The Behavior of Spin-Labeled Mutants of the *Escherichia coli* Cobalamin Transporter BtuB Probed by EPR Spectroscopy in Native Environments

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Abstract

Gram-negative bacteria rely on active transport proteins on their outer surface for the import of large, scarce nutrients across the outer membrane. These TonB dependent transporters have two main domains, with a cylindrical β-barrel surrounding a globular hatch domain. The hatch domain must undergo substantial conformational changes to facilitate substrate, but the mechanistic details of the transport process are still unknown. Much of the work to date has focused on the study of these proteins in vitro, but the work presented here focuses on the use of CW and pulsed-EPR techniques to study them in native systems. To this end, EPR results are presented for the E. coli cobalamin transporter BtuB in both whole cells and isolated outer membranes. These results demonstrate conformational responses to substrate binding on the extracellular face of BtuB, and potentially substrate independent extension of the N-terminal tonbox sequence on the periplasmic side. Additionally, pulsed-EPR measurements on BtuB in native systems display novel long-distance components that appear to indicate crowding and potentially organization in the outer membrane. Finally, CW EPR spectra for a set of sites across the extracellular face of BtuB are presented, from which substrate dependent conformational shifts can begin to be mapped out in the native environment. These sites may also help to resolve the nature of the protein's organization on the OM. These EPR results are supported by the presentation of a method for denoising CW EPR spectra through the stationary wavelet transform.

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Chapter 1: Introduction

1.1 Overview

Vitamin B₁₂ is a general name for several members of the cobalamin (CbI) family of corrinoid compounds. It is the most complex natural cofactor, having a three-part structure consisting of a planar corrin ring, a flavin nucleotide derived 5,6-dimethylbenzimidazole (DMBI) group, and an exchangeable active group surrounding a central cobalt(III) (1). The octahedral coordination of the cobalamin center is fulfilled by four nitrogens from the corrin ring, an additional nitrogen from DMBI, and a carbon from the active group. The latter Co-C bond was the first



Figure 1. 2d projection of cyanocobalamin structure

biological organometallic bond to be identified (2). The common structural features of cobalamins are shown in Figure 1, where the exchangeable ligand (X) can be one of a variety of adenosyl or methyl donors, leading to: 5'-deoxyadenosyl, methyl, hydroxo, and cyanocobalamins, among others (1, 2). Of particular relevance is cyanocobalamin (CnCbl), which is light stable and the principal commercially produced cobalamin derivative, at a rate of more than 10 tons a year (2). Additionally, adenosylcobalamin (AdeCbl), which is also known as coenzyme B₁₂, and methylcobalamin (MeCbl) are widely used in the human body as cofactors of the enzymes methylmalonyl-CoA mutase and methionine synthase, respectively.

While vitamin B_{12} is required in vertebrates, some invertebrates, half of all algae, and most bacteria and archaea, it is produced only by a subset of bacterial and archaeal species (3). Interest in vitamin B_{12} has continued now for almost a century, beginning with its implicit discovery in the 1920s, when it was discovered that eating liver cured pernicious anemia, which led to a 1934 Nobel Prize for Minot, Murphy, and Whipple (2). By the late 1940s the red compound responsible for this clinical effect had been isolated from liver by the corporations Merck and Glaxo, and termed vitamin B₁₂. The first biologically active coenzymes of B₁₂ were produced in 1958 and the three dimensional structures of CnCbl and later AdeCbl were determined by the group of Dorothy Hodgkin in the latter half of the 1950s (2, 4). Hodgkin's work led into the second Nobel prize related to B₁₂, this time recognizing her work in crystallographic structure determination. The means of producing this important cofactor quickly became a topic of interest. A synthetic route to vitamin B₁₂ was finally completed in the early 1970s, with two variant approaches by Robert Woodward, who had won a Nobel of his own in 1965 for his achievements in organic synthesis, at Harvard and Albert Eschenmoser, who would later go on to be a pioneer in origin of life and artificial RNA research, at ETH. These synthetic routes contained nearly 70 steps, however, and were not efficient or cost-effective enough to be used in industrial production (2). Instead, the identification of the aerobic microbial pathway to B₁₂ biosynthesis, described first in the organism *Pseudomonas denitrificans* in 1993, combined with subsequent mutagenic selection and genetic engineering, has led to today's production of vitamin B₁₂ being exclusively via bacterial fermentation (2). More details are provided in the following sections.

1.2 Cobalamin in Eukaryotes and Humans

Humans and other animals that are dependent on vitamin B_{12} lack biosynthetic pathways and are thus reliant on consuming sufficient quantities in their diet. The recommended intake varies between countries, but is on the order of 1-3 ug, whereas the body can store several mg of B_{12} , often delaying by years the onset of adverse effects from B_{12} deficiency (5). Dietary B_{12} is not reserved for the human host, however, as more than 80% of the trillions of gut bacteria that reside in the colon are also dependent on B_{12} uptake (3, 6). Thus, the human system for B_{12} uptake and storage must be tightly regulated and efficient to ensure that the bodies' needs are met. The first step in cobalamin uptake is the release of the glycoprotein haptocorrin (HC) by the salivary glands in the mouth. This protein binds tightly to most cobalamin derivatives but initial binding in the mouth is low, as the cobalamin is still tightly bound to proteins and molecules within the food. Instead, the majority of initial binding to HC occurs after the low pH environment and proteases of the stomach release the rest of the bound cobalamin (1). Progressing into the small intestine, the pH shift and action of pancreatic enzymes result in the HC being cleaved and releasing most of its bound cobalamin load (1, 5). They are then transferred to intrinsic factor (IF), which binds preferentially to the human usable derivatives, and functions as a selectivity filter in the system (1). The IF-cobalamin complex is then absorbed via receptor-mediated endocytosis using the cubilin receptor in the ileum (1). In the blood, the cobalamin load is split between HC and another binder, transcobalamin, although the majority of tissue cobalamin is stored in complex with HC (5). Unused cobalamin accumulates in the liver, where as noted above it can reach milliGram levels, sufficient for several years.

In humans and other eukaryotes, the primary uses of cobalamin involve its use as a catalytic cofactor in the enzymes methylmalonyl-CoA mutase and methionine synthase. The former is located in the mitochondria, where it uses AdeCbl as a cofactor to convert methylmalonic acid to succinate (7). This reaction is critical in the catabolism of branched or odd-numbered fatty acids (1, 7). The latter is instead located in the cytoplasm, where it uses MeCbl as a cofactor in the transfer of methyl groups from methyl tetrahydrofolate to homocysteine, remaking methionine. Thus, methionine synthase is a principal controller of methylation reactions in the body (1, 7). The

structures of these proteins are shown in Figure 2, with the cobalamin cofactors highlighted in red.



Figure 2. The crystal structures of (A) human methylmalonyl-CoA mutase (PDB ID: 1REQ) and (B) the B₁₂ binding domains of *Escherichia coli* methionine synthase (PDB ID: 1BMT)

1.3 Cobalamin in Prokaryotes

Vitamin B₁₂ may be the oldest biological cofactor, with potential roots in the RNA world (2, 7). Its initial role was probably in anaerobic fermentation of small molecules, but as atmospheric oxygen became more available, new offshoots of its biosynthesis were created that eventually led to siroheme and later to heme and chlorophyll that support today's eukaryotic organisms (2). Biosynthesis of B₁₂ is exclusive to certain bacteria and archaea, with the elucidation of the aerobic bacterial pathway representing a 25 year journey led by several groups at Rhone-Poulenc (RP, currently part of Aventis) (2). They were joined by Sir Allen Battersby at Cambridge, who often alluded to B₁₂ synthesis in terms of grand feats of mountaineering, and a host of other notable scientists (2). To accomplish this, the groups at RP checked for complementation between over 150 mutants of known B₁₂ biosynthetic genes in *Agrobacterium tumefaciens and Pseudomonas putida* against more than three and a half thousand *E. coli* strains, each containing a piece of the *Pseudomonas* denitrificans genome (2). This let them identify a cluster of 22 biosynthetic genes in *P. denitrificans*, but it would be several more years of work on sequencing, purification, and isolation of intermediates until the full pathway was solved (2). Bacteria have two different pathways towards the synthesis of cobalamin, one anaerobic and one aerobic (8). They differ in

the point at which the cobalt is incorporated, with the aerobic pathway, found in *P. denitrificans*, inserting the cobalt much later (8). This was beneficial to the researchers, as the cobalt containing intermediates tended to be unstable. In both cases, most bacterial syntheses start from a glutamate-tRNA molecule with progression to the key cyclic intermediate uroporphyrinogen III, from which the pathways for chlorophyll, bacteriochlorophyll, heme, siroheme, and cobalamin diverge (2). In total, the biosynthesis requires more than 30 genes but has only 20 steps (9). Thus, the bacterial pathway is more efficient than the synthetic pathways of Woodward and Eschenmoser.

The majority of the world's B_{12} is still produced by RP (Aventis) using derivatives of *P*. *denitrificans*. The research groups at RP continued their work with the organism for another ten years, using random mutagenesis and selection for B_{12} production to increase the yield by two orders of magnitude (2). Since then, production strains have been enhanced with plasmids containing more efficient genes from other bacterial strains. The process of growth and extraction involves several days of aerobic fermentation, after which the vitamin B_{12} is extracted through superheating and the stable cyanocobalamin complex is formed by addition of cyanide. The solution can then be filtered and crystallized until the pure vitamin is isolated (2).

