed total mass (red) versus variable total mass (blue) models.

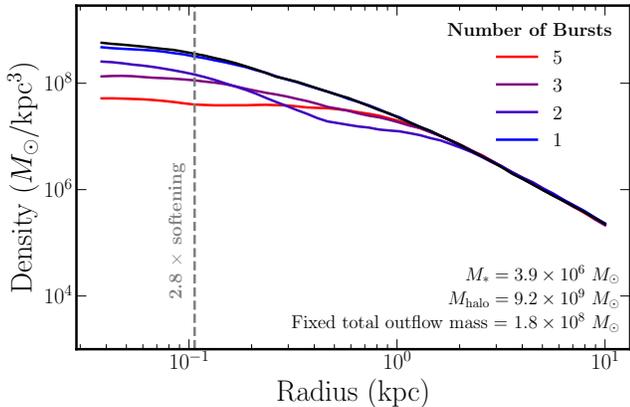
Increasing the number of bursts makes a more cored profile initially, but this reverses after five bursts, which is perhaps unsurprising. Indeed, in our fixed total outflow mass models, the limit of  $N_{\text{bursts}} \rightarrow \infty$  becomes indistinguishable from a smooth model—which we have already demonstrated to form a cusp. What is more surprising is that core formation is mitigated in the limit where the number of bursts approaches only a single event (or very small number of events). To explore this further, we plot the density profiles for the models with constant total outflow mass over 1, 2, 3, and

5 bursts in Figure 4. The most cored profile is produced when the galaxy undergoes five bursts, shown in red, which has a core radius and inner log-slope of 2.05 kpc and  $-0.38$ , respectively. When there are three bursts, the density profile is steeper but still cored with  $\alpha = -0.89$  and  $r_c = 0.44$  kpc. The two and one-burst models, however, produce profiles that are more cusped. As previously mentioned, the two-burst model has a shape that makes the slope shown in Figure 3 less useful as a metric; we can see visually in Figure 4 that it is not cored. Finally, the one-burst model produces a profile nearly indistinguishable from the smooth model, with  $\alpha = -0.83$  and  $r_c = 0.15$  kpc.

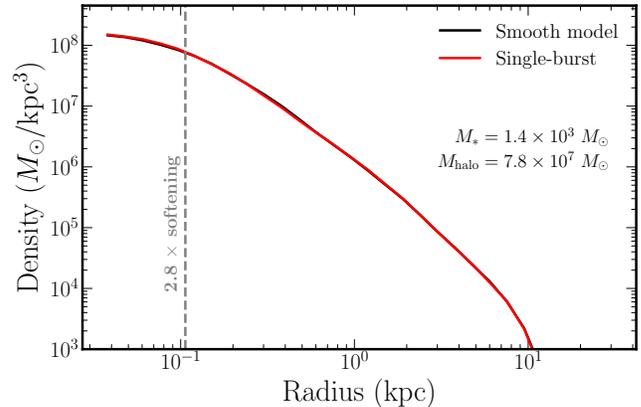
### 3.2. Ultra-Faint Dwarfs

As discussed in §1, some UFD galaxies have been observed (i) to have little variation in their stellar ages, and (ii) to have formed the vast majority of their stellar mass long ago (e.g., Brown et al. 2014; Simon 2019; Galarrut et al. 2021; Sand et al. 2010; Okamoto et al. 2012; Sacchi et al. 2021; Weisz et al. 2014). It has also been suggested that some of these systems have cored DM densities (Almeida et al. 2024). Together, this begs the question: can a single burst, long ago, turn a cusp to a core? The approach we introduce in §2.2 to modeling bursts of star formation allows us to shed light on this question by manually varying the timing and size of such a single outflow event to determine for what values of these parameters a core forms.

In all simulations described below, the galaxy has a final halo mass of  $7.8 \times 10^7 M_\odot$  and to match obser-



**Figure 4.** Present-day density profiles for a fixed amount of total mass expelled ( $1.8 \times 10^8 M_\odot$ ) over time and a varied number of bursts. The black line depicts the smooth model. As the number of bursts decreases (and therefore, the amount of mass expelled per burst increases) larger cores form. However, cores stop forming altogether when the number of bursts becomes very small (i.e.,  $\sim 1$ – $2$ ) despite the large amount of mass being expelled. The gray dashed line indicates the radius at which numerical softening effects begin to impact the results. Note that the results are shown for 1, 2, 3, and 5 bursts (not 4).



