UTILIZATION OF CLASSIFICATION METHODS ON BRIDGE DATABASES IN VIRGINIA

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ABSTRACT

The National Bridge Inventory (NBI) was created in 1972, and stores all the information collected from these inspections. It is the largest collection of bridge data in the world and contains detailed information on more than 600,000 United States highway bridges and large culverts. Pontis is a bridge management system and product of the American Association of State Highway and Transportation Officials (AASHTO). Pontis has the capability of storing and analyzing bridge inspection and inventory data, recommending optimal preservation policies, predicting needs and performance measures for bridges, and developing projects to include in an agency's capital plan.

Previously, there has been little analysis performed on the VDOT Pontis and NBI from the perspective of data mining; therefore, the objectives of this study are to consolidate and compile multiple bridge data sets, and to discover previously unknown patterns and trends in the data using data mining and classification methods. The scope of the study includes the application of six classification methods on bridge inspection data to determine when certain bridge types will become structurally deficient. Bridge attributes studied include age, average daily traffic (ADT), truck percentage, district, element condition state, and presence of smart flag elements, and the significance of each is discussed.

Overall, classification methods produced strong results as classifiers of structural deficiency of bridges. The comparison of each classification method using the Orange data mining software is conducted and descriptions and performance of bridges in Virginia have been investigated and are presented in the following sections.

iii

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iv

ABSTRACTiii
ACKNOWLEDGEMENTSiv
TABLE OF CONTENTS. v
LIST OF TABLESvii
LIST OF FIGURES viii
INTRODUCTION
Project Development1
Motivation2
Scope and Summary
BACKGROUND
Summary NBI and NBIS4
Summary of Pontis4
Pontis Element Details and Inspection Guidelines6
Data Mining in Bridge Management Systems7
Deterioration Modeling9
Markov Chain Models9
Regression Models11
Model Findings11
METHODS
Data Collection
<i>Element 107</i> 14
<i>Element 109</i>

TABLE OF CONTENTS

<i>Elements 12, 18, 22, 26</i> 17
Classification Methods
Naïve Bayes19
K-Nearest Neighbor
Support Vector Machines
Logistic Regression
Classification Trees
CN2 Rule Learner
Orange Data Mining Software
RESULTS
Significant Attributes
Selecting a Classification Method
CONCLUSIONS
Findings43
Conclusion
Recommendations
REFERENCES
APPENDIX A – ELEMENT CODES AND DESCRIPTIONS
APPENDIX B – NOMOGRAPHS OF LOGISTIC REGRESSION RESULTS

LIST OF TABLES

Table 1: Estimated Service Lives of Selected Elements	10
Table 2: Years to Become Structurally Deficient	11
Table 3: Bridge Types	.13
Table 4: Painted Steel Girder Attributes	16
Table 5: Prestressed Concrete Girder Attributes	.17
Table 6: Deck Element Attributes	18
Table 7: Area Under the Receiver Operating Characteristic Curve Results Summary	36

LIST OF FIGURES

Figure 1: Separating Hyperplane (MathWorks, Inc., 2014)	3
Figure 2: Input Space vs. Feature Space (StatSoft Inc., 2014)	3
Figure 3: Linear regression vs Logistic regression (Sayad, 2012)	5
Figure 4: An example of a data set with three classes labeled 1, 2, and 3 (Loh, 2011) 2	6
Figure 5: Orange Canvas for Bridge Element Data	0
Figure 6: Performance Measures for Painted Steel Girders	2
Figure 7: Receiver Operating Characteristic Curve for Painted Steel Girders	3
Figure 8: Receiver Operating Characteristic Curve for Prestressed Concrete Girders	3
Figure 9: Receiver Operating Characteristic Curve for Bare Concrete Deck (Uncoated Rebar). 3	4
Figure 10: Receiver Operating Characteristic Curve for Concrete Deck (Thin Overlay)	4
Figure 11: Receiver Operating Characteristic Curve for Concrete Deck (Rigid Overlay)	5
Figure 12: Receiver Operating Characteristic Curve for Bare Concrete Deck (Coated Rebar) 3	5
Figure 13: Attribute Influence on Painted Steel Girders	7
Figure 14: Attribute Influence on Prestressed Concrete Girders	7
Figure 15: Attribute Influence on Deck Elements	8
Figure 16: Nomograph of Painted Steel Girders 4	0
Figure 17: CN2 Rules for Painted Steel Girders 4	-1
Figure 18: CN2 Rules for Prestressed Concrete Girders 4	-1
Figure 19: CN2 Rules for Bare Concrete Deck (Uncoated Rebar) 4	-2
Figure 20: CN2 Rules for Concrete Deck (Thin Overlay) 4	-2
Figure 21: CN2 Rules for Concrete Deck (Rigid Overlay) 4	.3
Figure 22: CN2 Rules for Bare Concrete Deck (Coated Rebar) 4	.3

Figure B - 1: Nomograph of Prestressed Concrete Girders	. 58
Figure B - 2: Nomograph of Bare Concrete Deck (Uncoated Rebar)	. 59
Figure B - 3: Nomograph of Concrete Deck (Thin Overlay)	. 60
Figure B - 4: Nomograph of Concrete Deck (Rigid Overlay)	. 61
Figure B - 5: Nomograph of Bare Concrete Deck (Coated Rebar)	. 62

INTRODUCTION

This introduction is divided into three sections. The first section, Project Development, describes how this study came about, the databases utilized throughout this study, and how the advisory groups were formed as a result of various internal forces in the Virginia Department of Transportation (VDOT). The second section, Motivation, presents the incentive behind investigating statistical classification methods to provide an improved forecasting capability for bridge management systems. The final section, Scope and Summary, outlines the mining process and its results.

Project Development

As a result of political and public demands for improved bridge management and inspection practices, the National Bridge Inventory (NBI) and Pontis databases were created in 1972 and 1991, respectively. The use of these databases has allowed the Federal Highway Administration (FHWA) to manage the National Bridge Program and provided them the ability to prioritize and allocate funds based on bridge condition. This project performs data mining utilizing various classification methods on these databases to discover trends in bridge performance across the state of Virginia.

The NBI utilizes general condition ratings (GCR) to describe the condition of 5 major bridge components: superstructures, substructures, decks, channels, and culverts. Inspectors are required to give an average rating that provides an overall indication of the general condition of the entire component based on the National Bridge Inspection Standards (NBIS). The Pontis database breaks down these components further into elements such as steel open girder – painted (element 107) and reinforced concrete pier wall (element 210); a full list of the elements is

available in Appendix A. Pontis stores condition states for each quantity (each, square feet, linear feet) of the elements that comprise a bridge.

Knowledge Discovery in Databases (KDD) is an idea developed by John Tukey where he states, "exploratory data analysis can never be the whole story, but nothing else can serve as the foundation—as the first step" (Tukey, 1977). The methods of KDD, specifically exploratory data mining, and classification methods are predicated on the fact that the user does not necessarily know what the data will tell him/her when beginning the analysis. Therefore, this project reduced the raw Pontis database and NBI database into useable tables to investigate existing trends in bridge performance.

A Bridge Information Systems Laboratory was created to perform research utilizing exploratory data analysis on legacy bridge data in Virginia. This research includes the research performed and completed by Jamie Johnston, a former Master's student at the University of Virginia. The VDOT Technical Advisory Group (TAG) which helps direct the research undertaken by the laboratory include Mr. Adam Matteo, Mr. Jeffrey Milton, Mr. Rex Pearce, Dr. Michael Brown, and Mr. Prasad Nallapaneni. Mr. Todd Springer joined the group in 2014 when he replaced Mr. Nallapaneni.

Motivation

This special study was undertaken by the Virginia Center for Transportation Innovation and Research in Charlottesville, Virginia at the request of the VDOT. The lack of a strong bridge maintenance management system in the state of Virginia has been the driving force for this study, and these models were desired and developed to provide statistical support for a planned proposal of a new Interstate bridge maintenance initiative. The objectives of this special study

were to provide technically sound and statistically valid models to determine the best method for structural integrity classification of Virginia's Interstate bridges.

With previous development of Markov chain and logarithmic regression models to predict deterioration, VDOT's need for further investigation of bridges' structural integrity was improved. Specifically, VDOT desired the ability to predict when bridges would likely become structurally deficient. A structurally deficient bridge has a deck, superstructure, or substructure GCR of 4 or less. Classification methods, a set of data mining techniques, were utilized in this study to determine the best method for forecasting when a bridge will become structurally deficient. They were chosen in order to provide the Department, or anyone, with a statistically significant and easy to understand means of predicting structural deficiency. A number of different classification methods were applied and produced results on bridge data sets derived from the VDOT Pontis and NBI databases.

Scope and Summary

This project focused on the application of various classification methods and on bridge data in the state of Virginia. The project began with a review of exploratory data mining literature and its application (if any) with bridge inspection data, followed by an evaluation and assessment of previously performed deterioration modeling. Next, the selection and application was conducted of classifications methods that were suitable for the requests made by VDOT. Finally, the performance of the different classification methods were evaluated using multiple performance metrics and ultimately one method was chosen as the best classification method to predict bridge structural deficiency.

BACKGROUND

Summary of NBI and NBIS

The NBIS were created in the early 1970s in response to the 1967 failure of the Silver Bridge between West Virginia and Ohio that resulted in the deaths of 46 people (National Transportation Safety Board, 1970). Since, the FHWA has used bridge inspections to determine states' eligibility for federal funding for bridge programs. The NBI was created in 1972, and stores all the information collected from these inspections (Small, Philbin, Fraher, & Romack, 1999). In, 1985, the FHWA initiated a two-phase program to evaluate the utility of various management approaches. Phase one assessed existing state bridge management system (BMS) practices and called for an overall synthesis of fundamental elements of a national BMS. Phase two created a computer tool, eventually named Pontis, which each state could implement to manage its own bridge inventory (AASHTO, Pontis User Manual, Pontis Technical Manual, 2005).

Summary of Pontis

The Pontis is a bridge management system that incorporates a relational database and is a product of the American Association of State Highway and Transportation Officials (AASHTO). Although it has recently been superseded with a newer system, the AASHTO Bridge Manager software, the data utilized for this study was collected using the Pontis system. Pontis has the capability of storing and analyzing bridge inspection and inventory data, recommending optimal preservation policies, predicting needs and, reporting or tracking performance measures for bridges, and aids in developing projects to include in an agency's capital plan (AASHTO, Pontis User Manual, Pontis Technical Manual, 2005); it has been adopted for use by 39 states/territories, 7 other U.S. agencies, and 7 international systems. Pontis is maintained

through AASHTO's joint software development program, which allows agencies to both implement and maintain their inventories more cheaply while maintaining an industry standard of best practice that standardizes bridge management on a national level (Robert, Marshall, Shepard, & Aldayuz, 2003).

The Pontis database for Virginia was created in 1991 in response to the Intermodal Surface Transportation Efficiency Act (ISTEA) which required each state DOT to implement a more functional and detailed bridge management system. It is maintained as a transactional relational database in an Oracle® application that includes records of all bridges across the state since 1995. The NBI inspection program contains ratings of bridges based on bridge components such as deck, superstructure, substructure, channel, and culvert. Under the NBIS, inspectors are required to give an average rating that provides an overall indication of the general condition of the entire component based on NBIS guidelines (Pontis User Manual, 2005).

Because the NBI GCR were determined to be too subjective, Pontis was developed as a more quantitative BMS that looks at structures at the element level. Elements are well-defined subdivisions of bridge components such as girders, joints, and railings, each of which is broken down further by material type. Funding may be more effectively used on maintenance if managers know which specific elements contribute most to deterioration of a bridge.