Within the human gut, however, the bacterial community does not have the luxury of relying on mutant strains engineered specifically for B₁₂ production. Indeed, a review of 303 species present in gut flora found that more than 80% utilized cobalamin, while only about 20% had a full biosynthesis pathway (6). As their human host possesses a highly efficient system to harvest most of the dietary cobalamin, these organisms must possess their own, highly effective means of vitamin B₁₂ uptake. The uptake machinery in Gram-negative bacterium, including those of phylum Bacteroidetes, and from family Enterobacteriaceae, such as the model organism *Escherichia coli*, have been studied for decades. These Gram-negative bacteria rely on a family of proteins that form the BtuBFCD transport system to move cobalamin derivatives across their

two membranes into the cytoplasm (3). The details of this system are discussed in the following sections. The first protein, BtuB, which sits in the outer membrane of the bacterium, is responsible for the binding of cobalamin derivatives in the medium. Competition in the gut is sufficiently fierce that most members of Bacteroidetes encode not one, but two, three, or even four analogues of the BtuB protein (6). As an example, *Bacteroides thetaiotaomicron*, the second most common bacterium in the adult gut, encodes three distinct homologs of BtuB, with two binding to a broad range of variants and one only to cobalamins with adenine or benzimidazole ligands (6, 10) This competition and specialization into variants of cobalamin among gut residents has even led to proposals for targeted remodeling of gut species by selective supplementation with specific cobalamin analogues.

The experiments presented in this work focus on the role of the BtuB transport protein in the organism *E. coli*, and so the unique structural elements of Gram-negative bacteria, and the details of the BtuBFCD transport system are presented in the following sections.

1.4 Structural features of the *E. coli* membrane environments.

Like other Gram-negative bacteria, the cytoplasm of *E. coli* is surrounded by both an inner and outer membrane (IM, OM), with the periplasm between them. While the inner membrane is comprised of phospholipids and is filled with proteins comprised mainly of helical bundles, the outer membrane has a unique, asymmetric composition. The inner leaflet again consists of phospholipids, while the outer leaflet is populated by large lipopolysaccharides (LPS) interspersed with protein β -barrels. The gel-like periplasm that stretches between them is filled with chaperones, energy transduction complexes, and structural elements that link the outer membrane to the semi-rigid peptidoglycan (PG) matrix that helps the cell maintain its shape.

1.5 The Inner Membrane

The inner membrane of Gram-negative bacteria is a phospholipid bilayer made primarily of phosphatidylethanolamine (PE), phosphatidylglycerol (PG), and cardiolipin (CL). The ratios of these components are approximately 75% PE to 25% PG to 5% CL, although this varies depending on the strain, growth conditions, environment, and point in the cell cycle (11). PE is a zwitterionic lipid, whereas both PG and CL carry a net negative charge between the pH values of 5.5 and 7.0 used for most bacterial growths presented here (12). In the rod-shaped *E. coli* cell, PG and CL are enriched towards the higher curvature region of the cell poles due to their higher intrinsic curvature (13). This is particularly apparent for CL, which has a relatively small glycerol head-group and 4 fatty acid tails.

In addition to phospholipids, the inner membrane is filled with both integral and peripheral membrane proteins and protein complexes. In fact, more than 20% of the open reading frames in the *E. coli* genome may encode for IM proteins, which generally are comprised of α -helical bundles (14). These inner membrane proteins are responsible for generation of energy for the cell via the electron transport chain, and thus to creation of the proton motive force (PMF). The PMF is the sum of both the electrical potential created across the IM, and the chemical potential created by the pH difference between the cytoplasm and periplasm, and in *E. coli* can be generated through both aerobic and anaerobic respiration (15). The PMF is essential to many IM and OM processes, including active transporters and the generation of ATP through ATP synthase. Inner membrane proteins are also critical to cell division, signal transduction, and the efflux of toxic or antimicrobial compounds.

Regarding the BtuBFCD system for cobalamin uptake, the IM contains the BtuCD protein complex. BtuCD is a heterotetrameric complex, with the stoichiometry $BtuC_2D_2$. It belongs to the ABC transporter family and couples the binding and hydrolysis of ATP to ADP with import of cobalamin across the IM. The structure of a closed conformation of BtuCD, bound to the

periplasmic element of the BtuBFCD system, BtuF, is shown in Figure 3. Each BtuC monomer contributes ten transmembrane (TM) domains, which together form a 20 helix bundle structure, which is capable of creating an alternating access pore large enough for the 1.5 kDa cobalamin substrate (16). The BtuD monomers, meanwhile, are involved in nucleotide binding. There are 2 ATP-binding cassettes in the overall complex, with each site containing elements of both BtuD monomers (16). The action of ATP binding and hydrolysis is coupled to motion in these nucleotide binding domains (NBDs), which in turn cause rearrangements of the TMDs that alter the facing direction of the pore (16). In bacteria, most ABC transporters are involved in the import of rare nutrients, as with BtuCD (17). Some are instead used for the export of



Figure 3. The structure of the BtuCD complex with bound BtuF (PDB ID: 4FI3). The TM domains of BtuC are colored gray, and are attached to the two nucleotide binding domains of BtuD in blue. The periplasmic transport protein BtuF, shown in orange, shuttles cobalamin between the OM and IM.

hydrophobic molecules, however, which is the predominant mode in eukaryotic cells (18). For a bacterium, these hydrophobic molecules are most commonly toxins or drugs, giving ABC transporters an important role in bacterial drug resistance.

1.6 The Periplasm

Between the IM and OM lies the periplasm, or alternatively periplasmic space. This aqueous compartment is filled with chaperones and substrate binding proteins and is critical in the folding and insertion pathways for OM proteins. The periplasm possesses no ATP, and so the only source of energy is the PMF across the IM. The periplasm is thus also home to a variety of energy transducing complexes that link the IM and OM, including the mot, tol, and ton systems. In addition to protein elements, the middle of the periplasmic space contains the peptidoglycan

(PG) matrix, a hybrid protein and sugar structure with glycan strands cross-linked by short peptide chains (19). The PG confers structure to the cell but it is also highly flexible, permitting the cell to respond to a wide variety of mechanical stressors and changes in osmotic strength.

The diameter of the periplasm is about 15-20 nm, although there is still substantial ambiguity regarding its size and it is possible that the diameter varies across the cell (20, 21). The distance between the inner leaflet of the OM and the PG matrix is controlled by Braun's lipoprotein (BLP), one of the most common *E. coli* proteins (22, 23). BLP is an elongated, helical protein that forms a stable homotrimer (24). The trimer is stabilized by a three-helix coiled-coil arrangement with an alanine-zipper, affording it a high degree of strength and stability (24). The N-terminus of BLP is covalently attached to the phospholipids of the OM inner leaflet, while the C-terminus is covalently linked to the PG matrix, directly coupling the two (23). The solution length of a BLP trimer is approximately 9 nm, but molecular dynamics simulations found that in membrane it is able to bend slightly, and also adopts a substantial tilt, resulting in an overall separation between OM and PG of about 7 nm (23). Less is known about what controls the distance between the PG and the IM, but the lengths of periplasm spanning proteins, including LpoA and TonB, are consistently between 14 and 15 nm (21, 25). For a periplasm of length 15 nm, consistent with the length of these proteins, this would place the PG in the middle of the aqueous compartment.

The peptidoglycan matrix itself is highly complex, being a mixed polymer of between 1.5 and 3 nm in thickness with both sugar and peptide substituents (26). The glycan strands consist of alternating N-acetylglucosamine (GlcNAc) and N-acetylmuramic acid (MurNAc) sugar units linked by a B-(1,4) glycosidic bond (19). The glycan strands average 25 to 35 disaccharides in length and are cross linked by short peptides consisting of alternating D and L-amino acids (27). The peptides are short, about five amino acids in length, and the alternating structure allows for interpeptide crosslinks between L and D constituents (27). The combination of flexible peptides

with rigid glycans allows the PG to maintain the shape of the cellular envelope while accommodating changes in the extracellular environment. The matrix is expandable, with the surface area increasing up to three-fold before rupture and the pores stretching to accommodate proteins of between 20 and 100 kDa in size (28-31).

This flexibility in pore size also has implications in PG synthesis, which must be tightly controlled to maintain the intended rod-like shape. *E. coli* cells have two distinct modes of PG synthesis. During growth, the cell grows mostly through elongation, and PG synthesis occurs throughout the side walls of the cell at elongasomes (32). Prior to division, however, a different cluster of proteins is recruited to form a divisome and synthesize the components of the two new cell poles in the resulting daughter cells (32). The two main GTase/TPases responsible for PG polymerization and peptide crosslinking in *E. coli* are PBP1A and PBP1B (32). These proteins associate with structural elements, cytoskeletal proteins, and hydrolases for recycling of the old PG components at the elongosomes, and divisomes, respectively (32). Yet, if the complexes were formed stochastically, the cell might lose its shape. Instead, it appears that interactions between PBP1A/PBP1B and the lipoproteins LopA/LpoB, which contain relatively bulky domains that must pass through the PG matrix, allow the synthesis of PG to targeted only to regions of a particular pore size (33).