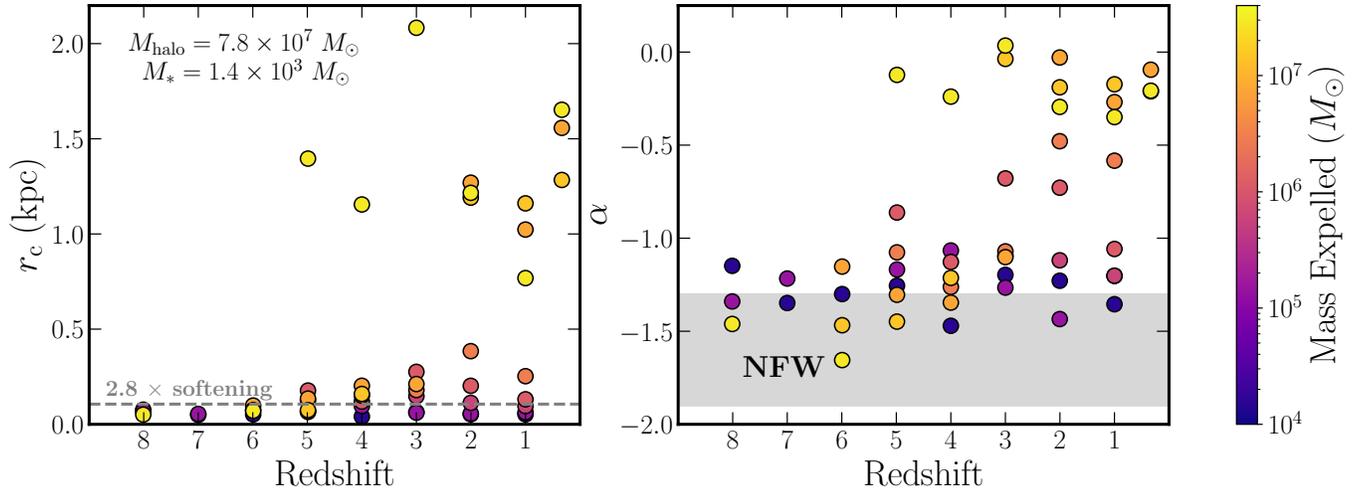
**Figure 5.** Comparison of the present-day DM density profile for an UFD galaxy if it has a smooth growth history (black) or forms in a single burst at  $z = 7$  (red) resulting in the ejection of  $1.4 \times 10^4 M_\odot$ . The density profiles are both cusped with  $r_c = 0.07, 0.05$  and  $\alpha = -1.25, -1.35$  for the smooth-growth and single-burst models, respectively.

596 vational mass measurements of the MW satellites that  
 597 motivated this analysis, we prescribe a final stellar mass  
 598 of  $1.4 \times 10^3 M_\odot$  (Sacchi et al. 2021). We assume that  
 599 all of the ultra-faints have 95% gas fractions prior to  
 600 the burst, such that  $M_{gas} = 1.4 \times 10^4 M_\odot$ . The pre-  
 601 outflow mass ( $M_* + M_{gas}$ ) is then equal to  $1.54 \times 10^4$ .  
 602 We assume all the gas is expelled in the outflow, leaving  
 603 a post-outflow mass of  $1.4 \times 10^3 M_\odot$ . Given that many  
 604 of the UFDs in our Local Group have been observed  
 605 to form  $> 80\%$  of their stellar mass prior to reioniza-  
 606 tion (Sacchi et al. 2021), we begin by testing three single-  
 607 burst models where the outflow from the galaxy occurs  
 608 at  $z = 8, 7$  and  $6$ . We compare the present-day density  
 609 profiles of these models with that of a smooth model  
 610 that also adheres to the aforementioned observational  
 611 constraints on the stellar ages of these systems, as de-  
 612 scribed in §2.3. The tracer mass in this smooth model is  
 613 increased at each timestep such that 80% of the stellar  
 614 mass forms by  $z = 7$  and 90% forms by  $z = 3$ .