The NBI database stores condition information on five structural components of a bridge: deck, superstructure, substructure, channel, and culvert. Inspectors assign a condition rating to each of these components on a scale from 9 (perfect) to 1 (severe deterioration). Inspectors using Pontis assign each defined element a condition state on a scale from 1 (perfect) to 3, 4, or 5 (severe deterioration), depending on the element. Bridge inspectors give and overall average

condition rating to bridge components using the NBIS and NBI database. However, those using the Pontis break down the condition assessment into the units each element is assigned.

In Pontis, elements are assigned quantitative units. For example, girders are quantified intervals of linear footage, while elements such as bearings are assigned "each", thereby quantifying the total number of bearings on a given bridge. Using more specific inspection records and guidelines enables the user to truly understand how much of certain elements are in or approaching a deteriorated condition state. Pontis also contains "smart flag" elements. These track certain types of deterioration that are specific to certain elements and are not listed in the structural element condition state definitions. This study investigated the effects of certain smart flags, such as impact damage and steel fatigue, because they have a serious impact on bridge condition and do not necessarily exhibit a logical pattern of deterioration.

Pontis Element Details and Inspection Guidelines

The Virginia Pontis Element Data Collection Manual defines 111 elements and their associated condition states and definitions for bridges in the state of Virginia. The Commonly Recognized (CoRe) elements make up 100 of these elements and have identical definitions between agencies in order to facilitate more uniform data collection and analysis on the national level. The other eleven elements were uniquely defined by VDOT based on particular guidelines defined in the Pontis that allow states to add additional elements to track their condition. Additionally, there are nineteen smart flags recorded in Virginia, eight of which are CoRe while the remaining eleven are uniquely defined by the Virginia DOT. The full list of the 111 elements and nineteen smart flags is presented in Appendix A.

The Pontis Element Data Collection Manual defines the condition state guidelines for the Pontis element-level inspection reporting (VDOT, 2007). Additional guidelines for

responsibility of inspection of state and federal bridges are presented in The National Bridge Inspection Standards (FHWA, 1994). The specific procedures for inspection and reporting are outlined in the AASHTO Maintenance Manual for Roadways and Bridges (AASHTO, 2007), the AASHTO Manual for Bridge Evaluation (AASHTO, 2011), the Recording and Coding Guide (FHWA, 1995), and the Bridge Inspector's Reference Manual (Ryan, Hartle, Mann, & Danovich, 2006). These documents were used as references in this study for their detailed explanation of the different bridge members and their definitions of the associated condition ratings for the superstructure, substructure, and deck.

Data Mining in Bridge Management Systems

Data mining is the analysis of large observational data sets to find unsuspected relationships and to summarize the data in novel ways that are both understandable and useful to the data owner. The application of data mining has become more important with the growth of huge databases as a result of progress in digital data acquisition and storage technology (Hand, Mannila, & Smyth, 2001). The Pontis database and National Bridge Inventory are two of the largest collections of bridge data and there has been very little analysis performed on each from the perspective of data mining.

Transition probabilities and deterioration modeling have been used before to find trends in both of these bridge databases. Samer Madanat refers to Markovian transition probabilities as the expected-value method of condition ratings observed over time. This method contains three important steps: structures are classified into groups containing the same attributes; a deterioration model with condition rating, as the dependent variable, and age, as the independent variable, is estimated; and, a transition probability is estimated (Madanat, Mishalani, & Wan Ibrahim, 1995).

A few years later, Markovian models were used in the state of California to employ a network optimization model for preservation. Cost/benefit models were produced to maintain a program that is optimized with budget constraints that generates project alternatives by combining preservation and improvement needs on each bridge (Thompson, Small, Johnson, & Marshall, 1998). Another study, conducted by Richard Shepard and Michael Johnson (an author to the previous study) in California, takes element-level inspection data from Pontis to determine a bridge's overall economic worth. Then, a single number assessment is determined and The Health Index was created. This index is used to ascertain the structural quality of a bridge and have the ability to make objective comparisons to other bridges (Shepard & Johnson, 2001).

Traditional statistical methods cannot be easily applied to databases with the magnitude of Pontis and NBI and practical hypotheses and significant results may not be derived from these methods. Data mining using classification methods has not been at the forefront of bridge management research, and most bridge analyses rely on the development of deterioration curves. For example, a study in the state of Illinois (Bolukbasi, Mohammadi, & Arditi, 2004) uses two means to construct deterioration curves of state and interstate bridges. The first applies an adjustment in condition ratings based on the notion that unless there is evidence of improvement work, the condition rating cannot be larger than previous ratings, and the second is based on the duration between consecutive inspections.

Few studies have been conducted like the ones above, yet further knowledge of the future condition state of our bridges is highly desired. Therefore, the objectives of this study are to consolidate and compile multiple bridge data sets, and to discover previously unknown patterns and trends in the data using data mining and classification methods.

Deterioration Modeling

Earlier work in Virginia focused on deterioration modelling and is documented in the Exploratory Investigation of Legacy Bridge Databases in Virginia (Johnston, 2013). Initially, two different approaches were taken to develop deterioration models. The first approach used the Pontis element level data and fit Markov Chain models to predict deterioration. The second approach used NBI data and fit logarithmic regression models to predict deterioration for these same bridges. The available data was reviewed and records with inconsistent quantities, too few bridges and unexplained condition improvement were excluded from the study. The bridges with the most prevalent superstructure and deck elements were investigated with ages ranging from 65 years to brand new.

Markov Chain Models

For the Markov Chain model, the proportion of bridges in each of the defined condition states for each element was determined for each age bin. This data was used to fit a Markov Chain deterioration model for each of the six elements identified. It is assumed that the proportion within each condition state will change as the element deteriorates. This change in proportion is considered as a change in the probability that the condition state will take on one of the defined values. This transition was modeled with a Markov Chain, where the probability of the condition state remaining unchanged and the probability of the condition state becoming lower (worsening) is assumed to remain constant for each transition (assumed to occur annually). Using this simple model, the condition state transition probabilities, which resulted in the minimum squared error between a simulation and the observed data, were determined with an Excel worksheet.

Virginia DOT's Technical Advisory Group (TAG) reviewed the Markov model results, and established thresholds which were considered suitable for defining when a particular element has reached the end of its service life. Different percentages for each of the different condition states were defined based upon the TAG's judgment and the condition state definitions. The thresholds and the number of years it would take for a particular element to reach a threshold value, based upon the Markov Chain models are presented in Table 1.

Years to Reach Threshold Values							
Condition	Superstructure	Superstructure	Deck 12	Deck 18	Deck 22	Deck 26	Threshold
State	107	109	Deck 12	Deck 10	Deck 22	Deck 20	mesholu
1	51	>65	23	15	23	36	50%
2	22	>65	10	7	10	16	25%
3	33	>65	31	40	45	40	10%
4	43	>65	37	39	52	33	5%
5	42	N.A.	21	42	38	>65	1%

Table 1: Estimated Service Lives of Selected Elements

The TAG decided that a particular element would need to be replaced if 50 percent of the total quantity of an element was worse than condition state 1, or if 25 percent was in condition state 2 or worse, or if 10 percent was in condition state 3 or worse, or if 5 percent was in condition state 4 or worse, or if 1 percent was in condition state 5.

While, considered useful by the TAG, the Markov Chain models did not immediately provide an estimate of structural deficiency. They also did not provide any indication of uncertainty and modeling error. Another set of models were developed, based upon regression to provide further assistance to the TAG.

Regression Models

The second modeling methodology utilized was to fit a regression model to the NBI general condition ratings for superstructure and deck for the sample bridges. Along with VDOT's desire to be able to estimate the time it would take for a bridge to become structurally deficient, there was a desire to obtain error bounds estimates as well.

For each group of bridges in the sample, using the same age bins as previously, the minimum, maximum and first, second and third quartiles of the NBI general condition rating (GCR) for superstructure or deck were determined as appropriate. There were many age bins where the number of bridges was below 5, and, consequently, the quartile estimates were not reliable. The age bins with a sufficient number of bridges were retained and a weighted linear least squares regression model was used to fit the median GCR to the log-transformed age. A similar procedure was used to define the curves for the first and third quartile estimates.

Based upon the regression models, an estimate of the time it would take for the GCR to become 4 can be estimated. These estimates are presented in Table 2 below.

Time to Become Structurally Deficient						
Element	Superstructure 107	Superstructure 109	Deck 12	Deck 18	Deck 22	Deck 26
Years to SD	>100	>100	100	85	75	>100

Table 2: Years to Become Structurally Deficient

Modeling Findings

Several models were developed which provided the Virginia Department of Transportation forecasting capabilities. These assisted them in developing a new bridge maintenance initiative for Interstate bridges in Virginia. Overall, reasonable deterioration models were developed for the most significant elements present in the Interstate Highway Bridge population in Virginia.

However, by request of VDOT's TAG, further examination was desired for the following reasons. The age of the bridges studied was limited to sixty five years or less. Therefore, any extrapolation beyond this limit must be regarded with skepticism. Also, the data had many instances of missing values. This reflects bridge engineering practice and policies over the sixty five years examined and the resulting models should be used with this knowledge.

Furthermore, in the process, it was found that there is a significant difference between the forecasts developed using element level data from the VDOT Pontis database and models developed using general condition ratings from the NBI database. Therefore, the relationship between the element condition state data and general condition ratings for each of the six elements was examined more closely across the state of Virginia.

METHODS

This section is divided into three sub-sections. The first sub-section, Data Collection, describes how each of the six bridge element data sets were compiled and organized. The second sub-section, Classification Methods, provides an explanation of each of the six classification methods used to investigate the bridge data. The final sub-section, Orange Software, describes the Orange data mining software system utilized in this research and its capabilities and how each classification method is implemented within the program.

The purpose of this study was to use the VDOT Pontis database and NBI database to investigate classification methods and forecast when a bridge will become structurally deficient. As defined by FHWA, a structurally deficient bridge is one with a bridge deck, superstructure, or

substructure reaching a rating of 4 or less. This does not imply that the bridge is unsafe or may collapse; simply that it must be monitored, inspected, and maintained, and that it may be restricted to weight limits, closed to traffic, and/or require significant rehabilitation. The scope of the modelling was limited to bridges in Virginia on the Interstate system.

Bridge data sets were compiled for six different elements. These data sets were comprised of attributes including age, the district it is located in, average daily traffic (ADT), truck percentage, a condition state profile (defined below for each element), and applicable smart flags that may be present. A current classification of each bridge's general condition rating (GCR) from the NBI was also included in the data sets to be compared with predicted classification values. The superstructure GCRs were compared for the substructure elements, while the deck GCRs were compared for the deck elements.

Data Collection

Bridge data sets were compiled based on element type, and the same six elements were investigated for this study as previously done for the deterioration modelling.

Bridge Type	Element #
Painted Steel Girders	107
Prestressed Concrete Girders	109
Bare concrete decks with uncoated rebar	12
Concrete deck with thin overlay	18
Concrete deck with rigid overlay	22
Bare concrete deck with coated bars	26

 Table 3: Bridge Types

All Interstate bridges containing painted steel girders, element 107, (and each additional element) were sorted by bridge key, a unique identification number assigned to each bridge, and inspection date. The inspection records contain element condition states (1-5 rating) reported by inspectors over the years. In most cases, inspections on each bridge were performed every two

years; however, some bridges had more frequent inspections while some inspections were greater than five years apart. The scope of this study focused on the two most recent inspections for each bridge. The data collection process for each element is provided below and presents the element condition state descriptions as defined by the VDOT Pontis Manual.

Element 107

As defined in VDOT's Element Level Coding Guide, painted steel superstructures include two girder systems as well as rolled beams on multiple spans. The data set was compiled of bridges in which the structure carried only Interstate routes; it consisted of a total of 546 bridges. In order to facilitate classification, "condition state profiles" were created. A letter grade was assigned based on the certain percentages in each condition state. An "A" was given to inspections containing the entire quantity in condition state 1, a "B" to those having partial quantities in condition state 2, a "C" to those having partial quantities in condition state 3, and a "D" to those having any quantity in condition state 4 or worse.