The periplasm is also home to the periplasmic member of the BtuBCDF system, BtuF. This substrate binding protein shuttles cobalamin across the periplasm from BtuB in the OM to the periplasmic binding pocket of the BtuCD complex. The structure of BtuF is shown in Figure 4. The cobalamin is surrounded by two binding lobes, each with fingerlike helices around a central β -sheet, joined by a helical backbone (34). The interaction between BtuF and BtuB at the OM is poorly understood, but the interaction between BtuCD and BtuF has been revealed through several crystal structures, one of which was shown in Fig. 3. There are two negatively charged regions on BtuF, one on each binding lobe, that fit into positively charged pockets on the TM domains of BtuC (34). This creates a closed cavity where the vitamin can be transferred to the BtuC pore. Concurrently, binding of BtuF to BtuCD opens the two binding lobes on the former, which together with insertion of loop residues on BtuC reduces the affinity of BtuF towards cobalamin, allowing it to enter the cavity (35). The BtuCD transporter is then free to complete the cycle, moving the cobalamin substrate into the cytoplasm.



Figure 4. Crystal structure of BtuF (PDB ID: 1N2Z) with bound cobalamin

1.7 The Outer Membrane

Like the IM, the OM of *E. coli* contains a similar ratio of PE, PG, and CL phospholipids in its inner leaflet. The outer leaflet, in contrast, is comprised of unique lipopolysaccharide (LPS) molecules, which consist of lipid A linked to a polysaccharide that projects up out of the bilayer. Lipid A is unique in that its headgroup consists of a glucosamine disaccharide linked by a β -1',6 glycosidic bond (36). The sugars are linked to 3-hydroxymyristic acids at the 2, 3, 2', and 3' positions, and on one of the sugars the two fatty acids are acylated again off their hydroxy groups (36). This produces a total of six tails, which are typically fully saturated. The saturation and number of tails leads to an extremely low fluidity for the outer leaflet hydrocarbon. In isolation, LPS can withstand temperatures of up to 75° C before melting, ensuring that the outer leaflet is always in an ordered, gel-like state *in vivo* (37).

The lipid A is linked to a polysaccharide core that extends up and away from the bilayer surface. K-strain possesses only the core-oligosaccharide, whose general sugar scheme is given below, but in virulent strains a further set of repeating O-antigen sugars is present (36).



Here α Glc is α -D-glucose, Hep is L-glycero-D-manno-heptose, α Gal is α -D-galactose, and Kdo is 3-deoxy-D-manno-oct-2-ulosonic acid. Portions of the core-oligosaccharide are essential, as truncation mutants lead to defects in OM protein biogenesis and insertion (38).

LPS also has a high anionic charge density, with a phosphate group on each sugar, carboxy groups on the Kdo species, and mono or di-phosphates linked to the heptose sugars (36). This gives it a charge density per acyl chain twice that of most anionic phospholipids. To stabilize these charges, LPS typically contains a 4:1:1 ratio of stabilizing Mg²⁺ and Ca²⁺ counterions per LPS (39). This charge network also creates strong lateral bridging between LPS molecules, which is supplemented by extensive hydrogen bonding between neighboring sugars. In combination with the extreme ordering of the acyl chains, domains of LPS can even remain stably isolated in phospholipid bilayers for days at a time (40). The strength of these lateral associations also means that LPS is a potent diffusion barrier, blocking the passage of most small solutes and particularly hydrophobic ones, which diffuse about two orders slower than through a typical phospholipid bilayer (41, 42). The structure of a model OM bilayer produced using the CHARMM-GUI tool with a 100 Angstrom box and 18:1:1 PE:PG:CL ratio in the inner leaflet is shown below in Figure 5 (43, 44).



Figure 5. Model bacterial OM. The outer leaflet is composed solely of LPS, with lipid A (darker blue) and the core-polysaccharide (lighter blue). The inset shows an enlarged view of one LPS molecule. The phospholipid inner leaflet is composed of PE (gray), PG (red), and cardiolipin (yellow). Membrane generated using the CHARMM-GUI Membrane Builder tool.

The Tip3 water model atoms have been omitted in Fig. 5 for clarity. The simulated bilayer highlights the difference in order between the acyl chains of the inner leaflet phospholipids when compared to the outer leaflet lipid A. It is also immediately apparent that the core polysaccharide is stabilized by an extensive network of calcium counter ions (yellow spheres); magnesium was omitted for simplicity.

1.8 Outer Membrane Proteins

Proteins of the OM constitute a variety of porins, transporters, and sensory systems. They are composed of 8 to 26-strand β -barrels, and range in copy number from dozens to thousands.

Together, they cover the majority of the cell surface, ensuring that important compounds and ions are exchanged between the extracellular medium and the periplasm.

The most common proteins on the surface of *E. coli* K-strain are the major trimeric porins, OmpF, and OmpC. In some cases, these two proteins alone can constitute 80% of OM protein content, dominating the membrane landscape (45). These OM proteins are responsible for the passive movement of small molecules (<600 Da), and are highly efficient ion conductors with rates of 10⁸-10⁹ ions/s in physiological conditions (46). Compared to OmpC, OmpF produces a larger channel and thus leads to greater membrane permeability. This change in permeability can be exploited by the cell, with environmental stressors including: high osmotic stress, high temperature, antibiotics, bile acids, and acidic pH tending to favor incorporation of OmpC over OmpF (36).

Other major surface proteins include the porin OmpA and several specific transporters. OmpA is a two-conformer protein, able to fold into both an 8-stranded β -barrel with a C-terminal globular domain, and a larger 16-stranded β -barrel (47). In the two-domain form, OmpA lacks a continuous, water accessible channel in its barrel, but possesses the ability to anchor to the PG matrix via the C-terminal domain (47). The single domain form, in contrast, appears to be mobile in the membrane but has channel forming properties (47). Early studies on the propensity of each form found that only 2-3% of total OmpA appeared to be in the larger conformation while later studies at elevated temperatures have instead shown that the larger conformer is greatly enhanced and may even represent the native fold at physiological temperatures (47). Other porins include the recently discovered OmpL and PhoE, which is expressed in phosphate starvation conditions and has some selectivity towards anions, instead of the cation-selectivity seen in OmpF and OmpC (48).

Much of the remaining surface is taken up by various specific transporters, which move substrates that are too large or too rare to be taken up via nonspecific diffusion through the major porins. Specific transporters can be passive, as with the maltose and sucrose transporters LamB and ScrY, or active, as with the TonB dependent transporters (TBDTs) responsible for the movement of iron siderophores and cobalamin. The first passive transporter, LamB, is responsible for enhancing the rate of diffusion of maltose and oligosaccharides across the OM, which would otherwise diffuse very slowly through the nonspecific OmpF and OmpC porins. In the intestine, maltose is the principal breakdown product of dietary starch, and so efficient uptake is crucial for a cell's survival (36). Structurally, LamB is another trimeric protein, with each subunit contributing an 18-stranded β -barrel (36). Inside the barrel is a narrow channel with a diameter of half a nm, which is lined with a string of aromatic residues called the greasy slide (49). The residues of the greasy slide interact with the less polar regions of maltose and other sugars, facilitating their movement (49). The center of the channel also contains several polar residues that can hydrogen bond to the hydroxyl groups of the translocating sugars, although the orientation of this region has the unintended consequence of preventing the translocation of sucrose (49). Thus, growth in the presence of sucrose requires the expression of a different channel, ScrY. Like LamB, ScrY is also trimeric, but it has a larger pore with a diameter of about 0.8 to 1.1 nm, and lacks the bulky residues of LamB that prevent the diffusion of sucrose (36). Other selective transporters that still rely on passive diffusion include the nucleoside transporter Tsx and OmpW, which enhances the diffusion of small hydrophobic compounds (36, 50).

To capture even rarer substrates, the cell must turn to active transport processes. The outer membrane portion of the BtuFCD system, BtuB, is an example of an OM active transporter. It and the various BtuB homologs are again responsible for the uptake of various cobalamin derivatives. The other principal target for active transport in the gut is iron, whose free concentration in the human host is as low as 10⁻²⁴ M (51). As with cobalamin, nearly all of the free iron is tightly bound to large siderophores, and so the cell must use a variety of active transporters to capture one or more of these iron complexes to survive. Other active transporters

might capture large polysaccharides or other metals, but in most cases they belong to the family of TonB dependent transporters, which are discussed in Section 1.11.

Finally, the OM of *E. coli* is also home to proteins and protein complexes that function in extracellular export, motility, or adhesion. Examples of the former functions include the six major extraction systems that move proteins into the extracellular medium, and the bacterial flagellum that permits movement. Adhesion, meanwhile, is modulated by various proteins, but the 8-stranded B-barrel OmpX plays a key role in both biofilm formation with neighboring bacteria, and the invasion of eukaryotic cells (52, 53). These proteins and complexes tend to be minimally expressed or absent in K-strain *E. coli* and are further repressed in the Dsb knockout strains used in much of this work, limiting their impact on the present results.