615 We find that none of the three single-burst models  
 616 form a core, with  $\alpha$  between  $-1.35$  and  $-1.15$  and  $r_c$   
 617 between  $0.05$  and  $0.08$  kpc. As one example, Figure 5  
 618 compares the density profiles of the smooth model and  
 619 the single-burst model when the outflow occurs at  $z = 7$ .  
 620 In the region to the right of the gray dashed line, which  
 621 indicates the point at which numerical effects begin to  
 622 impact the results, the two profiles are visibly cusped

623 and nearly indistinguishable, as is the case for the mod-  
 624 els with an outflow at  $z = 6$  or  $z = 8$ .

625 Finally, we run a suite of simulations to determine  
 626 at what point, in terms of mass expelled and timing of  
 627 the burst, cores begin to form. The results, in terms of  
 628 the inner log-slope and core radius, are summarized in  
 629 Figure 6 as a function of the time at which the burst  
 630 occurs. The horizontal dashed gray line in the left panel  
 631 indicates the length scale affected by numerical soften-  
 632 ing. A core radius below this should be disregarded,  
 633 since the density profile is artificially flattened in this  
 634 region. The shaded gray band in the right panel indi-  
 635 cates the expected range of values for an NFW (Navarro  
 636 et al. 1996b) profile when accounting for concentration  
 637 scatter found from N-body simulations (Macciò et al.  
 638 2007), calculated using COLOSSUS (Diemer 2018). We  
 639 note that the mass-concentration relation from Macciò  
 640 et al. (2007) was fit on more massive halos than the UFD  
 641 in our simulations. However, we include this shaded  
 642 band not to make detailed quantitative comparisons  
 643 with our results but rather to guide the eye. Whether  
 644 we look at  $r_c$  or  $\alpha$ , it is apparent that outflows prior to  
 645  $z = 5$  impact the DM less than those at  $z \geq 5$ . Prior to  
 646  $z = 5$ , the profiles are all cusped, with negligibly small  
 647 core radii relative to the softening length of the simula-  
 648 tion particles and  $\alpha < -1$ . Outflows at  $z \leq 5$ , however,  
 649 are able to impact the DM density for sufficient mass ex-  
 650 pelled. The earliest outflow to form a core is that with  
 651  $2.9 \times 10^7 M_\odot$  expelled at  $z = 5$ , with  $\alpha = -0.12$  and  
 652  $r_c = 1.40$  kpc. Less massive outflows, however, must  
 653 occur later to have a dramatic impact on the present-  
 654 day density. As one example, an outflow of  $1.2 \times 10^6 M_\odot$   
 655 produces a cored density profile with  $\alpha = -0.68$  and



**Figure 6.** *Left:* Best-fit values for the core radius  $r_c$  as a function of redshift at the time at which the single outflow occurs for the UFD. The color depicts the size of the outflow in terms of the mass expelled. Notably, cores of appreciable size do not form prior to  $z = 5$ , indicating that DM cores do not easily form when bursty activity is relegated to the earliest times, even when extreme mass outflow events are considered. *Right:* Inner DM density profile slope,  $\alpha$ , as a function of redshift at which the single outflow occurs. The shaded band represents the expected range of slopes for an NFW profile (accounting for concentration scatter). Just as with the left panel, the upper left region is unoccupied, showing consistency between these two metrics.

656  $r_c = 0.28$  kpc if the burst occurs at  $z = 3$ . The same  
 657 mass expelled at  $z = 6$  is less impactful, producing a  
 658 density profile with  $\alpha = -0.86$  and a negligibly small  
 659 core radius. We discuss the physical intuition behind  
 660 and implications of these results in §4.

#### 661 4. DISCUSSION

662 In §3.1 we find that our prescriptive approach to mod-  
 663 eling bursty feedback can produce results that are con-  
 664 sistent with literature expectations—by modeling 20  
 665 bursts we find cores of comparable size to those obtained  
 666 in hydrodynamic simulations such as the FIRE-2 simu-  
 667 lations (Hopkins et al. 2018; Lazar et al. 2020). The result  
 668 of varying the total mass ejected from the galaxy (and  
 669 therefore the total energy transferred to the DM parti-  
 670 cles) shown in Figure 2 suggests perhaps how cusped or  
 671 cored the present-day DM density is depends simply on  
 672 the total outflow mass over all bursts. However, we find  
 673 that this is not the case—the efficacy of bursty out-  
 674 flows at modifying the DM density depends on factors  
 675 such as the number of outflow events and, in the case of  
 676 one burst, the timing of the outflow.