Element 107 condition state descriptions:

1	There is no evidence of active corrosion and the coating system is sound and
	functioning as intended.
	For coated cables, the protective coating is sound and functioning as intended,
	For coated cables, the strand and anchor sockets show no signs of distress.
2	There is little or no active corrosion.
	Surface or freckled rust has formed or is forming.
	The coating system may be chalking, peeling, curling or showing other early
	evidence of coating system distress but there is no exposure of metal.
	For coated cables, the strand and anchor sockets show no signs of distress.
3	Surface or freckled rust is prevalent.
	There may be exposed metal but there is no measurable section loss caused by
	active corrosion.
	For coated cables, protective system is no longer effective.
	For coated cables, the strand and anchor sockets show no signs of distress.
4	Corrosion is present.
	Section loss due to active corrosion does not warrant structural analysis.
	For coated cables, the cable banding, if any, may show some loosening or
	slippage.
	For coated cables, the cable anchor devices may be loosening.
	Also code Element 363 (Section Loss).

5 Corrosion is advanced.

Section loss due to active corrosion is sufficient to warrant structural analysis.For coated cables, the cable strands or wires may be broken or severely abraded.For coated cables, the anchors may show signs of slippage.Also code Element 363 (Section Loss).

This type of structure warranted the investigation of certain smart flag elements. Therefore, steel fatigue, traffic impact damage, and section loss were also taken into account. Letter grades were assigned for smart flag elements which contain quantities in entire condition states. An "A" was given in the presence of no smart flags, a "B" to those in condition state 1, a "C" to those in condition state 2, and a "D" to those in condition state 3. The attributes investigated for element 107 are listed in Table 4.

Steel Fatigue (smart flag 356) condition state descriptions:

- N No presence of fatigue damage.
- 1 Fatigue damage to the bridge has been repaired or arrested. The bridge may still be fatigue prone.
- 2 Fatigue damage exists which is not arrested.
- 3 Fatigue damage exists which is sufficient to warrant structural analysis.

Traffic Impact Damage (smart flag 362) condition state descriptions:

- N No presence of impact damage.
- 1 Impact damage has occurred and has been repaired. Prestressing system is covered by patch concrete. Steel has been straightened or repaired.
- Impact damage has occurred.
 Prestressing system is exposed, but is not impaired.
 Steel condition does not threaten the ability of the bridge to function as intended.
- 3 Impact damage has occurred and strength of the member is impaired. Impact damage is sufficient to warrant structural analysis.

Section Loss (smart flag 363) condition state descriptions:

- N No presence of section loss.
- 1 Section loss has been repaired or cleaned and coated over.
- 2 Section loss exists and has not been repaired or coated over. Structural analysis is not yet warranted.
- 3 Section loss exists which is sufficient to warrant structural analysis or an analysis has determined that the ability of the bridge to function as intended has not been affected.
- 4 Section loss has affected the load carrying capacity or the ability of the bridge to function as intended.

Painted Steel Girder Attributes
Age
District
Average Daily Traffic (ADT)
Truck Percentage
Condition State Profile
Steel Fatigue – SF 356
Traffic Impact Damage – SF 362
Section Loss – SF 363
Table 4: Deinsted Steel Cinden Attributes

 Table 4: Painted Steel Girder Attributes

Element 109

The prestressed concrete girder data set was expanded from Interstate bridges to all state maintained bridges in Virginia because there were too few structurally deficient bridges in the Interstate sample. This increased the sample size to allow for stronger model development; it consisted of a total of 473 bridges. Similar to element 107, the inspection quantities were in multiple condition states, and "condition state profiles" were also created based on the same criteria. These profiles also ranged from A-D.

Element 109 condition state descriptions:

- 1 Little or no deterioration. There may be discoloration, efflorescence, and/or superficial cracking but without effect on strength and/or affecting the ability of the element to function as intended.
- Minor deterioration.
 Hairline cracks & spalls may be present and there may be exposed reinforcing with no evidence of corrosion.
 There is no exposure of the prestressed system.
 Moderate deterioration.
 Some delaminations and/or spalls may be present.
 There may be minor exposure but no deterioration of the prestressed system.
 Corrosion of non-prestressed reinforcement may be present but loss of section is incidental and does not warrant structural analysis.
 Advanced deterioration.
 Delaminations, spalls and corrosion of non-prestressed reinforcement are
 - Detaininations, spans and corrosion of non-prestressed remorcement are prevalent.
 There may also be exposure and deterioration of the prestressed system (manifested by loss of bond, broken strands or wire, failed anchorages, etc.).
 There is sufficient concern to warrant structural analysis.

The prestressed concrete structure only warranted the investigation of one smart flag: traffic impact damage. The same criteria and smart flag mapping were used as with element 107. The attributes investigated for element 109 are listed in Table 5.

Prestressed Concrete Girder Attributes
Age
District
Average Daily Traffic (ADT)
Truck Percentage
Condition State Profile
Traffic Impact Damage – SF 362

Table 5: Prestressed Concrete Girder Attributes

Elements 12, 18, 22, and 26

All decks in this study were reinforced concrete decks. Similar to element 109, the scope of each of the deck data sets was expanded to all state maintained bridges in Virginia. The data sets of elements 12, 18, 22, and 26 consisted of 1,338, 787, 403, and 1,575 bridges, respectively. The inspection records of the deck elements are coded as "each;" therefore, condition state profiles weren't necessary, and condition states were directly mapped. For example, condition state 1 received an "A", condition state 2 received a "B", and so forth.

Concrete Deck condition state descriptions:

- 1 This element exhibits no patched areas and/or deficiencies such as spalling, delamination, etc.
- 2 Patched areas, spalling/delamination and/or potholes exist. Their combined area is 10% or less of the total deck area.
- 3 Patched areas, spalling/delamination and/or potholes exist. Their combined area is more than 10% but 25% or less of the total deck area.
- 4 Patched areas, spalling/delamination and/or potholes exist. Their combined area is more than 25% but less than 50% of the total deck area.
- 5 Patched areas, spalling/delamination and/or potholes exist. Their combined area is 50% or more of the total deck area.

The reinforced concrete decks warranted the investigation of two smart flag elements. Therefore, deck cracking and soffit of concrete decks/slabs were taken into account. The same smart flag mapping was performed for the deck element as above, and the attributes investigated for these elements are listed in Table 6.

Deck Cracking (smart flag 358) condition state descriptions:

- N No presence of deck cracking
- 1 The surface of the deck is cracked, but the cracks are either filled/sealed or insignificant in size and density (cracks less than 1/16 inch in width and spaced greater than 10 feet apart).
- 2 Unsealed cracks exist which are of moderate size OR density (cracks greater than or equal to 1/16 inch and less than 3/16 inch in width OR where cracks are spaced 5 feet to 10 feet apart).

- 3 Unsealed cracks exist in the deck that are of moderate size AND density (cracks greater than or equal to 1/16 inch and less than 3/16 inch in width AND where cracks are spaced 5 feet to 10 feet apart).
- 4 Unsealed cracks exist in the deck that are of severe size AND/OR density (cracks greater than 3/16 inch in width AND/OR are spaced less than 5 feet apart).

Soffit of Concrete Decks/Slabs (smart flag 359) condition state descriptions:

- N No presence of concrete soffit
- 1 There are few symptoms of distress and any cracking or efflorescence is less than 2% of the total underside area.
- 2 Cracking and/or efflorescence is light any the combined distressed area is 2% to 10% of the soffit.
- 3 Moderate efflorescence and/or cracking (cracks greater than or equal to 1/16 inch and less than 3/16 inch in width OR where cracks are spaced 5 feet to 10 feet apart) and the combined distressed area is greater than 10% but 25% or less of the soffit.
- 4 Light to moderate rust staining and/or delamination/spalling and heavy cracking (cracks greater than or equal to 1/16 inch and less than 3/16 inch in width AND where cracks are spaced 5 feet to 10 feet apart) and/or efflorescence and the combined distressed area is more than 25% but less than 50% of the soffit.
- 5 Heavy to severe rust staining and/or delamination/spalling and severe cracking (cracks greater than 3/16 inch in width AND/OR are spaced less than 5 feet apart) and/or efflorescence and the combined distressed area is 50% or more of the soffit.

Deck Element Attributes
Age
District
Average Daily Traffic (ADT)
Truck Percentage
Condition State Profile
Deck Cracking – SF 358
Soffit of Concrete Decks/Slabs – SF 359

Table 6: Deck Element Attributes

Classification Methods

Multiple classification methods were investigated and utilized in this study to determine the best method for forecasting when a bridge will become structurally deficient. Each bridge data set was used as an input for six different classification methods: naïve Bayes, *k*-nearest neighbor, support vector machine, logistic regression, classification tree, and the CN2 rule learner. The classification methods developed and produced "classifiers" based on the attributes for each bridge. These attributes were used to determine a prediction of "structurally deficient" or "not structurally deficient" for each bridge. Comparisons of these predictions were made to those of the current classifications.

Each classification method produces a classification model, "classifier", providing a prediction of structural deficiency. In pattern recognition and statistical classification, a classifier is a distinct algorithm or precise function that maps input data into a category (Jain, Duin, & Mao, 2000).

Naïve Bayes

A naïve Bayes classifier is a probabilistic classifier based on the application of Bayesian statistics and the assumption of independent features. This means that the classifier assumes that each individual feature is unrelated to the others. Naïve Bayes has been used for pattern recognition and information retrieval for almost forty years (Lewis, 1998). Although independence is commonly a poor assumption, the naïve Bayes classifier has advantages that allow it to compete well against more sophisticated classifiers. Its ability to undertake a high dimensionality of inputs and handle an arbitrary number of independent variables regardless of type (e.g., categorical or continuous) are two of its major advantages (Rish, 2001).

The basic theory of naïve Bayes classifier is presented. First, consider how to design a learning (or training) algorithm based on Bayes rule in which an unknown target function $f: X \rightarrow Y$, equivalently P(Y|X), or the probability of Y given a known X is approximated. In order to reduce the complexity of the Bayesian classifiers, the assumption of conditional independence is used which dramatically reduces the number of parameters. For example, given random

variables *X*, *Y* and *Z*, variable *X* is conditionally independent of *Y* given *Z*, if and only if the probability distribution governing *X* is independent of the value of *Y* given *Z*; that is:

$$(\forall i, j, k)P(X = x_i | Y = y_j, Z = z_k) = P(X = x_i | Z = z_k)$$
Eq. 1

To describe conditionality further, consider the current weather: *Rain, Thunder*, and *Lightning*. The presence of *Thunder*, in this example, is independent of *Rain* given the presence of *Lightning*. We know that *Lightning* causes *Thunder*, and once we know whether or not there is currently *Lightning*, no additional information about *Thunder* is provided by the value of *Rain*. Certainly there is a clear dependence of *Thunder* on *Rain* in general; however, there is no conditional dependence after the value of *Lightning* is known (Mitchell, 2010).

The Bayes rule, defined as P(Y|X), contains the attributes $X_1...X_n$ that are all independent of one another. This assumption drastically simplifies the representation of P(Y|X) and makes the problem of estimating it from the training algorithm easier. Consider the simple case where $X = \{X_1, X_2, X_3\}$. In this case:

$$P(Y|X_1...X_3) = P(Y) P(X_1...X_3|Y)$$

= P(Y) P(X_1|Y) P(X_2...X_3|Y, X_1)
= P(Y) P(X_1|Y) P(X_2|Y, X_1) P(X_3|Y, X_1, X_2)
Eq. 2

Since Bayes rule assumes conditional independence, assume each attribute X_i is conditionally independent to the next X_j for $j \neq i$ given the category Y. Therefore the joint model may be expressed as:

$$P(X_1...X_3|Y) = P(Y, X_1, ..., X_3)$$

= P(Y) P(X_1|Y) P(X_2|Y) P(X_3|Y)

This series of equations may be expressed more generally as:

$$P(X_1 \dots X_n | Y) = P(Y) \prod_{i=1}^n P(X_i | Y)$$

Eq. 4

Eq. 3

K-Nearest Neighbor

The *k*-nearest neighbor (kNN) rule is a non-parametric technique, that is it does not assume that the model has a fixed size and that it can change with the complexity of the data, used in statistical estimation and pattern recognition by an algorithm that stores all available cases and classifies new cases based on similarity measures or distance functions (Weinberger, Blitzer, & Saul, 2005). Unlike other common classifiers, the kNN rule does not build a classifier in advance; each new sample finds the *k* neighbors nearest it from training space based on the attributes and a distance metric (Khan, Ding, & Perrizo, 2002).