1.9 Folding and Insertion of Outer Membrane Proteins

Getting nascent OM proteins from the cytosol where transcripts are produced to the membrane where they can be folded and inserted requires the coordinated work of several protein complexes. In *E. coli*, there are a total of eight systems that can serve to export proteins targeted to the IM, periplasm, OM, or extracellular medium, although not all present in K-strain derivatives (54). For OM insertion, the first step is to translocate an unfolded peptide across the IM, which is handled primarily by the Sec system. Proteins targeted for Sec translocation typically have an N-terminal signal sequence of hydrophobic and/or helical character, which is recognized by the signal recognition particle (SRP) that handles membrane targeting of the nascent protein (54). In the case of IM proteins, anchor sequences are also possible, which play a role in targeting but also halt translocation, leaving the protein in the IM with the anchor as a TM helix (55).

Sec translocation is used for unfolded peptides. It takes place co-translationally, although only once a majority (about 80%) of the sequence has been translated by the ribosome (54). In addition to the SRP, the unfolded protein is bound to the tetrameric chaperone protein SecB. This chaperone has a high affinity for the motor protein SecA, which is an ATPase and provides the energy necessary for translocation (54). SecA and SecB in turn form a complex with the SecYEG translocon, which provides the channel through which the substrate is translocated (54). The Sec system can also interact with the YidC insertase, which can insert some smaller IM proteins on its own and is critical in the insertion of subunits of ATP synthase and some cytochrome oxidases (56).

While the Sec complex mediates the passage of unfolded substrates across the IM, folded proteins are translocated via the twin-arginine translocation (Tat) pathway. The Tat pathway is named for the dual arginine motif in its signal sequence, S-R-R-x-F-L-K, and tends to move proteins that are already folded and sometimes already oligomerized (57). Its substrates can be destined for excretion, but also include redox proteins used in anaerobic respiration and those used for production and maintenance of the cell membranes (58). The Tat system consists of oligomers of a six-pass protein, TatC, and the single-pass protein TatB interspersed with a few single-pass TatA monomers. The TatBC complex forms a partially curved, wall-like structure with an upper gate, and several appear to work together to form the translocon. While the Tat complex moves a few substrates bound for the extracellular medium, the primary means of excretion to the exterior are the type I-VI secretion pathways. Periplasmic proteins are excreted via the type I and V systems, whereas movement directly from the cytoplasm to the exterior is handled by the type I, III, IV, and VI systems (54).

Both lipoproteins and OM targeted β -barrels enter the periplasm primarily through the Sec system. After translocation, lipoproteins are first anchored to the IM through attachment of a diacylglyerol to their N-terminal cysteine, which in *E. coli* is further modified with a third acyl chain (59). The +2 position relative to this cysteine then determines their final destination; an apartate residue causes them to be retained in the IM, while any other residue results in transfer to the periplasmic leaflet of the OM via the lipoprotein outer membrane localization (Lol) pathway (59).

Transfer is initiated by the ABC transporter LoICDE complex, which releases the lipoprotein complexed to the LoIA chaperone (59). The complex then moves to the LoIB receptor, which reattaches the lipoprotein to the periplasmic OM leaflet (59).

In contrast to lipoproteins, OM barrels are targeted through a C-terminal signal sequence, which is recognized by part of the Bam complex that handles integral OM insertion. Since the periplasm lacks ATP, the sorting and insertion events are driven by the energy sink of the folding event, which can exceed -20 kcal/mol (60). Together with the high tendency of unfolded β -barrels to aggregate, driven by their great number of hydrophobic residues, it is clear that periplasmic chaperones must be present to ensure that OM barrels reach their intended destination. These chaperones can employ one of two strategies to prevent folding and aggregation of their substrates.

The first involves several domains capable of forming a cage around the nascent protein, with the cage restricting the available conformers. This strategy is pursued by the seventeenkilodalton protein Skp, which is a helical trimer with three flexible arms that give the protein a form reminiscent of a jellyfish or octopus (61). The flexibility allows for the substrate to sample an extended, ovular conformational space while protecting it from significant outside contacts. The chaperone and serine endoprotease DegP also follows this strategy, although it does so by constructing huge circular or near spherical complexes with nearly 20 nm diameters that can span the width of the periplasm (62). The resting state of DegP appears to be as a hexamer, but it assembles into larger 12-mers and 24-mers both to act as a chaperone and to enhance its proteolytic activity towards misfolded targets by 15-fold (62). Both the 12-mer and 24-mer forms have gaps between monomers of a size sufficient for the free diffusion of unfolded substrates. The internal cavity, meanwhile, is about 8 nm in diameter making it just large enough to fit a folded porin such as OmpF or OmpC (62). The addition of proteolytic activity to degrade substrates that are trapped in off-pathway conformers makes DegP a powerful solution to OM protein folding. Alternatively, the two periplasmic prolyl-isomerases FkpB binding protein A (FkpA) and survival protein A (SurA) opt to cradle their substrates between two binding domains, separated by an extended helix (63, 64). This helix can rotate relatively freely, allowing the two domains to flex and compress with the movements of the nascent protein (63, 64). There is some redundancy between chaperones, with Skp and DegP able to rescue mutant strains deficient in SurA (65).

Prior to insertion, the structural disulfide bonds (DSBs) of some OM proteins must also be formed and checked for accuracy. DSBs are extremely uncommon in the cytoplasm of most organisms, including *E. coli* due to the reducing environment. They become possible in the significantly more oxidizing environment of the periplasm, however, and are handled by the aptly named Dsb system. These proteins are also localized to the IM, and disulfide formation happens in-line with extrusion of the nascent protein through the SecYEG translocon. This means that initial disulfides are formed in sequence order, and additional proteins are required to function as disulfide isomerases, to ensure that in the case of multiple cysteine residues only the correct disulfides are maintained (66).

Mechanically, cysteine residues on the new OM protein are contacted first by the periplasmic protein DsbA, which is part of the thioredoxin-family and contains an internal C-x-x-C motif (67). These cysteines are initially disulfide bonded, but interaction with the substrate cysteine causes a disulfide bond transfer, resulting in a covalent link between the substrate and DsbA with consequent reduction of one of the DsbA catalytic cysteines (67). The appearance of a second substrate cysteine results in a second transfer reaction, which forms a disulfide bond within the substrate and reduces the remaining catalytic DsbA cysteine.

The means to recycle the catalytic motif of DsbA is provided by the integral IM protein DsbB (67). Inside this protein is a quinone cofactor, with the type being dependent on growth conditions. Ubiquinones are generally present in aerobic growth, while menaquinones are found in anaerobic conditions (68). As with the formation of the substrate disulfide, the catalytic

cysteines of DsbA are recharged by passing the electrons to a matching C-x-x-C motif on a periplasmic loop in DsbB (67). This loop passes the electrons in turn to another, more membrane proximal loop, which finally passes them to the quinone cofactor (67). Finally, the quinone passes the electrons to terminal oxidases in the respiratory chain, completing the cycle (67).

Since disulfide formation occurs sequentially during translocation, the disulfide isomerase DsbC is used to ensure that only native disulfides are retained. DsbC is a homodimeric, periplasmic protein with a C-x-x-C motif on each monomer (67). The catalytic domains of DsbC begin in a reduced state, allowing for nucleophilic attack by each cysteine on improperly formed DSBs. Creation of the native DSB can follow a concerted isomerization or separated rounds of DSB dissolution and formation (67). DsbC is regenerated through reduction by DsbD, another integral IM protein that is itself reduced by thioredoxins in the cytoplasm (67, 69).

Null mutants of DsbA and DsbB prevent the formation of most disulfide bonds in the periplasm. A null mutant of DsbC, meanwhile, causes the accumulation of misfolded substrates if more than two cysteines are present in the template. Interestingly, a null mutant of DsbD results in the accumulation of oxidized DsbC, which can replace DsbA in certain cases, while overexpression of DsbD creates an excess of reductive potential in the periplasm and presents the same phenotypically as DsbA and DsbB null mutants (69, 70).

After translocation, chaperone binding, and possible disulfide bond formation, the new OM barrel can proceed to the Bam complex for insertion. The Bam complex has four scaffold lipoproteins arrayed around a central BamA barrel (71). These lipoproteins associate through a set of five periplasmic polypeptide transport-associated (POTRA) domains (71). The fifth POTRA domain is responsible for binding to the BamCDE complex, which contains the essential protein BamD (71). This lipoprotein appears to be responsible for binding to the C-terminal signal sequence and passing the substrate to the BamA protein (71). BamD may also regulate the function of BamA, as it remains associated to the fifth POTRA domain until the substrate has been

completely inserted (71). BamC and E appear to modulate the activity or structure of BamD. Finally, BamB also interacts with BamA through the third POTRA domain, but its role is not well understood.

There is still some controversy regarding the functional mode of the Bam complex, although recent work on the mitochondrial homologue of BamA, Sam50, has provided a highly plausible model. *In* vivo crosslinking of the yeast Sam50 determined that the first and final β -strands of the Sam50 barrel can separate, opening a lateral gate in the barrel (72). The first two strands of the new OM protein appear to form a β -hairpin and are guided into the gate by an overhead loop conserved in Sam50 and BamA (72). The substrate hairpin then inserts, forming 2 new sheets in the now mixed-protein β -barrel. This sequence of opening and insertion of another β -hairpin continues until the new OM protein is fully formed (72).