677 In Figure 3, we see that even with a fixed total out-  
 678 flow mass, both the core radius and the inner log-slope  
 679 strongly depend on the number of bursts in a non-trivial  
 680 way. Initially, when decreasing the bursts from 62 to  
 681 5, the dominant effect in terms of the strength of core  
 682 formation is the amount of mass being expelled: fewer,  
 683 larger bursts are more impactful. Critically, we find that  
 684 this trend reverses as the number of bursts is decreased

685 further. For fewer than five bursts, the dominant factor  
 686 in determining how many of the inner-region DM parti-  
 687 cles that can be impacted is the number of bursts, not  
 688 the size of them.

689 Figure 6 demonstrates a similar point for the case of  
 690 a single outflow in the UFD regime. While there is a  
 691 strong dependence on the mass of the outflow, as we  
 692 expect from our findings in the classical dwarf regime  
 693 (columns of Figure 2), we also find a dependence on the  
 694 timing of the outflow. A core of appreciable size only  
 695 forms if the burst occurs at  $z < 6$ . Notably, this result  
 696 holds regardless of the total amount of mass expelled,  
 697 even in the case of expelling  $2.9 \times 10^7 M_\odot$ , which is  $> 10\%$   
 698 of the halo mass, and  $\sim 10^4 \times M_*$  at  $z = 0$ . Even in  
 699 this case, a burst at  $z = 5$  forms a core while a burst at  
 700  $z = 6$  does not. In particular, the clear differences that  
 701 we see in the inner log-slopes and core radii for  $z > 5$   
 702 vs  $z \leq 5$  are most likely the result of the major merger  
 703 that occurs between  $z = 6$  and  $z = 5$  for this galaxy.

704 We note that there are some limitations associated  
 705 with modeling the impact of bursty feedback on the DM  
 706 particles in this manner: While we make physical argu-  
 707 ments for the timing and magnitude of the bursts in our  
 708 models, they may not be identical to those that would  
 709 occur in an observed system. We prescribe a set of times  
 710 for which the central potential is changed dramatically  
 711 and suddenly, however, nothing physically causes this  
 712 burst to occur. In particular, we do not impose any  
 713 constraints on the times at which bursts can happen.  
 714 As described in Section 2.2, the list of burst times was

715 created by assuming that a burst happens with temporal  
 716 spacings proportional to the halo dynamical time. One  
 717 potential consequence of this is that the models with a  
 718 larger number of bursts in particular have bursts occur-  
 719 ring later than may be physically realistic.

720 The generalizability of our results is limited in two  
 721 ways. Firstly, we do not vary the formation history (in  
 722 other words, the set of initial conditions) for either halo.  
 723 In the context of the results delineated in Section §3.2,  
 724 this may affect the precise range of times for which a  
 725 single burst can flatten the DM density profile. We  
 726 would not expect this to dramatically affect our qual-  
 727 itative conclusions, though. While the transition in core  
 728 radii/inner log-slope we see in Figure 6 is likely a result  
 729 of the merger that occurs between  $z = 6$  and  $z = 5$ , we  
 730 would expect a similar result for a galaxy with a different  
 731 formation history. This is simply because the earlier an  
 732 outflow occurs, the more likely it is that there is at least  
 733 one major merger after the outflow. Secondly, our simu-  
 734 lations are of field galaxies, not satellites like the UFDs  
 735 in the Local Group which in part motivated the anal-  
 736 ysis. The role of the environment and the impact that  
 737 this may have on our results is yet to be tested, though  
 738 we anticipate that our methods effectively capture the  
 739 physics of episodic/bursty feedback independent of se-  
 740 lected environment.