Before determining the proper distance metric, the first step in k-nearest neighbor classification is choosing an appropriate k value. The nature and size of the data ultimately determines the optimal value for k. Using a k value that is too large may include data points that are not as similar; however, using a small k value may exclude some significant data points. After trial and error testing, a k value of 5 was chosen for this study as it produced the strongest results and is the most appropriate for the sample size while maintaining significant results.

Next, the appropriate distance metric is chosen. The performance of *k*-nearest neighbor classification is highly dependent on the distance metric chosen to identify nearest neighbors. Distance metrics for kNN classification are tailored to specific problems and change when the

desired resultant class changes. For example, the optimal distance metric used to investigate gender identification is most likely not the same distance metric used to study face recognition. There are four main distance metrics:

Euclidean:	$d(x,y) = \sqrt{\sum_{i=1}^{n} (x_i - y_i)^2}$
Hamming:	$d(x,y) = \sum_{i=1}^{n} (x_i \neq x_j)$
Manhattan:	$d(x,y) = \sum_{i=1}^{n} x_i - y_i $
Maximal:	$d(x, y) = \max(x_i - y_i)$

The Hamming distance is not suitable for continuous data and utilizes the number of attributes in which two examples differ. The Manhattan distance calculates the sum of absolute differences for all attributes while Maximal distance calculates the maximal difference between attributes. The Euclidean distance metric is used in the most simple kNN classifications and was selected for this study because of its simplicity under the assumption of an absence of prior knowledge about the data sets.

Support Vector Machines

Support vector machines (SVMs) classify data into two classes by finding the best decision plane (or hyperplane) that separates all data points between a set of objects having different class memberships. SVM is known to be especially efficient in handling large classification problems due to its ability to manage very large feature spaces (Widodo & Yang, 2007).

The best plane for SVMs is the one with the largest margin, or maximum width of margins away from the hyperplane, between the two classes (MathWorks, Inc., 2014). Figure 1 depicts a schematic example of a linear hyperplane between two classes: positive and negative

data points. The support vectors are those data points closest to the hyperplane that lie directly on the margin boundary.

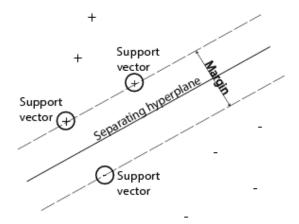


Figure 1: Separating Hyperplane (MathWorks, Inc., 2014)

Most cases, however, do not yield a perfectly linear relationship. Therefore, a set of mathematical functions, known as kernels, are used on input space objects to rearrange and map them into a feature space (StatSoft Inc., 2014). The mapping transformation is performed to utilize a linear separating hyperplane rather than a more complex curved hyperplane relationship. Figure 2 shows how mapping is used to transform input space to feature space. The test object (white circle) is classified correctly based on the proper mapping of the training objects (red and green circles).

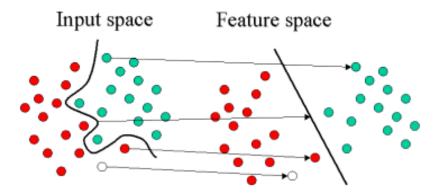


Figure 2: Input Space vs. Feature Space (StatSoft Inc., 2014)

The four basic kernel functions are:

Linear:	$K(x_i, x_j) = x_i x_j$
Polynomial:	$K(x_i, x_j) = (\gamma x_i x_j + c)^d$
Radial Basis Function (RBF):	$K(x_i, x_j) = e^{(-\gamma x_i x_j ^2)}, \gamma > 0$
Sigmoid:	$K(x_i, x_j) = \tanh(\gamma x_i x_j + c)$

The radial basis function was the chosen kernel for this study. It, unlike linear relationship kernels, handles cases in which the relationship between attribute and class is nonlinear (Hsu, Chang, & Lin, 2003), much like the nature of bridge inspection data. Additionally, the decision to utilize the RBF kernel was reached because the number of parameters influences the complexity of model selection; RBF uses fewer parameters than the

where, γ , c, and d are kernel parameters.

polynomial and sigmoid parameters. The gamma, γ , parameter used in RBF is recommended to be 1/k, where *k* is the number of attributes used for each data set.

Logistic Regression

Logistic regression is another classification method and statistical model that utilizes a series of predictor variables that influence the probability of an outcome. The difference between it and ordinary linear regression is that logistic regression contains a value predictor that is binary and dichotomous. Therefore, in order for a logistic regression to be applied, modifications to the equation are made to express the outputs in terms of probability:

$$\log\left(\frac{p}{1-p}\right) = \beta_o + \beta_1 X_1 + \dots + \beta_i X_i$$

Eq. 5

where *p* is the probability of the outcome of interest, β_i coefficients are associated with each variable and calculated to minimize error, and X_i are the values of the potential predictor variables, such as age of the bridge, its location, etc. (Tu, 1996). Figure 3 below depicts the difference between linear regression and logistic regression.

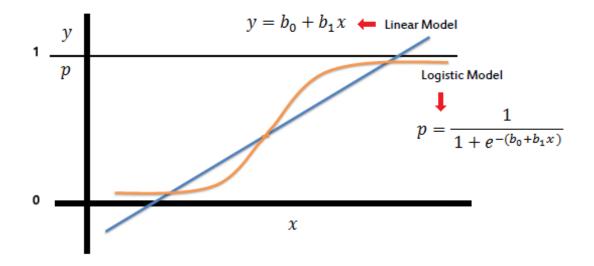


Figure 3: Linear regression vs Logistic regression (Sayad, 2012)

The assumption is that the predictor variables, *Xi*, are related linearly to the odds of $log\left(\frac{p}{1-p}\right)$ for the outcome of interest (Ottenbacher, Linn, Smith, Illig, Mancuso, & Granger, 2004), and that there exists a hyperplane, or decision boundary, of all points *X_i* that separates successful events from failed events (Dreiseitl & Ohno-Machado, 2002).

Logistic regression may also be expressed as an *odds* function that an event *E* occurs:

$$Odds(E) = \frac{p(E)}{p(E')} = \frac{p(E)}{1 - p(E)}$$

Eq. 6

Here, the *odds* function can be transformed by taking the natural log of both sides to yield:

$$ln\frac{p(E)}{1-p(E)} = lnp(E) - \ln(1-p(E)) = e^{\beta_0 + \beta_1 X_1 + \dots + \beta_i X_i}$$
Eq. 7

Now, the event *E* is a dependent variable that takes on the values of 0 or 1 (Zaiontz, 2014). In this study, when the Odds(E) > 0.5; the bridge will be classified as structurally deficient; otherwise, the bridge is classified as not structurally deficient.

Classification Trees

Classification trees (or regression trees) are rules that are developed for predicting the class of an object from the values of its predictor variables. They are a machine-learning classification method in which prediction models are obtained by recursively partitioning a learning sample of the data in which the predictor values and label classes are already known for each case. These partitions are signified by a node in the "tree" (Loh, 2011, Loh & Shih, 1997). Figure 4 displays an example of a partitioned data set where the variables get assigned to the left node at each intermediate node when the specified condition is satisfied.

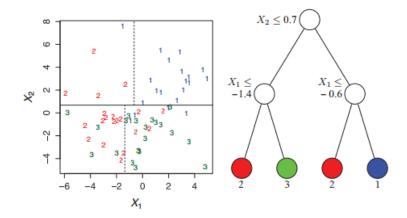


Figure 4: An example of a data set with three classes labeled 1, 2, and 3 (Loh, 2011)

Gini index, a way of selecting attribute criterion, was chosen for this study as it is a way of measuring inequality (Loh, 2011, Langel & Tillé, 2013). It is appropriate for our data divided into two classes as it generalizes a binomial variance. The empirical Gini index, defined in Equation 8, considers a variable X_j in the special case of binary response Y. The relative class frequency, N_{2j}/N_j , is the maximum likelihood estimator based on the number of observations indicated by the index *j* (Strobl, Boulesteix, & Augustin, 2007).

$$G_j = 2\frac{N_{2j}}{N_j} \left(1 - \frac{N_{2j}}{N_j}\right)$$

Eq. 8

The data are then subjected to pre-pruning to keep results simple and easy to comprehend, and a minimum number of instances is set that each "leaf" must contain. The data are then post-pruned in two ways. First, the leaves are recursively merged with the same majority class. This reduces overfitting by generating the whole set of classification rules and then removing a number of rules and terms. This will prevent trees from becoming too large and difficult to grasp (Bramer, 2002). Secondly, the data is post-pruned using an m-estimate statistic. This estimate takes into account prior unconditional probabilities of classes and contains a tunable parameter *m*, which allows for adaptation based on noise level of the data (Dzeroski, Cestnik, & Petrovski, 1993). The default m-estimate of 2 was used for this study.

<u>CN2</u>

The CN2 rule learner and induction algorithm was developed in the 1980s based on previous classification processes; namely, the Iterative Dichotomiser 3 (ID3) and Algorithm quasioptimal (AQ) algorithms. The ID3 algorithm is applied to a set of data and generates a decision tree for classifying the data based on attribute selection by information gain (Umano, Okamoto, Hatono, Tamura, Kawachi, Umedzu, & Kinoshita, 1994). The AQ algorithm is a rule induction technique that produces a complete and consistent description of classes (Michalski, Mozetic, Hong, & Lavrač, 1986).

These older algorithms are far more basic and assume no noise in the data. The CN2 technique uses an if-then rule that was designed to modify and combine each of these algorithms to handle real-world domains by relaxing certain constraints that the induced description must classify the training data perfectly (Clark & Niblett, 1989).

The nature of the ID3 algorithm allows for relative easy modification, while the AQ algorithm is more difficult to modify due to its dependence on specific training examples during search. The goals of the CN2 algorithm are to increase the space of rules searched, ensure accurate classification with simple rules, and utilize an efficient and simple to understand rule generation (Clark & Niblett, 1989).

The CN2 algorithm utilizes three possible evaluation functions for implementation: the Laplace function, used in the original CN2 algorithm; the m-estimate of probability, used in more recent versions of the CN2 algorithm; and the weighted relative accuracy (WRACC) function, used in the CN2-SD algorithm.

The CN2-SD (subgroup discovery) is a modified version of CN2 that improves its evaluation measures and covering algorithm. The search methods and classification of instances were both adapted to reduce the number of induced rules and increase both rule coverage and rule significance. Therefore, due to its utilization with CN2-SD, the WRACC function was chosen for this study:

$$WRACC(Class \leftarrow Cond) = p(Cond) * (p(Class|Cond) - p(Class))$$

Eq. 9

where *Class* is the class value and *Cond* are feature attributes and their values (Lavrač, Kavsek, Flach, & Todorovski, 2004).

Next, pre-pruning rules are defined. Likelihood ratio statistics (LRS) parameters are used at a 5% significance rating, while 10% weighted covering of the data was implemented.

Orange Data Mining Software

The six classification methods used in this study are implemented in a data mining and machine learning software called Orange. This comprehensive, component-based framework helps experienced researchers and beginners to perform data processing, modelling, and evaluation in many facets. Orange's capabilities include:

- Data management and preprocessing, like sampling, filtering, scaling, discretization, and construction of new attributes
- Induction of classification methods and regression models
- Descriptive methods like association rules and clustering
- Scoring of prediction models, including different hold-out schemes and range of scoring methods and visualization approaches.