1.10 Organization of the Outer Membrane

While LPS possesses unique properties that make it an ideal permeability barrier and provide a great deal of stability to the outer envelope of the cell, it is not the only constituent of the bacterial OM. The surface of a Gram-negative bacterial cell is densely packed with β-barrel proteins covering the majority of the membrane envelope. The major trimeric porins, OmpF and OmpC, make up most of the protein content, but they are interspersed with active transporters, specific channels, and other barrels of varying oligomeric state. The emerging picture of the membrane is not one of a fluid, lipid driven bilayer, but that of a molecular sieve with an extensive network of protein pores thinly separated by LPS molecules.

Recent developments in atomic force microscopy have begun to produce images of native bacterial OM and intact cells sufficient to directly resolve the protein complexes on their surfaces. Work on OM sheets obtained from the marine picoplankton *Roseobacter denitrificans* determined that complexes of the *R. denitrificans* trimeric porin covered most of the surface and were

organized into constricted and relaxed forms based on local density (45). In the tightest packing regions, these complexes covered more than 75% of the available surface area (45). Compared to *E. coli, R. denitrificans* has a higher percentage of major porins as a function of total protein, at 90% instead of 80%, but the *E. coli* OM is still likely to be a densely packed network of trimeric porin complexes (45). Atomic models of the porin assemblies determined that the distances between them were consistent with interactions between aromatic residues. Such interactions have been identified before, and aromatic girdles are present in almost all β -barrels near the lipid headgroups (73). Additionally, the individual trimers were found to have little directional correlation, indicating a lack of specific interaction faces between the complexes (45). Similar results were also seen for an AFM study of the magnetotactic *Magnetospirillum magneticum*, where the surface of the protein was revealed to consist of an interlocking net-like structure (74). Individual holes or pores in the net were found to display limited, bounded diffusion and were consistent with trimeric porins moving on the surface (74).

These AFM results corroborate a large body of evidence stemming from fluorescence diffusion and single-particle tracking studies, which has indicated that most OM proteins display highly anomalous, confined diffusion behavior. An extensive review of this work is available, but some of the details are summarized here (75). Fluorescence recovery after photobleaching (FRAP) experiments on the porin OmpA showed that photobleaching persisted without recovery for a full 15 minutes (76). OmpA has a noncovalent PG interaction domain, but recovery was absent even when this domain was removed (76). Similar experiments using colicins E9 and Ia, bacteriocins that bind specifically to OM proteins BtuB and Cir, respectively, found no recovery after three minutes (77). These results indicate that long range diffusion on the order of 100 nm or more is entirely absent for these OM proteins. Single-particle tracking (SPT) of the maltose channel, LamB, using microspheres and gold particles for tracking has also demonstrated local Brownian diffusion on very short time scales, but increasingly confined behavior in longer ones.

The former study found that the LamB receptor appeared to diffuse within domains with a radius of about 25 nm, while the latter identified a slow moving population within a 20-50 nm compartment on the surface (78, 79). A variant approach using fluorescent antibodies to BtuB and OmpF failed to show confinement of BtuB but did determine that its diffusion was slowed five-fold in the presence of its periplasmic binding partner, TonB. This study did determine that the trimeric porin OmpF was confined, this time with domains of about 100 nm in size (80). Overall, these studies point to the existence of confined diffusion for many elements of the OM.

Various fluorescence approaches have also demonstrated that specifically labeled proteins rarely display diffuse surface fluorescence, but instead appear in distinct surface puncta, or patches. This patch-like fluorescence has been observed for LamB, and for BtuB and Cir bound to fluorescently tagged colicin molecules (77, 79). The latter study also determined that these fluorescent patches migrated towards the cell poles, and the authors proposed that these puncta represented islands of particular OM proteins (77). The mechanism of formation for these OMP islands involves the insertion machinery. Since all OM barrels must be inserted across the membrane by the Bam complex, if the unfolded precursors of a single protein were localized to a single Bam complex, it would become locally enriched on the cell surface. The presence of a very high protein density and confined diffusion would then prevent the members of this island from spreading significantly, ensuring that it continued to increase in density. Analysis of the fluorescent patches determined that the islands had a likely diameter of about half a micron (77).

Protein-protein contacts and inter-protein distances within these domains would be mediated through a number of weak driving forces. The aromatic interactions of the girdles that surround each protein at the headgroup interface were described previously. In the case of BtuB, simulations with high densities of BtuB found that these aromatic residues, in conjunction with other hydrophobic residues buried in the lipid bilayer contributed to extensive promiscuous protein interactions (PPIs) between neighboring BtuB molecules (77). In addition to protein-protein

contacts, most OM proteins display an asymmetric height distribution around their circumference. Given that the lipid bilayer is of relatively even thickness, this results in an asymmetric lipid mismatch around the protein. For BtuB, the variation is about 11 Å in membrane thickness from the shortest to the longest β -strand (81). Lipid mismatch has been observed to drive aggregation of proteins in several molecular dynamics studies, even when protein-protein interactions are entirely omitted (82, 83).

In addition to being confined to patches, domains, or islands on the membrane, these concentrated regions of protein are in constant, slow motion towards the cell poles. In the case of LamB, this movement was dependent on the cell cycle, and was halted when cells were treated with the RNA polymerase inhibitor rifampicin (84). This indicated that the motion was entirely due to insertion events, creating a conveyor-belt like motion of the cell surface driven by stochastic insertion events which are heavily biased towards the mid-cell. This trend towards the pole is greatly accelerated at each division event, where parts of the mid-cell become new poles for each daughter cell. Since the net direction of motion is towards the poles, once proteins enter, they will tend to remain.

Additionally, the large folding free energies for OM barrels provided an excellent energy sink to drive their insertion, but also make it impossible for the cell to recycle them. The eventual effect is then a slow accumulation of old OM proteins at the cell pole. Each division event creates daughter cells with one new pole and one old one, and over time generations can be assigned to the pole contents, and by extension to the cells themselves. As the environment that the cells are subjected to changes over time, and the outer membrane is filled with porins and transport proteins that must respond to the environment, cells with older poles will become increasingly unable to compete. Phenotypically, these cells display many of the hallmarks of aging and senescence in more complex organisms, including decreased metabolic efficacy which leads to smaller offspring, and even an increased chance of death (85).

1.11 TonB dependent Transporters and BtuB

In addition to the cobalamin transporter BtuB, E. coli encodes several TonB dependent transporters (TBDTs) primarily for the transport of iron siderophores across the OM. In the laboratory K-strain derivatives, the most common is the ferric enterobactin transporter, FepA. Other E. coli iron TBDTs transport ferrichrome (FhuA), coprogen (FhuE), citrate (FhuE), catecholates (Cir), and dihydroxybenzoylserine (Fiu) (36). Beyond cobalamin and iron siderophores, other organisms encode TBDTs that transport: copper, nickel, chitooligosaccharides, maltodextrin, thiamine, and sucrose (86). TBDTs are even critical to digestion. The starch utilization system (SUS) in many gut bacteria that helps break down the hosts dietary starches relies on a TBDT, SusC (87). Diversity in available glycans can lead some gut bacteria to express a wide variety of SUS TBDTs, with *B. thetaiotaomicron* exceeding 120 TBDT paralogs (87). Structurally, TBDTs are separated into a two-domain structure where an internal, globular hatch domain is surrounded by a 22-strand β -barrel. Crystal structures are currently available for several of these proteins, and a selection is shown below in Figure 6. The extracellular face of the transporter has a central depression for substrate binding, surrounded by a series of long, flexible loops. On the periplasmic side, the loops take the form of short turns. The hatch domains of these proteins are extensively solvated within the barrel, and some are stable on their own (88). Interactions between the barrel and hatch-domain are mediated by a series of ion-pairs, and the two domains are connected by a short linker. The N-terminal region of the hatch domain contains a short sequence known as the ton-box, which interacts with the partner protein TonB. In FhuA, there is also a switch-helix upstream of the ton-box, which changes conformation in response to substrate binding.

Several elements of the TBDT structure are known to be involved in the transport process. On the extracellular side, the long, flexible loops are capable of gating by closing over the bound substrate. This can be seen directly in the crystal structures of citrate bound and unbound FecA and has also been demonstrated via cross-linking of FepA to neighboring OMPs, which blocked substrate binding (89). Additionally, EPR studies on BtuB detected a significant reduction in the distance between loops 8 and 10 of BtuB after binding of cobalamin (90). On the periplasmic side, the ton-box is known to interact with TonB to form a mixed β -sheet. In BtuB, the ton-box spans residues 6-12 and has sequence DTLVVTA (91). Proline mutations at even numbered



Figure 6. Structures of the TonB dependent transporters BtuB (A, pdb ID: 1NQH) and FhuA (B, PDB ID: 1BY5). The transporters are shown in gray from the side (left) and top (right), while the hatch domain is shown in blue (center). The cobalamin and ferrichrome ligands of BtuB and FhuA, respectively, are shown in dark red.

sites in the ton-box disrupt β -strand hydrogen bonding with TonB and result in a transport deficient phenotype (91). The most widely used of these transport defective mutants in BtuB are the L8P and V10P mutations. In the crystal structures of BtuB, the ton-box region displays a minor

conformational change upon cobalamin binding, flipping over inside the transporter. In EPR studies, however, lineshape analysis and pulsed-EPR measurements show a substrate dependent extension of the ton-box, potentially by several nm, into the periplasm (92). Such an extension would greatly facilitate the interaction with TonB. It is now assumed that changes in the ton-box are passed allosterically to the extracellular side of the transport, but the mechanism of these conformational changes is not currently understood (93).