## 741 5. CONCLUSIONS

742 In this paper, we introduced a novel approach to mod-  
 743 eling the impact of bursty outflows on the orbits of DM  
 744 particles in the inner region of dwarf galaxies to con-  
 745 strain the regimes for which bursty feedback is capa-  
 746 ble of turning cusps to cores. We modeled the gravi-  
 747 tational impact of baryons with a massive tracer parti-  
 748 cle, which allowed us to maintain control over how and  
 749 when these bursty outflows occur within a cosmologi-  
 750 cal environment. This technique sits at the intersec-  
 751 tion of the two avenues bursty feedback has typically  
 752 been studied through: cosmological simulations where  
 753 baryonic processes are modeled explicitly (e.g., [Hopkins  
 754 et al. \(2014\)](#); [Oñorbe et al. \(2015\)](#); [Lazar et al. \(2020\)](#);  
 755 [Chan et al. \(2015\)](#)) and the more controlled analytic  
 756 or idealized modeling of the impact a changing gravi-  
 757 tational potential has on the DM particle orbits (e.g.,  
 758 those of [Pontzen & Governato 2012](#)). Specifically, we  
 759 introduced this method to evaluate the ability of a single  
 760 burst to form cores under realistic conditions for an  
 761 UFD galaxy with a key constraint: the stars form in a  
 762 short period of time and in the early universe. We intro-  
 763 duced two suites of modified DMO simulations: a classi-  
 764 cal dwarf and UFD analog, and studied how varying the  
 765 prescribed evolution of the tracer particle (representing

766 the baryon mass) in a way that corresponds to different  
 767 star formation histories impacted the present-day DM  
 768 density profile. Our key findings are as follows:

- 769 • Our simplified model reproduced the cusp-to-  
 770 core transformation for a galaxy of halo mass  
 771  $\approx 10^{10} M_{\odot}$ , which is the regime where we expect  
 772 this to take place based on the results of hydro-  
 773 dynamic simulations that model baryonic physics  
 774 (including bursty feedback) explicitly ([Chan et al.  
 775 2015](#)). We find our smooth-growth model pro-  
 776 duced a cusp, while our fiducial bursty model pro-  
 777 duced a core.
- 778 • Whether or not a core forms depends on the  
 779 amount of mass expelled in the burst and how  
 780 many bursty outflows there are. When the total  
 781 outflow mass over all bursts is variable, a larger  
 782 number of bursts or a larger outflow mass expelled  
 783 produced a more cored profile at present-day. This  
 784 result was consistent across both metrics that we  
 785 used to quantify the strength of core formation:  
 786 the inner log-slope ( $\alpha$ ) and the best-fit value for  
 787 the core radius ( $r_c$ ).
- 788 • Holding the total mass expelled over all the bursts  
 789 fixed (and therefore holding the total energy trans-  
 790 ferred irreversibly to the DM particles fixed), we  
 791 still found a dependence on the number of bursts  
 792 that the mass is expelled over. We found that for  
 793 five or more bursts, it is more effective to have  
 794 fewer, larger bursts. However, for fewer than five  
 795 bursts, the profiles became cusped once again even  
 796 for extremely large outflows.
- 797 • Applying this method to an ultra-faint galaxy  
 798 analogous to the satellites within our Local Group,  
 799 we found that a single burst was insufficient to  
 800 transform the DM density profile if we made re-  
 801 alistic assumptions about the outflow mass and  
 802 when the burst occurs.
- 803 • By varying the timing and outflow mass of our  
 804 single-burst models, we discovered two barriers to  
 805 core formation in UFDs that form in one, early  
 806 burst: (i) the amount of mass that can be ejected  
 807 must be sufficiently large to impact the DM den-  
 808 sity, and (ii) the outflow must occur sufficiently  
 809 late ( $z < 6$ ).
- 810 • Given that the SFHs of the Local Group satellites  
 811 are largely constrained to before reionization ([Sac-  
 812 chi et al. 2021](#)), the previous point indicates that a

single burst of star formation is insufficient to explain the density profiles of these systems if they are cored as suggested in Almeida et al. (2024).

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*Software:* Astropy (Astropy Collaboration et al. 2013), Matplotlib (Hunter 2007), COLOSSUS (Diemer 2018), AREPO (Springel 2010; Weinberger et al. 2020), MUSIC (Hahn & Abel 2011)

## 7. DATA AVAILABILITY

The data and code used to produce this paper can be made available upon reasonable request to the corresponding author.

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