Orange utilizes a visual programming paradigm and the graphical user's interface (GUI) is composed of multiple widgets that communicate through channels. Connected widgets, called a schema, can be written in a Python script or designed through a visual programming interface called Orange Canvas (Demšar, Zupan, Leban, & Curk, 2004). For this study, the Canvas reads in the bridge element data sets as inputs, performed various machine learning classifications, and produced evaluations on the data.

RESULTS

Six different classifications using six different methods were conducted for each of the elements; steel open girder – coated (element 107), prestressed concrete open girder (109), bare concrete deck with uncoated reinforcement (12), concrete deck with then overlay (18), concrete deck with rigid overlay (22), and bare concrete deck with coated reinforcement (26). For each of the bridge data sets, six classification methods were applied; naïve Bayes, *k*-nearest neighbor, support vector machines, logistic regression, classification trees, and the CN2 rule learner. The classification methods developed and produced results based on the attributes for each bridge. These attributes determined a prediction of "structurally deficient" or "not structurally deficient" for each bridge. Figure 5 displays the interface for each of the data sets.

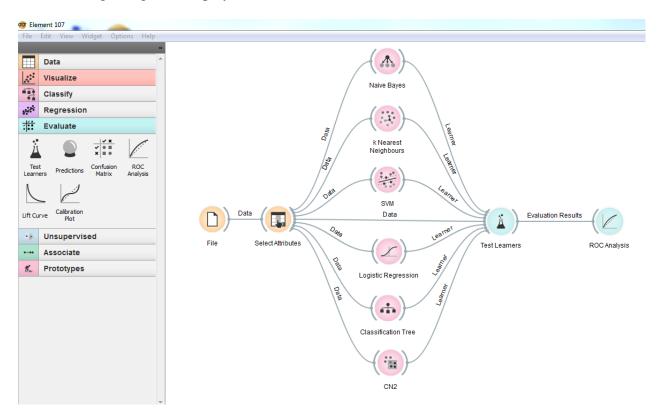


Figure 5: Orange Canvas for Bridge Element Data

The Orange software contains many performance measures that report how well each classification method performed. These include:

- Classification accuracy the proportion of correctly classified examples
- Sensitivity (also called true positive rate, hit rate, and recall) the number of detected positive examples among all positive examples, e.g. the number of structurally deficient bridges correctly classified as structurally deficient
- Specificity the proportion of detected negative examples among all negative examples, e.g., the proportion of not structurally deficient bridges correctly recognized as not structurally deficient
- Area under the ROC the area under the receiver-operating characteristic curve
- Information score the average amount of information per classified instance
- F-measure a weighted harmonic mean of precision and recall, calculated as 2*precision*recall/(precision+recall)
- Precision the number of positive examples among all examples classified as positive, e.g. the number of structurally deficient bridges among all diagnosed as structurally deficient
- Recall same as sensitivity, except that it is the proportion of relevant documents which are retrieved
- Brier score the measure of accuracy of probability assessments, which measures the average deviation between predicted probabilities of events and actual events

Figure 6 displays all nine performance measures for steel open girders – coated (element 107). The receiver operating curve (ROC) illustrates the performance of a binary classifier system as its discrimination threshold is varied (Swets, 2014). Receiver operating curve points

are produced by a maximum likelihood estimation and two parameters, the difference of means and the ratio of variances, are obtained. A number of indices can be calculated from these parameters; among which the area under the fitted smooth curve is the most popular (Hanely & McNeil, 1982). The curve is plotted of the false positive rate (x-axis) against the true positive rate (y-axis), known as recall for machine learning purposes. The higher, and closer to 1, the area under the ROC curve is, the better that classification method is at predicting structural deficiency of bridges. Area under the ROC curve was chosen as the most useful performance measure for this study. First, it is easily conveyed and understood, and, secondly, Orange has the ability to produce ROC plots for each classification method (Figures 7-12).

Sampling	Ev	aluation Results				\wedge					
Oross-validation		Method	CA	Sens	Spec	AUC	IS	F1	Prec	Recall	Brier
Number of folds: 5	1	Naive Bayes	0.9667	0.9794	0.6207	0.9463	-0.0832	0.9827	0.9859	0.9794	0.0563
Leave-one-out	2	Logistic regression	0.9760	0.9937	0.4966	0.9710	0.0172	0.9876	0.9817	0.9937	0.0374
Random sampling	3	SVM	0.9838	0.9947	0.689	0.9840	0.1135	0.9916	0.9886	0.9947	0.0301
Repeat train/test: 10 🚔	4	Classification Tree	0.9917	0.9957	0.8828	0.9686	0.1709	0.9957	0.9957	0.9957	0.0150
Relative training set size:	5	CN2 rules	0.9880	0.9944	0.8138	0.9654	0.1444	0.9938	0.9932	0.9944	0.0207
70%	6	kNN	0.9912	0.9962	0.8552	0.9805	0.1605	0.9954	0.9947	0.9962	0.0144
						V					

Figure 6: Performance Measures for Painted Steel Girders

As displayed in the figure above, the support vector machines classification method produces the highest area under the ROC curve for element 107. Subsequent analysis of each of the bridge elements was conducted, and the area under the ROC curve was the only performance measure used to evaluate performance.

Figures 7-12 display the ROC curves for each of the six elements studied. Within each of the figures, each of the six classification method curves is shown and results are compared. Table 7 following the curves summarizes the results of each element.

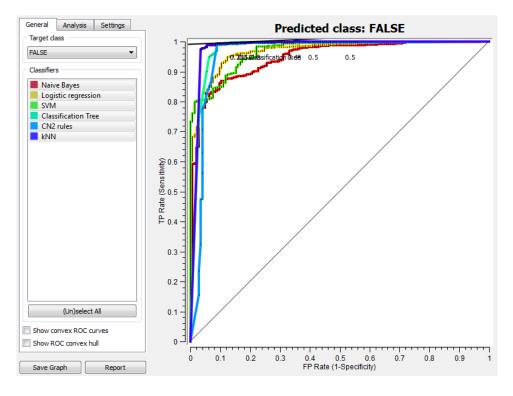


Figure 7: Receiver Operating Characteristic Curve for Painted Steel Girders

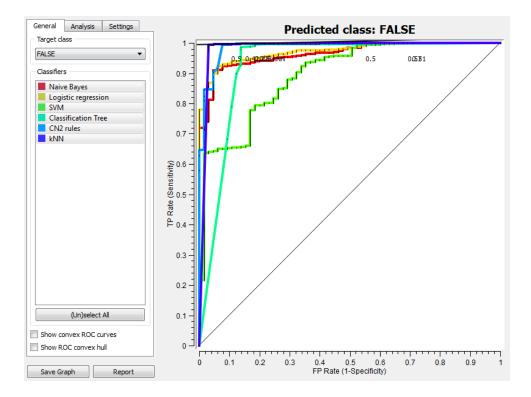


Figure 8: Receiver Operating Characteristic Curve for Prestressed Concrete Girders

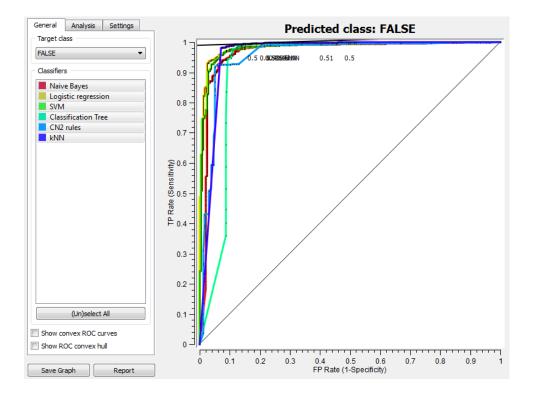


Figure 9: Receiver Operating Characteristic Curve for Bare Concrete Deck (Uncoated Rebar)

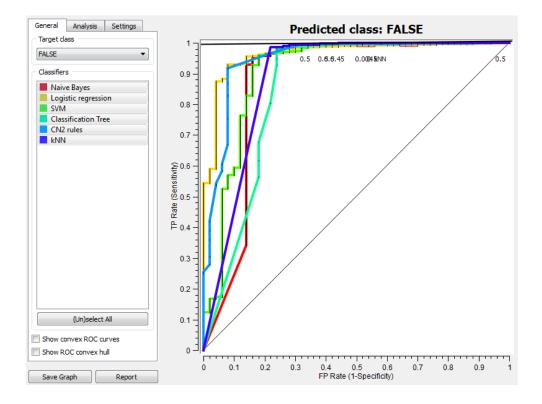


Figure 10: Receiver Operating Characteristic Curve for Concrete Deck (Thin Overlay)

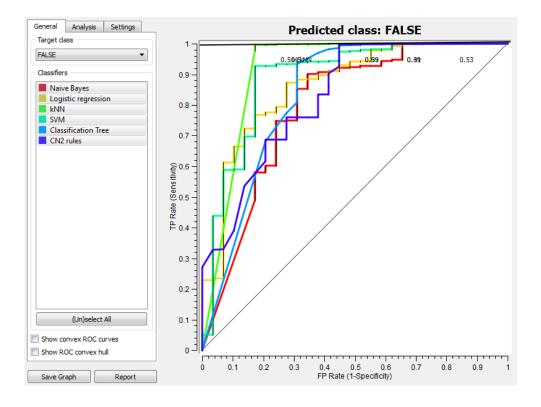


Figure 11: Receiver Operating Characteristic Curve for Concrete Deck (Rigid Overlay)

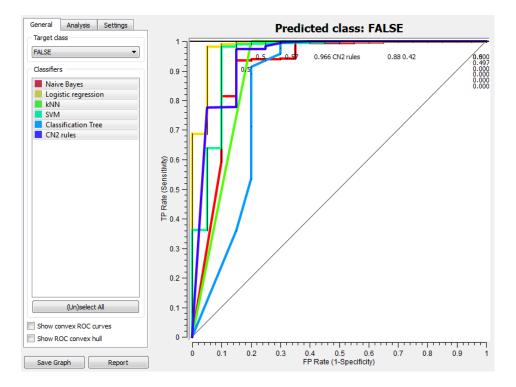


Figure 12: Receiver Operating Characteristic Curve for Bare Concrete Deck (Coated Rebar)

Area Under the Receiver Operating Characteristic Curve								
				Element				
Classification Method	107	109	12	18	22	26	Average	
Naïve Bayes	0.9463	0.9654	0.9681	0.8750	0.8049	0.9077	0.91	
k-Nearest Neighbor	0.9805	0.9831	0.9622	0.8870	0.9140	0.8997	0.94	
Support Vector Machines	0.9840	0.9695	0.9847	0.9136	0.9117	0.9693	0.96	
Logistic Regression	0.9710	0.9730	0.9837	0.9628	0.8621	0.9807	0.96	
Classification Trees	0.9686	0.9259	0.9230	0.8583	0.8058	0.8612	0.89	
CN2 Rule Learner	0.9654	0.9859	0.9585	0.9508	0.8180	0.8743	0.93	

Table 7: Area Under the Receiver Operating Characteristic Curve Results Summary

Table 7 summarizes the results for each element and the area under the ROC curve for each classification method. The top performing classification methods, based on an overall average, were logistic regression, support vector machines, *k*-nearest neighbor, and the CN2 rule learner, respectively. Each of the methods was the top performing classifier in at least one of the elements, and the range between their averages was a slight three-hundredths. Classification trees and naïve Bayes produced consistently worse results and were not considered as an appropriate classifiers for structural deficiency.