Expression levels of BtuB are regulated by AdeCbI responsive riboswitches in the btuB mRNA (94). In the gut where competition for cobalamin is fierce, BtuB paralogs might be the dominant TBDTs on the OM surface. In contrast, *E. coli* natively expresses BtuB at a modest 200 copies per cell (95). The low levels may stem from its ability to utilize a cobalamin independent methionine synthase, MetE, aerobically, reducing its reliance on cobalamin uptake (96). When overexpressed with the high copy pAG1 plasmid used in this work copy numbers are instead expected at 40-50% of the native porins (95, 97). At least at native copy numbers, TBDTs are currently thought to exist as monomers *in vivo*, although early work on FepA noted that it purified as a trimer while FhuA clearly purified monomerically (98, 99). The uptake of both Ferric enterobactin and micron E492 from *Klebsiella pneumoniae* by FepA also show cooperativity with a Hill coefficient of about 3, indicative of either 3 sites per monomer or a trimeric organization (100, 101). When grown in 2d crystals, FhuA can also be induced to form dimers, and may have been detected in the dimeric form in AFM images of the surface of *R. denitrificans* (45, 102). Overall, however, most evidence points to TBDTs functioning monomerically on the OM surface.

1.12 The ExbB, ExbD, TonB complex

The Ton complex, composed of the inner membrane proteins ExbB and ExbD together with the trans-periplasmic protein TonB, is responsible for the transduction of energy from the IM to TBDTs in the OM. ExbB is generally believed to serve as a scaffolding element, while ExbD is somehow sensitive to the PMF and drives conformational changes that energize TonB. There is
extensive homology between the Ton systems and other periplasmic systems for energy transduction, namely the Ton and Mot systems. In the case of the Ton system, TolQ and TolR can even partially replace ExbB and ExbD function *in vivo*, preventing a total loss of ton system function in null mutants (103).

The first member of the energy transduction complex, ExbB, is a 26 kDa integral IM protein (104). Structures of ExbB are only available for assembled complexes with ExbD, and unfortunately come in a variety of oligomeric states. Still, the general features of each ExbB monomer are consistent. The protein forms seven helices, with two of them forming an extended, kinked helix for a total of six TM passes (105). Very little of the protein is unstructured, and each monomer has a line of six lysine residues that usually point inward toward a central core (105). Two residues have been implicated to be critical to the Ton complexes energy transduction, T148 and T181 (106).

ExbD is a smaller 17 kDa protein, with 141 residues and a single TM helix (107). The first 22 residues are cytoplasmic and may form a small structured domain (107). The TM helix extends from residues 23-42 and is followed by the 98-residue periplasmic domain (107). The TM helix contains a protonatable aspartate, D25, that is conserved in the homologous Tol and Mot system proteins and is essential for the complex to respond to the PMF (108). A deletion scanning approach with 10-residue units determined that the periplasmic domain can be further subdivided into residues 42-61, which appear to modulate PMF dependent interactions with TonB, and residues 62-141, which engaged in TonB contacts independent of PMF (109). Thus, these two regions may play different roles in the energy transduction process. These deletion scanning results agree favorably with an NMR solution structure of the periplasmic domain, which found a flexible region between residues 43-63 followed by an extended folded domain from 64-133 and finally an unstructured tail from 134-141 (110). The structured domain has two, kinked helices next to a 5-stranded sheet.

It has been frequently suggested that the periplasmic domain of ExbD may play a role in binding to the PG matrix. The domain is only about half the size of the comparable periplasmic domain of the homologous MotB, however, and has no sequence similarity in the PG binding region (109). Further, the topology of the ExbD periplasmic domain is almost identical to some periplasmic substrate binding proteins, such as FhuD, that receives ferrichrome siderophores from the FhuA TBDT (110).

Finally, TonB is also a 26 kDa protein with a single TM pass and 239 residues (104). Its first 33 residues contain the TM helix which is followed by a proline rich region from residues 66-102, a flexible linker from 103-149, and a globular C-terminal domain from 150-239 (104). TonB is an integral IM protein, but its C-terminus must interact with TBDTs on the periplasmic surface of the OM. To this end, distance measurements using pulsed-EPR revealed that the total length of the protein was about 14.5 nm, enough to span the shorter end of estimates for the width of the periplasm (21). Also, this distance was most consistent with the presence of a type II polyproline helix, where all of the proline residues are oriented in their trans isomer, for the proline-rich region from residues 66-102 (21). An extended conformation for the proline-rich region was also observed in solution NMR (111)

Crystal structures of the globular C-terminal domain of TonB show a structure containing two helices in front of a 3-stranded β -sheet. This sheet interacts with the ton-box of TBDTs,



Figure 7. Structure of the interaction between FhuA and TonB (PDB ID: 2GRX) from the side (A) and bottom (B). FhuA interacts with a monomeric TonB C-terminal domain, forming a mixed 4-strand β-sheet through incorporation of the FhuA ton-box residues. forming a stable 4-stranded sheet through which force is putatively applied to the transport protein. Binding to the TBDT has a 1:1 stoichiometry, and an example is shown in Figure 7, for the interaction of TonB with the TBDT FhuA. EPR studies of the C-terminal domain binding to the FhuA ton-box indicate that even after binding the complex remains dynamic, sampling several nm in pulsed-EPR distance measurements (112).

In addition to forming complexes with TBDTs, TonB can also form homodimers through its C-terminal domain under certain conditions (113). Two models of the dimer interface are shown in Figure 8. The initial dimeric structure, shown in Fig. 8A, used a truncated C-terminal construct with residues 164-239 (114). This construct formed a stable dimer with β-strand exchange leading to substantial contacts between the two monomers (114). Later attempts with a longer construct consisting of residues 148-239, however, produced a protein that was monomeric in solution but with dimeric crystals (Fig. 8B) (115). Here, the dimer interface is made primarily through a less extensive exchange of the C-terminal strand and the orientation is markedly different from the short construct. Follow up work with analytical ultracentrifugation



Figure 8. Models of the TonB C-terminal dimer interface. (A) The original dimer interface (PDB ID: 1IHR) obtained for shorter constructs (residues 164-239) of the TonB C-terminal domain. Here, the two domains form a stable dimer through strand exchange. (B) The dimer interface (PDB ID: 1U0) obtained for a slightly longer construct (residues 148-239) of the TonB C-terminal domain. In this case, the construct is monomeric in solution, but dimeric in the crystal.

confirmed that the shorter construct produced solution dimers, while the longer construct produced solution monomers (116, 117). Currently, there is still a great degree of controversy over the role of the dimeric form in the transport process.

In vivo, the levels of each member of the Ton complex are tightly regulated and varied primarily in response to changes in iron concentration. In cells grown in abundant iron, the WT levels of TonB are around 300 copies per cell, with a 2-fold excess of ExbD and 7-fold excess of ExbB. Iron starvation conditions or deregulation, however, can lead to the production of more than 1300 TonBs, with the ratios of ExbB and ExbD to TonB maintained at approximately 2:1 and 7:1. Thus, in the cell ExbD is more abundant than TonB, and ExbB is three or four times more abundant than ExbD (118). Various attempts have been made to determine the stoichiometry of the actual functional complex, with chromatography and in vivo cross-linking indicating a wide range of 2 to 6 ExbB monomers per complex (119, 120). Later work with cryo-EM has been used to generate structures of ExbB₄/ExbD₂ complexes, as well as heterodimeric complexes of the form ExBB₄/ExbD₁/TonB₄ (121). Subsequent studies using crystallography and cryo-EM, meanwhile identified several pentameric and hexameric complexes of ExbB (105, 122). Electron densities consistent with a single ExbD are found in the ExbB pentameric structures, while three ExbD helices were found within the ExbB hexamer (105, 122). It has been speculated that the complex stoichiometry may change with pH, but it nevertheless appears to be heterogeneous in these in vitro preparations (122).

1.13 Models for TonB Dependent Transport

Since Hancock and Brown first proposed in 1976 that the energy for TBD transport must be transduced across the IM to the transport proteins in the OM, various models have been proposed for how this might work, and the subsequent conformational changes that would be induced in TBDTs to effect transport (123). Shortly after, in 1980, it was proposed that TonB might use the PMF to generate a soluble messenger capable of dissociating cobalamin from BtuB (124). The model also proposed that BtuC would use the energy of acetyl phosphate moieties to drive cobalamin import across the IM. At the time, it was not known that BtuC formed part of the relatively new family of ABC transport proteins, and acetyl phosphate had been proposed as the energy source for active transport across the IM (125). Other models of the time included TonB functioning to bring the IM and OM into close apposition, or TonB as a regulator or protease that modulates the activities of BtuB and the IM importer (126). These early models were based primarily on null mutant phenotypes and the effects of phage and colicin binding events.

By 1990, knowledge of the system had progressed to the point that Robert Kadner proposed an alternative idea, that the TonB protein could be energized and transition between the IM and OM to provide energy to the OM receptor proteins (127). This was later expanded on by the group of Kathleen Postle into the shuttle model, which first appeared in 1997 when the Postle group determined that TonB was able to associate with both the IM and the OM (128). In the shuttle model, TonB is locked in a dynamic cycle, beginning in the inner membrane where it is energized via the PMF (129). The TM anchor of energized TonB would then dissociate in some manner, and the protein would travel to the OM, where it would release stored potential energy to the OM transporter (129). Finally, TonB would return to the IM, with its TM helix reinserting into the bilayer (129). The model was based on a variety of biochemical evidence. Stoichiometric analysis and chemical cross-linking out of the Postle group identified that there were multiple ExbB and ExbD proteins interacting with TonB as the functional energy transduction complex.

(129). These interactions were also determined to involve the N-terminus of TonB, where the TM domain is located (129). The authors then speculated that the ExbB/ExbD complex might form the majority of contacts with the TonB TM helix, reducing the energy barrier for its removal from the IM (129).

Structures of TonB, showing it to behave both as a monomer and a dimer dependent on construct length and experimental conditions, also became available in the years following the shuttle model's introduction (104). This led to speculation that the dimeric form of TonB might be responsible for storing the potential energy derived from ExbB/ExbD. Early evidence for the actual shuttling process came from the determination that the N-terminus of TonB could be fluorophore labeled, and so it appeared to be accessible to the periplasm (130). The amount of labeling increased when ExbB or D were deleted, and so it appeared that they were responsible for localizing TonB to the IM (130). Unfortunately, in 2011 the shuttle model was withdrawn. A fusion of the V. cholerae ToxR cytoplasmic domain to the N-terminus of TonB was found to produce a protein that was active, but was unable to be dissociated from the IM fraction (131). Thus, it appeared that TonB function was not dependent on whole protein movement between the two membranes. Curiously, several years after the shuttle model was retracted a structure was published which displayed a pentameric ExbB complex, with an internal protein pore that appeared to accommodate a TM helix that was completely isolated from membrane contacts and that may be able to move up and down within the pore (105). While unlikely to facilitate actual shuttling, such a complex would agree with the main biochemical observations that led to the formation of the shuttle model.

The appearance of dimeric structures of the TonB C-terminus also inspired the propeller, or rotational model of TonB dependent transport (114). This model was further based on the extensive homology between the Tol, Mot, and Ton systems. In particular, both the ExbB/D and TolQ/R proteins are highly homologous to the MotB/A proteins (132). The latter are known to use

the PMF to drive rotation of the bacterial flagellum, and so it is reasonable to assume that the Ton and Tol complexes may act in the same way (132). The initial homology study depicted TonB as a monomer in the ExbB/ExbD/TonB complex, but most subsequent depictions of the propeller model show TonB as a dimer, with the TonB monomers either inside or outside a ring-like ExbB/ExbD complex (104, 132). Direct evidence for rotation of the TonB complex comes primarily from a single study involving a GFP-fusion to the TonB N-terminus. Using fluorescence anisotropy, it was found that there was a PMF dependent motion of the fluorophore, which was assumed to correlate to rotational motion of TonB in the IM (133). This motion would be about two orders of magnitude faster than observed in the flagellum, but the mechanical details of how it is produced are unclear (133). Only ExbD is sensitive to the PMF, and it does display a high degree of structural similarity with the ion channels formed in the Mot complex (134). So, the ExbB/ExbD complex would be assumed to form the stator of the rotational complex. In both the Tol and Mot complexes there are PG binding domains in at least one member protein, which would appear to stabilize the outer, stator portion of the complex and permit efficient rotation of the inner elements (104, 132, 134). Both ExbB and ExbD lack a known PG binding domain or motif, however, and so it would appear that the entire complex might rotate, perhaps even nonproductively, in the presence of a proton gradient (104). Still, there is some evidence that the TonB protein can itself interact with PG, based on homology with the PG binding motif of LdtC, although this too would likely lead to nonproductive rotation of the ExbB/ExbD stator instead of TonB motion (135).

The propeller model has since been refined into the rotational surveillance and energy transfer (ROSET) model (136). In this model, it is speculated that the dimeric form of TonB possesses the PG affinity, and is responsible for keeping the C-terminus in proximity to the OM (136). The monomeric form of the protein, meanwhile, is responsible for binding events to TBDTs. Building on the realization that ExbB/ExbD lack PG binding motifs, the ROSET model posits the

movement of the stator complex as a feature, which permits a single ExbB/ExbD/TonB complex to sample wide areas of the OM above (136). This is supported indirectly by the copy number disparity between TonB and TBDTs, with iron starvation conditions able to produce a more than 12-fold excess of the latter on the OM surface (137). The ROSET model paints a convenient picture of the energy transduction complex, but it still lacks direct physical evidence for most of its component pieces.

An alternative to rotational motion driving TonB dependent transport is the pulling model. In this scheme, TonB interacts as a monomer with the ton box of the TBDT, and some downward force is created and mediated through TonB, which tugs on the ton box and releases the substrate. The pulling model was likely inspired by single molecule pulling experiments to study the unfolding of IgG and ubiquitin (138, 139). As in the structures of IgG and ubiquitin, a strong 4-stranded β -sheet is formed during TonB dependent transport between the ton box of a TBDT and TonB, and this linkage appears to be stable enough for sustained force transduction. Initial evidence for the pulling model came from steered molecular dynamics simulations, where a constant loading force was applied to the ton box of BtuB, and the N-terminal hatch domain was slowly pulled out, with applied forces ranging between 50 and 350 pN (140). Unfortunately, the creation of a channel large enough to permit cobalamin passage required a total unfolding of about 20 nm (140). This is comparable to the size of the periplasm, and it is unlikely that such an extension would be possible in vivo. Steered molecular dynamics was repeated more recently, again finding that a channel sufficient for translocation was formed after 20 nm of pulling and unfolding of about 50 N-terminal residues of the hatch domain (141). In this case, however, single-particle AFM experiments were also performed, where a TonB C-terminus covalently attached to an AFM probe tip was used to pull on immobilized BtuB and FhuA proteins (141). These AFM experiments confirmed that the beta sheet interaction is strong enough to sustain the force load from pulling events, and that 6 to 8 nm pulling events were tolerated before rupture of the complex was observed (141). Support for the pulling model has also been provided through cryo-EM work on the ExbB/ExbD/TonB complex, where the Coulton group has isolated several different forms of the complex that differ in the position of ExbD and TonB monomers, and in the extent of their heterodimerization (121). In one of the complexes, a downward projection of electron density was observed that may be a piston-like motion of ExbD in response to proton translocation, which could be transferred to TonB through heterodimer formation and used to drive a pulling motion at the TBDT (121).

Alternatively, the pulling motion could be provided by the structure of TonB. As noted previously, EPR measurements on TonB found that its length was consistent with a type II polyproline helix, an extended arrangement consisting of all trans-isomer proline residues (21). By exchanging environment polarity, e.g. by solvent exchange, polyproline type II helices have been observed to interconvert to the all cis type I form, which results in a 40 to 50% reduction in length (21, 142, 143). Such a conversion would provide a similar pulling distance to that tolerated by the TonB/ton-box pair in AFM experiments and could be induced by rotational motion imparted to the polyproline region of TonB once it became immobilized via ton-box binding. Alternatively, it could be induced in the pulling model by extensive heterodimerization between the TonB polyproline region and the extended domain of ExbD, potentially with subsequent motion from the piston-like rearrangement of ExbD in the ExbB/ExbD complex.

While the means by which the ExbB/ExbD/TonB complex may function to transduce energy from the PMF at the IM to the TBDTs in the OM are still controversial, even less is known about how TonB binding might drive rearrangements in the TBDT to create substrate movement across the OM. TBDTs move very large substrates that often have cross-sections almost as large as their globular hatch domains. Creation of a pore capable of substrate passage would necessitate a rearrangement of the hatch domain, or its partial or complete dissociation from the barrel. Speculating on the nature of conformational changes in the hatch domain is difficult, although some work has been done using unfolding titrations with urea and EPR spin-label reporters to attempt to observe hatch transitions in reconstituted TBDTs (144). Partial or complete removal, meanwhile, has been frequently proposed on the basis of the high-resolution crystal structures of TBDTs, where the hatch-barrel interfaces are highly solvated by so-called lubricating water molecules (88). In combination with the ability to express stable, isolated hatch domains of some TBDTs, the waters would facilitate a total removal of the hatch from the barrel. One problem with complete removal, however, is that the linker between the hatch domain and the barrel is only a few residues long, and it is unclear how it would accommodate the large motion required for hatch removal (88). Most recently, pulling, AFM, and molecular dynamics have suggested that the N-terminal approximately 50 residues may form a structurally weak domain, which could be selectively unfolded and removed from the barrel without disturbing the remaining hatch elements (141). Still, much more work will be required in order to understand the details of how these proteins are able to move such complex substrates.

1.14 Remaining Chapters in This Work

Chapter 2 gives an overview of EPR theory and provides the methods for both whole cell and OM sample preparations of spin-labeled BtuB.

Chapter 3 demonstrates the applicability of the stationary wavelet transform to the recovery of CW EPR samples. The methodology presented in this chapter facilitates the comparative analysis of CW lineshapes for very low signal-to-noise ratio spectra in the later sections.

Chapter 4 demonstrates the applicability of CW and pulsed-EPR to the study of BtuB in its native environment, the whole cell. The role of the *E. coli* Dsb system is examined as it relates to the labeling of BtuB cysteine double-mutants, and the means of successfully producing DEER spectra in the living cell are established. DEER results are provided for both the extracellular and periplasmic faces of the protein in living cells, with both displaying potentially novel conformational changes.