Significant Attributes

Understanding which attributes of bridges influences structural deficiency the most is very important. The area under the ROC curve was investigated for the addition of each attribute. First, age was the only attribute selected and classification was conducted on each element data set. Then the additional elements were added one by one to determine the influence they had on accurate classification. The order in which the attributes for each element were selected was age \rightarrow ADT \rightarrow truck percentage \rightarrow district \rightarrow condition state profile \rightarrow smart flags. Figure 13 displays the attribute influence on painted steel girders, Figure 14 displays the attribute influence on prestressed concrete girls, and Figure 15 displays the attribute influence on the deck elements.

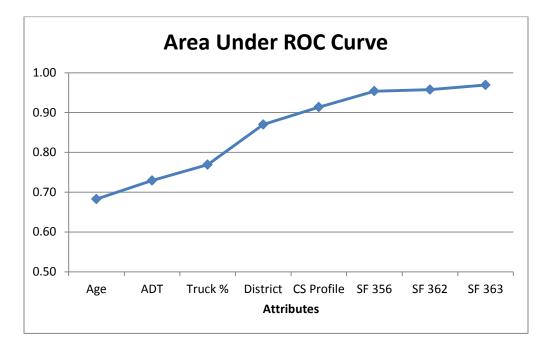


Figure 13: Attribute Influence on Painted Steel Girders

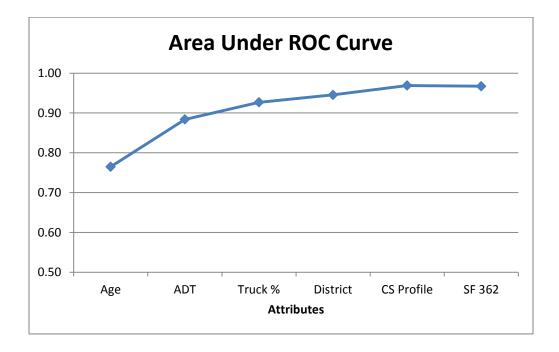


Figure 14: Attribute Influence on Prestressed Concrete Girders

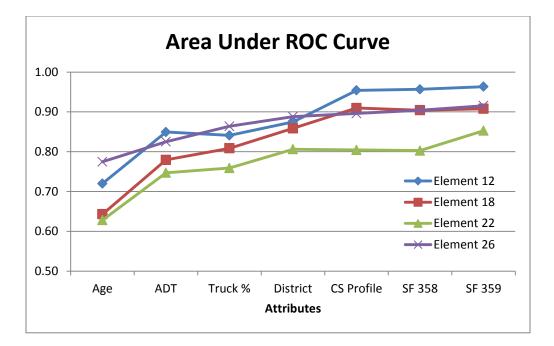


Figure 15: Attribute Influence on Deck Elements

Overall, the addition of individual attributes increases the classification performance in all elements with one exception: truck percentage in bare concrete decks with uncoated rebar (element 12). As expected, age and ADT were the two biggest influencers on classification performance. The condition state profiles seemed to have stronger influences on some elements than others.

Selecting a Classification Method

When determining which classification method was best to recommend as the most useful classifier of structural deficiency, two criteria were taken into account. First, the classifier must consistently produce strong classifying results, and second, these results must be easily understood by the user.

Classification trees and naïve Bayes were first eliminated as possible recommendations due to their poor results. Next, *k*-nearest neighbor and support vector machines were eliminated due to their more complex classifiers and black-box nature. For instance, support vector machines used a radial basis kernel function to transform, in this case, 6-8 dimensions (depending on the element). This produced 6-8 dimensional hyperplane equations that are completely abstract and of no significance to the user. Finally, the decision between logistic regression and CN2 rule learner came down to simplicity and ability to understand for the user.

The logistic regression classifier creates best-fit β coefficients to produce a classifier. Although still abstract to the user, Orange has the capability to produce nomographs of logistic regression classifier results. A nomograph consists of three (or more) parallel graduated lines of known values on any two (or more) scales that determines a straight index line that passes through the solution value of the third (or fourth, fifth, etc.) (Encyclopedia Britannica, 2014). Painted steel girders (107) contained 8 attributes, making it harder to understand the significance of the straight index line and the prediction it produces. Figure 16 displays the results of element 107's nomograph, and the nomographs for each other element are displayed in Appendix B.

Ultimately, it was determined that the CN2 rule learner would be the most useful for users by providing them with easy to understand "if...then" rules and results. Using the adapted version, the CN2-SD, improves the original algorithm's evaluation measures and covering. Additionally, the number of induced rules was reduced and both rule coverage and rule significance were increased. Orange has the capability of printing the rules produced by the algorithm for each of the elements studied. Figures 17-22 display these rules in a clean and clear manner for the user.

39

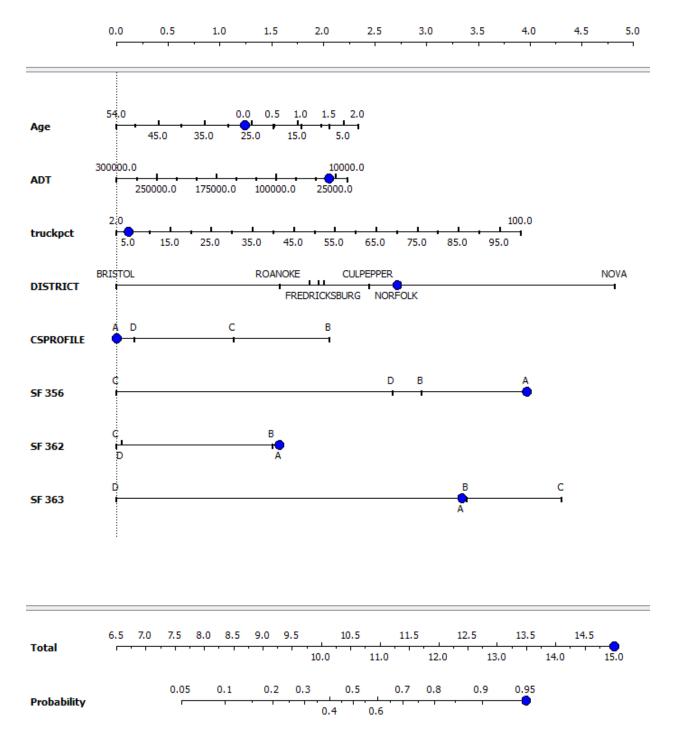


Figure 16: Nomograph of Painted Steel Girders

Rule	Rule quality	Coverage	Predicted class	Rule
2	0.026	3061.000	FALSE	IF SF 356=A AND SF 363=A THEN SD=FALSE
4	0.063	537.000	FALSE	IF Age<=42.00 AND Age>14.00 AND ADT>13344.00 AND SF 362=A THEN SD=FALSE
4	0.355	65.000	TRUE	IF SF 356=C AND CSPROFILE=A AND ADT>16785.00 AND ADT<=29899.00 THEN SD=TRUE
3	0.226	42.000	TRUE	IF CSPROFILE=D AND SF 363=D AND SF 356=A THEN SD=TRUE
4	0.242	14.000	TRUE	IF SF 356=C AND SF 363=A AND Age>30.00 AND Age<=36.00 THEN SD=TRUE
5	0.253	11.000	TRUE	IF CSPROFILE=D AND DISTRICT=BRISTOL AND truckpct<=11.00 AND Age<=30.00 AND ADT<=13344.00 THEN SD=TRUE
5	0.198	10.000	TRUE	IF SF 362=C AND SF 363=C AND ADT>23000.00 AND ADT<=52038.00 AND Age>40.00 THEN SD=TRUE
3	0.207	5.000	TRUE	IF SF 362=C AND ADT>80407.00 AND ADT<=85749.00 THEN SD=TRUE
3	0.210	4.000	TRUE	IF SF 356=B AND Age>42.00 AND SF 363=A THEN SD=TRUE
2	0.199	3.000	TRUE	IF SF 362=D AND Age<=13.00 THEN SD=TRUE
4	0.249	3.000	TRUE	IF CSPROFILE=D AND ADT<=4250.00 AND Age<=24.00 AND ADT>3953.00 THEN SD=TRUE
2	0.111	1.000	TRUE	IF SF 362=D AND Age>42.00 THEN SD=TRUE
3	0.166	3.000	TRUE	IF SF 362=C AND CSPROFILE=A AND Age<=44.00 THEN SD=TRUE
2	0.166	1.000	TRUE	IF SF 356=C AND SF 362=B THEN SD=TRUE
3	0.200	1.000	TRUE	IF DISTRICT=RICHMOND AND SF 363=C AND Age>44.00 THEN SD=TRUE
4	0.071	14.000	TRUE	IF SF 363=C AND DISTRICT=RICHMOND AND ADT>48110.00 AND Age>30.00 THEN SD=TRUE
3	0.500	1.000	TRUE	IF ADT<=3000.00 AND Age>37.00 AND ADT>1500.00 THEN SD=TRUE
3	0.200	5.000	TRUE	IF SF 356=C AND DISTRICT=RICHMOND AND Age<=28.00 THEN SD=TRUE

Figure 17: CN2 Rules for Painted Steel Girders

Rule length	Rule quality	Coverage	Predicted class	Rule
2	0.014	2184.000	FALSE	IF ADT<=37769.00 AND AGE<=37.00 THEN SD=FALSE
2	0.028	404.000	FALSE	IF SF 362=A AND ADT<=12068.00 THEN SD=FALSE
2	0.302	22.000	TRUE	IF CSPROFILE=D AND SF 362=D THEN SD=TRUE
6	0.247	11.000	TRUE	IF CSPROFILE=D AND AGE>33.00 AND pct truck<=2.00 AND pct truck>1.00 AND AGE<=38.00 AND ADT>23585.00 THEN SD=TRUE
4	0.450	15.000	TRUE	IF AGE>37.00 AND ADT>12068.00 AND ADT<=13112.00 AND ADT>13000.00 THEN SD=TRUE
4	0.344	23.000	TRUE	IF AGE>40.00 AND CSPROFILE=D AND ADT>509.00 AND ADT<=12500.00 THEN SD=TRUE
з	0.832	5.000	TRUE	IF ADT>37769.00 AND ADT<=38112.00 AND AGE>33.00 THEN SD=TRUE
3	1.000	1.000	TRUE	IF ADT>43074.00 AND ADT<=43842.00 AND AGE>31.00 THEN SD=TRUE

Figure 18: CN2 Rules for Prestressed Concrete Girders

Rule length	Rule quality	Coverage	Predicted class	Rule
з	0.015	6398.000	FALSE	IF Age<=44.00 AND Age<=39.00 AND ADT<=37209.00 THEN SD=FALSE
1	0.034	1326.000	FALSE	IF DK_CS=B THEN SD=FALSE
1	0.078	1006.000	FALSE	IF DK_CS=A THEN SD=FALSE
2	0.321	161.000	TRUE	IF DK_CS=E AND ADT>887.00 THEN SD=TRUE
3	0.329	141.000	TRUE	IF DK_CS=D AND ADT>2748.00 AND Age>33.00 THEN SD=TRUE
7	0.156	36.000	TRUE	IF DK_CS=D AND Age>44.00 AND PctTK<=2.00 AND ADT>136.00 AND ADT>310.00 AND ADT<=2261.00 AND Age<=60.00 THEN SD=TRUE
3	0.181	9.000	TRUE	IF DK_CS=D AND ADT<=136.00 AND Age>41.00 THEN SD=TRUE
4	0.165	7.000	TRUE	IF DK_CS=C AND SF 358=D AND Age>40.00 AND Age<=47.00 THEN SD=TRUE
4	0.120	3.000	TRUE	IF SF 358=C AND SF 359=C AND DK_CS=D AND Age>55.00 THEN SD=TRUE
6	0.136	3.000	TRUE	IF SF 358=C AND DK_CS=C AND Age>43.00 AND ADT>10881.00 AND ADT<=16110.00 AND PctTK<=4.00 THEN SD=TRUE
5	0.105	2.000	TRUE	IF DK_CS=C AND Age>37.00 AND Age>66.00 AND Age<=68.00 AND ADT<=149.00 THEN SD=TRUE
3	0.117	2.000	TRUE	IF SF 359=D AND Age<=28.00 AND SF 358=N THEN SD=TRUE
5	0.133	2.000	TRUE	IF DK_CS=E AND PctTK<=0.00 AND Age>56.00 AND ADT>147.00 AND ADT<=577.00 THEN SD=TRUE
6	0.173	4.000	TRUE	IF SF 359=C AND ADT>2233.00 AND SF 358=C AND PctTK<=2.00 AND Age>45.00 AND ADT<=4258.00 THEN SD=TRUE
4	0.200	2.000	TRUE	IF DK_CS=D AND ADT>11078.00 AND ADT<=12632.00 AND Age<=32.00 THEN SD=TRUE
2	0.125	1.000	TRUE	IF SF 359=E AND Age>52.00 THEN SD=TRUE
3	0.143	1.000	TRUE	IF District=Richmond AND SF 359=D AND Age>49.00 THEN SD=TRUE
6	0.222	3.000	TRUE	IF DK_CS=C AND SF 359=B AND District=Richmond AND PctTK>4.00 AND Age<=40.00 AND Age>36.00 THEN SD=TRUE
4	0.250	1.000	TRUE	IF Age>39.00 AND ADT>1904.00 AND ADT<=1906.00 AND Age<=47.00 THEN SD=TRUE
5	0.333	1.000	TRUE	IF SF 358=C AND PctTK>5.00 AND District=Richmond AND PctTK<=7.00 AND SF 359=B THEN SD=TRUE
з	0.014	36.000	TRUE	IF DK_CS=C AND District=Bristol AND ADT>1912.00 THEN SD=TRUE

Figure 19: CN2 Rules for Bare Concrete Deck (Uncoated Rebar)

Rule length	Rule quality	Coverage	Predicted	Rule
3	0.006	2472.000	FALSE	IF SF 358=N AND Age<=41.00 AND adt<=43842.00 THEN SD=FALSE
2	0.011	954.000	FALSE	IF DK_CS=A AND Age<=62.00 THEN SD=FALSE
2	0.037	686.000	FALSE	IF DK_CS=B AND Age<=70.00 THEN SD=FALSE
5	0.259	22.000	TRUE	IF DK_CS=C AND adt<=6641.00 AND adt>3658.00 AND Pct TK<=3.00 AND adt>4125.00 THEN SD=TRUE
5	0.242	15.000	TRUE	IF District=NOVA AND SF 359=D AND SF 358=N AND adt<=44541.00 AND Pct TK<=1.00 THEN SD=TRUE
3	0.362	8.000	TRUE	IF Age>62.00 AND District=Norfolk AND SF 359=C THEN SD=TRUE
3	0.214	3.000	TRUE	IF DK_CS=C AND Age>68.00 AND adt<=1723.00 THEN SD=TRUE
5	0.181	2.000	TRUE	IF SF 359=C AND Age>48.00 AND adt>3782.00 AND Pct TK<=2.00 AND Pct TK>0.00 THEN SD=TRUE
2	0.152	26.000	TRUE	IF DK_CS=D AND adt>3682.00 THEN SD=TRUE
2	0.025	13.000	TRUE	IF District=Richmond AND DK_CS=A THEN SD=TRUE
4	0,166	3.000	TRUE	IF Age<=22.00 AND District=Staunton AND Age>21.00 AND adt>800.00 THEN SD=TRUE
3	1.000	1.000	TRUE	IF adt<=367.00 AND adt>364.00 AND Age<=40.00 THEN SD=TRUE

Figure 20: CN2 Rules for Concrete Deck (Thin Overlay)

Rule length	Rule quality	Coverage	Predicted class	Rule
3	0.006	1164.000	FALSE	IF adt<=27800.00 AND adt>4356.00 AND Age>19.00 THEN SD=FALSE
1	0.011	754.000	FALSE	IF adt<=3542.00 THEN SD=FALSE
2	0.034	342.000	FALSE	IF Age<=57.00 AND adt>28116.00 THEN SD=FALSE
2	0.375	11.000	TRUE	IF Age>57.00 AND adt>11759.00 THEN SD=TRUE
3	0.221	4.000	TRUE	IF adt<=4356.00 AND adt>3955.00 AND Age>58.00 THEN SD=TRUE
4	0.284	4.000	TRUE	IF District=Richmond AND SF 359=B AND adt>8598.00 AND adt<=28116.00 THEN SD=TRUE
6	0.398	4.000	TRUE	IF SF 359=C AND adt<=3965.00 AND adt>2314.00 AND Age<=42.00 AND Pct TK<=6.00 AND Pct TK>2.00 THEN SD=TRUE
3	0.333	2.000	TRUE	IF Pct TK>17.00 AND Age<=19.00 AND Age>8.00 THEN SD=TRUE
2	0.250	1.000	TRUE	IF SF 358=D AND DK_CS=D THEN SD=TRUE
3	0.333	1.000	TRUE	IF adt<=3965.00 AND adt>3955.00 AND Age<=43.00 THEN SD=TRUE
3	0.500	1.000	TRUE	IF adt<=3436.00 AND adt>3402.00 AND SF 359=C THEN SD=TRUE
3	1.000	1.000	TRUE	IF adt<=487.00 AND adt>463.00 AND Age<=37.00 THEN SD=TRUE

Figure 21: CN2 Rules for Concrete Deck (Rigid Overlay)

Rule length	Rule quality	Coverage	Predicted class	Rule
2	0.001	8209.000	FALSE	IF adt>230.00 AND Pct TK<=13.00 THEN SD=FALSE
2	0.013	1222.000	FALSE	IF Age<=44.00 AND DK_CS=A THEN SD=FALSE
2	0.086	116.000	FALSE	IF DK_CS=B AND Age<=31.00 THEN SD=FALSE
2	0.148	17.000	FALSE	IF Pct TK>14.00 AND Age<=55.00 THEN SD=FALSE
1	0.152	7.000	FALSE	IF SF 359=A THEN SD=FALSE
1	0.229	6.000	FALSE	IF Age>79.00 THEN SD=FALSE
2	0.460	6.000	FALSE	IF District=Richmond AND Age>60.00 THEN SD=FALSE
1	0.870	3.000	FALSE	IF DK_CS=C THEN SD=FALSE
3	0.399	8.000	TRUE	IF Age>55.00 AND adt<=230.00 AND Age<=79.00 THEN SD=TRUE
2	0.416	5.000	TRUE	IF DK_CS=E AND Age>2.00 THEN SD=TRUE
з	0.571	4.000	TRUE	IF Pct TK>18.00 AND Pct TK<=19.00 AND Age<=60.00 THEN SD=TRUE
3	0.333	1.000	TRUE	IF Age>31.00 AND SF 359=D AND Age<=32.00 THEN SD=TRUE
2	0.027	74.000	TRUE	IF Age>44.00 AND adt<=4521.00 THEN SD=TRUE

Figure 22: CN2 Rules for Bare Concrete Deck (Coated Rebar)

CONCLUSIONS

Findings

The following is a summarization of the findings of this research:

> Classification methods can be used to develop a model to determine whether

or not a bridge is structurally deficient based upon vector attributes.

- The performance of classification methods was fairly strong overall as there was not a huge difference in area under the ROC curve results.
- Logistic regression, support vector machines, and the CN2 rule learner were the top three performing classifiers. Of the three, the CN2 rule learner is the recommended classification method due to its transparent nature and easy to understand rules.
- The investigation of smart flags as an attribute, especially in painted steel girders (element 107), strengthened the classification analysis.

Conclusion

This study investigated the benefits of data mining and the utilization of classification methods to improve the ability to forecast when certain bridge types will become structurally deficient. The results of this study provide valuable insight to state agencies, as well as the public, on the condition and safety risks of bridges listed in the VDOT Pontis and National Bridge Inventory across the state of Virginia. Knowledge discovery was used in this analysis and all available resources were implemented in order achieve the objectives of this study. The findings of this study are significant and will be useful to VDOT engineers, bridge owners, bridge inspectors, and consulting engineers involved in the design and maintenance process.

The bridge elements studied were chosen specifically because of their abundance in Interstate and state owned bridges. The specific metrics chosen were age, location, ADT, and previously inspected condition states. These were investigated because of their direct correlation to the deterioration of bridges and their significance to asset value and user cost.

This study has produced significant results and has successfully utilized the VDOT Pontis and National Bridge Inventory in data mining, a seldom researched manner. The methods in

44

which these results were produced can be modified by bridge type and the addition of bridge attributes can be implemented.

Recommendations

The top performing classification methods were logistic regression, support vector machines, *k*-nearest neighbors, and CN2 rule learner, respectively. Because these methods performed so closely together, it is recommended that the CN2 rule learner is implemented when predicted bridge structural deficiency is desired. The reason for this is that it is one of the top performers in classification while maintaining an easy to understand method. Support vector machines and logistic regression, especially, are not as preferred due to their more complex nature. Results are calculated in what is much-like a black box and user's comprehension is not guaranteed. They can be difficult to understand and results produced may not make sense to the user. The CN2 rule learner produces clean and clear results using "if…then" statements, and is therefore the recommended classification method for users.

The Pontis analysis methods in this report on Virginia bridge data can be modified and implemented in other states already using the Pontis bridge management system. Depending on individual state's specific areas of maintenance interest, more attributes, such as bridge length or environmental conditions, could be investigated to determine their effects on classification. Additionally, classification could be extended to non-state owned bridges as well.

In order to facilitate statewide collaboration and cross-over amongst districts, it would be beneficial to implement a uniform database for storing information on maintenance actions across the state of Virginia. This way inspection records would be consistent across the state and electronic resources could be more readily utilized in bridge maintenance analyses. Additionally, if a more comprehensive criterion for bridge inspection existed, the discrepancy

45

between inspector opinions would greatly be reduced. This would ensure inspection records to be more consistent, disparity between quantities would cease, and missing records could be reduced, and hopefully eliminated.

With time, more inspections take place and more data is collected. Following this report, it is suggested that methods are developed and incorporated to manage and analyze this data as it continues to pour in. Efficient means to handle inspection records, tables, and graphs is imperative to minimize man power and implement more sophisticated statistical software packages.

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APPENDIX A – ELEMENT CODES AND DESCRIPTIONS

Derived from the Pontis Element Data Collection Manual (VDOT, 2007)

Code	Element Description (V denotes Virginia element)
012	Concrete Deck – Bare – with Uncoated Reinforcement
013	Concrete Deck – with AC Overlay – without Membrane
014	Concrete Deck – with AC Overlay – with Membrane
018	Concrete Deck – Thin Overlay (less than 1") – no AC Overlay
022	Concrete Deck – Rigid Overlay (greater than 1") – no AC Overlay
026	Concrete Deck – Bare – with Coated Reinforcement
027	Concrete Deck – with Cathodic Protection
028	Steel Deck – Open Grid
029	Steel Deck – Concrete Filled Grid
030	Metal Deck – Corrugated/Orthotropic, Etc
031	Timber Deck
032	Timber Deck – with asphaltic concrete (AC) Overlay
038	Concrete Slab – Bare – with Uncoated Reinforcement
039	Concrete Slab – with AC Overlay – without Membrane
040	Concrete Slab – with AC Overlay – with Membrane
044	Concrete Slab – Thin Overlay (less than 1") – no AC Overlay
048	Concrete Slab – Rigid Overlay (greater than 1") – no AC Overlay
052	Concrete Slab – Bare – with Coated Reinforcement
053	Concrete Slab – with Cathodic Protection
054	Timber Slab
055	Timber Slab – with asphaltic concrete (AC) Overlay
092	V Reinforced Concrete Sidewalk
094	V Timber Sidewalk
098	V Steel Sidewalk, Open Grid – Coated
101	Steel Closed Web/Box Girder – Uncoated
102	Steel Closed Web/Box Girder – Coated
104	P/S Concrete Voided and Unvoided Closed Web/Box Girder
105	Reinforced Concrete Voided and Unvoided Closed Web/Box Girder
106	Steel Open Girder – Uncoated
107	Steel Open Girder – Coated
108	V Steel Open Girder with Timber Deck – Coated and Uncoated
109	P/S Concrete Open Girder
110	Reinforced Concrete Open Girder
111	Timber Open Girder
112	Steel Stringer – Uncoated
113	Steel Stringer – Coated
115	P/S Concrete Stringer
116	Reinforced Concrete Stringer
117	Timber Stringer
120	Steel Bottom Chord of Through Truss – Uncoated
121	Steel Bottom Chord of Through Truss – Coated
125	Steel Through Truss excluding bottom chord – Uncoated

126	Steel Through Truss excluding bottom chord – Coated
130	Steel Deck Truss – Uncoated
131	Steel Deck Truss – Coated
135	Timber Truss or Arch
140	Steel Arch – Uncoated
141	Steel Arch – Coated
143	P/S Concrete Arch
144	Reinforced Concrete Arch
145	Other Material Arch
146	Steel Cable – Uncoated (not embedded in concrete)
147	Steel Cable (not embedded in concrete) – Coated
151	Steel Floor Beam – Uncoated
152	Steel Floor Beam – Coated
154	P/S Concrete Floor Beam
155	Reinforced Concrete Floor Beam
156	Timber Floor Beam
160	Steel Pin and/or Pin & Hanger Assembly - Uncoated
161	Steel Pin and/or Pin & Hanger Assembly - Coated
201	Steel Column or Pile Extension - Uncoated
202	Steel Column or Pile Extension - Coated
204	P/S Concrete Column or Pile Extension
205	Reinforced Concrete Column or Pile Extension
206	Timber Column or Pile Extension
210	Reinforced Concrete Pier Wall
211	Other Material Pier Wall
215	Reinforced Concrete Abutment
216	Timber Abutment
217	Other Material Abutment
220	Reinforced Concrete Submerged Pile Cap/Footing
225	Steel Submerged Pile
226	P/S Concrete Submerged Pile
227	Reinforced Concrete Submerged Pile
228	Timber Submerged Pile
230	Steel Pier Cap – Uncoated
231	Steel Pier Cap – Coated
233	P/S Concrete Pier Cap
234	Reinforced Concrete Pier Cap
235	Timber Pier Cap
240	Metal Culvert
241	Concrete Culvert
242	Timber Culvert
243	Other Culvert
285	V Slope – Protected

286	V Slope – Unprotected
295	V Reinforced Concrete Wingwalls
296	V Timber Wingwalls
297	V Other Material Wingwalls
298	Smart Flag – Culvert Endwall/Headwall
298	V Smart Flag – Culvert Endwall/Headwall
299	V Smart Flag – Culvert Wingwall
300	Strip Seal Expansion Joint
301	Pourable Joint Seal
302	Compression Joint Seal
303	Assembly Joint/Seal
304	Open Expansion Joint
310	Elastomeric Bearing
311	Moveable Bearing (Roller, sliding, etc.)
312	Enclosed/Concealed Bearing or Bearing System
313	Fixed Bearing
314	Pot Bearing
315	Disk Bearing
320	Prestressed Concrete Approach Slab
321	Reinforced Concrete Approach Slab
330	Metal Bridge Railing - Uncoated
331	Reinforced Concrete Bridge Railing
332	Timber Bridge Railing
334	Metal Bridge Railing – Coated
356	Smart Flag – Steel Fatigue
357	Smart Flag – Pack Rust
358	Smart Flag – Deck Cracking
359	Smart Flag – Soffit of Concrete
360	Smart Flag – Settlement
361	Smart Flag – Scour
362	Smart Flag – Traffic Impact Damage
363	Smart Flag – Section Loss
444	V Mechanically Stabilized Earth – Abutment
701	V Smart Flag – Utilities
702	V Smart Flag – Drains
703	V Smart Flag – Lighting
704	V Smart Flag – Roadway Over Culverts
706	V Smart Flag – Soffit of Overhang of Concrete
707	V Smart Flag – Soffit of Concrete
708	V Smart Flag – Debris in Channel
709	V Smart Flag – Replacement
710	V Smart Flag – Deck Replacement
738	Concrete Slab – Covered with Fill

APPENDIX B – NOMOGRAPHS OF LOGISTIC REGRESSION RESULTS

Derived from the Orange Data Mining Software

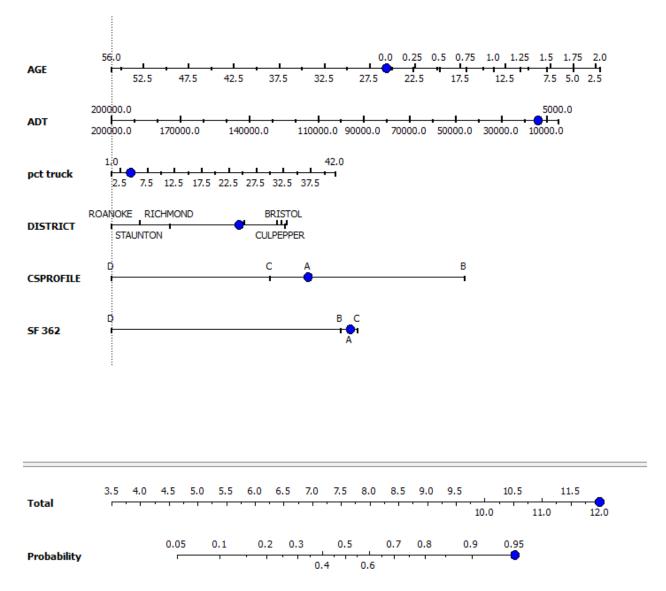


Figure B - 1: Nomograph of Prestressed Concrete Girders

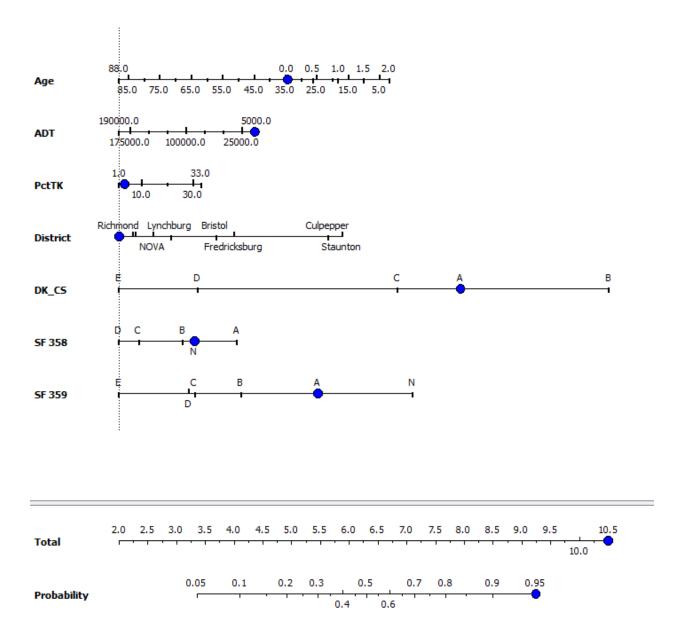


Figure B - 2: Nomograph of Bare Concrete Deck (Uncoated Rebar)

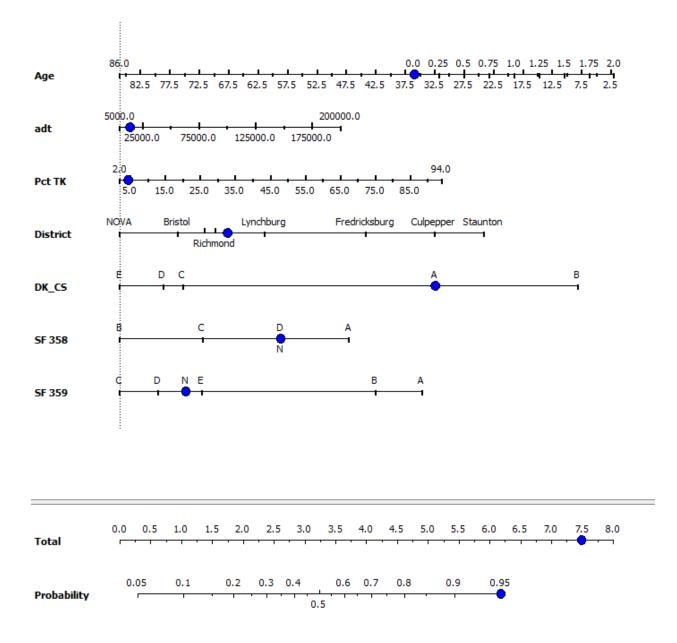


Figure B - 3: Nomograph of Concrete Deck (Thin Overlay)

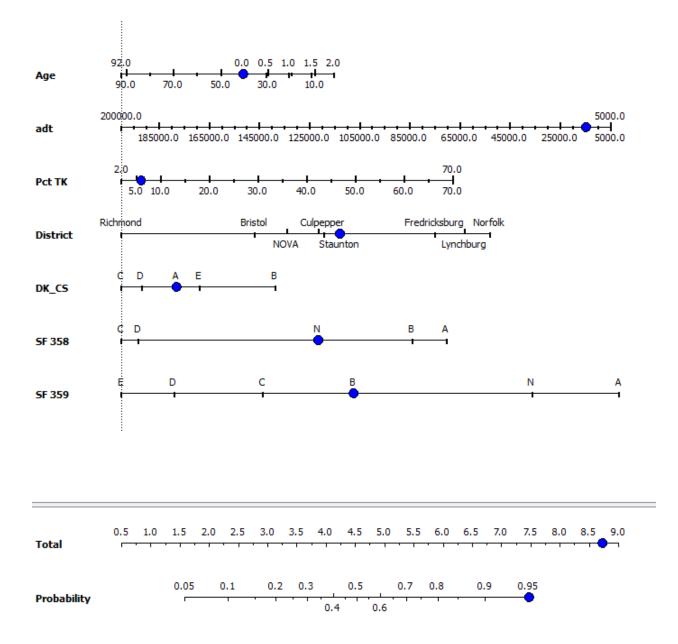


Figure B - 4: Nomograph of Concrete Deck (Rigid Overlay)

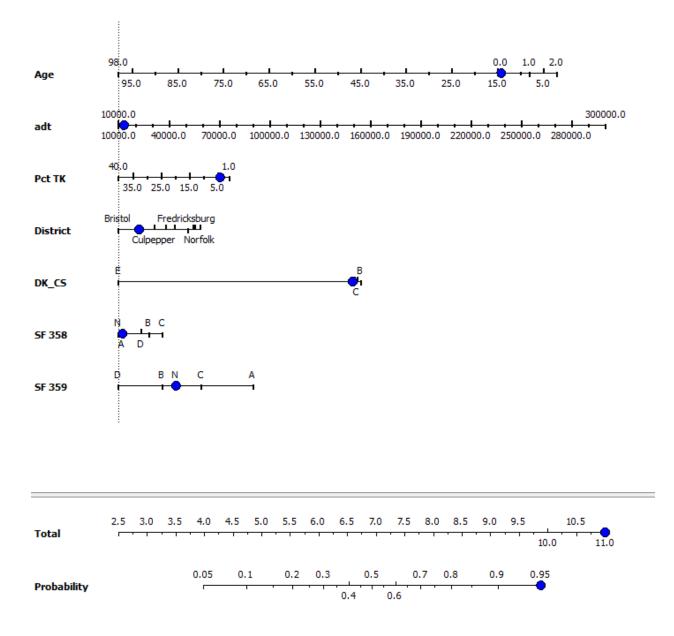


Figure B - 5: Nomograph of Bare Concrete Deck (Coated Rebar)