Chapter 5 explores the both fortuitous and frustrating discovery of additional DEER peaks in the cellular and OM samples. These peaks are indicative of crowding and potentially of organization on the cell surface, which has been an emerging area of interest via fluorescence and AFM. The results presented in this chapter indicate a role for DEER in these explorations, but also highlight limitations in the analysis of DEER data with relation to background subtraction.

Finally, **chapter 6** extends the previous chapters by introducing almost twenty more sites across the extracellular face of the protein. Preliminary CW results are shown for these sites, some of which display significant changes with the addition of cobalamin, and their future potential for mapping out conformational motions in the protein and for further localizing its interactions with neighboring OM proteins are highlighted.

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Chapter 2: Theory and Methods

2.1 EPR in Native Systems

The first true EPR result was obtained by Zavoisky in Tatarstan, Russia for hydrates of manganese sulfate and copper sulfate and was included as part of his doctoral thesis in 1944 and in publication in 1945 (1). He built the instrument himself, leveraging experience in amateur radio and in a military laboratory during WWII (1). By 1946, his discoveries had spread to the US and Europe, and by 1952 EPR was being applied to studies of biological materials. The first work on bacterial cells by EPR was likely performed in 1952 for samples of freeze-dried *pseudomonas fluorscens* by Barry Commoner, Jonathan Townsend, and George Pake at Washington University in St. Louis (2). They followed up on this work in 1954, publishing early evidence for EPR active metabolites in lyophilized plant and animal tissues (2). In the 1960s, several groups identified iron and copper compounds in *E. coli*, as well as T1 and T2 bacteriophages (3). Work by Isenberg and Baird in 1961 also identified free radical spectra in *E. coli*, which disappeared when the cells were killed via cyanide (3).

These early studies have grown into a variety of subfields, spanning EPR imaging, oximetry, cancer detection, the study of iron/sulfur complexes, and others (4) Here, the focus will be on continuous wave (CW) and pulsed measurements of bacterial outer membrane proteins in whole *E. coli* cultures, or in native OM isolate.

2.2 The Electron in the Magnetic Field

Generally, EPR deals with the detection of systems that have discrete Zeeman levels induced by the presence of a static, external magnetic field upon their unpaired electrons. For the simplest case, of an electron orbiting an isolated atom in the static field, the Zeeman energies are:

$$H_z = \beta_e g_e H S = \beta_e g_e H_0 S_z \quad (1)$$

where β_e is the Bohr magneton, g_e is the electron's spectroscopic splitting factor, H is the external field, H₀ its magnitude, and S is the spin angular momentum (5). In the case of a single unpaired electron, which will apply for all nitroxide spin labels, the allowed values of S are $m_s = -\frac{1}{2}$ and + $\frac{1}{2}$. The difference in energy between the two spin states in this system would then be $\beta_e g H_0$ (Figure 1).



Figure 1: Zeeman splitting for an electron

Following from above, if the energy separation is $\beta_e g H_0$ then application of microwave energy can induce a transition between the two energy levels when the field strength, H₀, is equal to $\frac{hv_0}{g\beta_e}$.

This simple behavior applies to a single atom, but in an EPR experiment there are typically micromolar level spins within the resonant cavity of the instrument. In the aggregate, the magnetic moments of the electrons will become aligned parallel to the applied magnetic field. If said field is considered to be applied along the positive x-axis, then the bulk magnetization, M, will lie along this same axis (Fig. 2A). Further, the static field exerts a torque on the electrons due to their angular momenta, resulting in a precession about the field vector. The frequency at which this occurs is called the Larmor frequency, and is given by:

$$\omega_{\rm L} = -\gamma H_0 \qquad (2)$$

where γ is the gyromagnetic ratio. The presence of the field will induce the Zeeman splitting described above, with the parallel, ground state being initially more populated. In the EPR spectrometer, however, there is a second, microwave field applied perpendicular to the static field. This applied field, which will be abbreviated H₁, can induce transitions from the parallel to

the antiparallel state (Fig. 2B). This causes the bulk magnetization to no longer be fully aligned with the external field, and effectively tips it out of the positive z-axis. The bulk magnetization vector now has non-zero magnitude in the transverse axes, which allows for the detection of EPR signals by the instrument (Fig. 2C).



Figure 2. The behavior of the bulk magnetization in the presence of applied fields. (A) in the presence of a static field along the z-axis, the bulk magnetization aligns parallel to the static field. The electrons precess about the z-axis with random orientations. (B) The ground state parallel to the static field is initially more populated, but the addition of a perpendicular field supplied by the EPR instrument can induce transitions. (C) These have the effect of causing the bulk magnetization to no longer be fully aligned, effectively "tipping" it out of alignment.

Before proceeding from this simple picture, it is necessary to cover several reference frames, as well as the deviations from equation 1 that arise when moving from atoms to molecules. Relaxation effects are discussed next, followed by continuous wave experiments, and finally pulsed-EPR and the 4P Double-Electron-Electron-Resonance (DEER) experiment.

2.3 Choice of reference frame

- 1.) The laboratory frame, with axes: x, y, z. In this coordinate system, the static field is aligned along the positive z-axis, having the benefit of simplifying it to a scalar quantity in most representations.
- 2.) The molecular axis system, with axes: p, q, r. This coordinate system is aligned to the molecular principle axes, having the benefit of simplifying tensor variables related to molecular orientation to their trace.
- 3.) The rotating frame, with axes: x, y, z. This is a special modification of the laboratory frame. At resonance, where the frequency of the applied field equals the Larmor frequency, fixing

the frame of reference to said frequency renders it stationary, greatly simplifying many expressions in pulsed-EPR.

From Atoms to molecules

2.4 Anisotropy in g

For an isolated atom, the value of g_e approaches the expectation value of 2.00232 (5). In the presence of an external magnetic field and considering spin-orbit coupling, however, deviations are seen for the value of g from the expected value. The magnitude of these difference depends on the orientation of the applied magnetic field with respect to the molecule and results in g being better represented as a second-rank tensor. In the laboratory frame, the tensor can be written as:

$$g = \begin{pmatrix} g_{xx} & g_{xy} & g_{xz} \\ g_{yx} & g_{yy} & g_{yz} \\ g_{zx} & g_{zy} & g_{zz} \end{pmatrix} \rightarrow g = \begin{pmatrix} & & \\ & & \\ & & \\ g_{zx} & g_{zy} & g_{zz} \end{pmatrix}$$
(3)

In the laboratory axis system, equation 1 can then be rewritten taking into account the ganisotropy as:

$$H_{z} = \beta_{e} H_{0} (g_{zx}S_{x} + g_{zy}S_{y} + g_{zz}S_{z})$$
 (4)

where the simplification results from the magnetic field being aligned along the +z axis (5). Likewise, in the molecular axis system, the tensor is:

$$g = \begin{pmatrix} g_{pp} & g_{pq} & g_{pr} \\ g_{qp} & g_{qq} & g_{qr} \\ g_{rp} & g_{rq} & g_{rr} \end{pmatrix} \rightarrow g = \begin{pmatrix} g_{pp} & & \\ & g_{qq} & \\ & & g_{rr} \end{pmatrix}$$
(5)

The Hamiltonian in the molecular axis system now becomes:

$$H_{z} = \beta_{e} \left(g_{pp} H_{p} S_{p} + g_{qq} H_{q} S_{q} + g_{rr} H_{r} S_{r} \right) \quad (6)$$

where the extra terms H_p , H_q , H_r , reflect the fact that the vector orientation of the external field no longer coincides with one of the system axes (5). Equation 6 can also be written in terms of the direction cosines of the external field as:

$$g = \left(g_{pp}^{2}l^{2} + g_{qq}^{2}m^{2} + g_{rr}^{2}n^{2}\right)^{\frac{1}{2}}$$
(7)

Finally, Equation 6 can be written in terms of the Euler angles (a, B, y) to rotate from the laboratory axis system into the molecular one. In this form, g can be represented as:

$$g = g_{pp}^2 \sin^2 \beta \cos^2 \gamma + g_{qq}^2 \sin^2 \beta \sin^2 \gamma + g_{rr}^2 \cos^2 \beta \quad (8)$$

Where I, m, and n are the direction cosines that relate the external magnetic field to the molecular axis system (5). In this case, the Euler rotations are intrinsic, with each subsequent turn occurring in the new axis system created by the previous rotation. The order is an initial rotation α about the z-axis, followed by a rotation β about the effective y-axis, and finally a rotation γ about the effective z-axis, which now corresponds to the r axis in the molecular frame. Equations 7 and 8 are useful when considering simulations of EPR spectra.

2.5 Hyperfine Interactions

Within a nitroxide spin-label, the unpaired electron is also subject to interactions with nearby nuclei, particularly that of the nitrogen atom. The magnitude of these interactions is much greater than those of the g-tensor deviations for nitroxides. To account for them, equation 1 can be extended as follows:

$$H_{z} = -\beta_{e} g_{e} \beta_{n} g_{n} \left(\frac{(I \cdot S)r^{2} \cdot 3(I \cdot r)(S \cdot r)}{r^{5}} - \frac{8\pi}{3}(I \cdot S)\delta(r) \right) \quad (9)$$

where the subscript e refers to the electron, N to the nucleus, I is now the nuclear spin, r is the vector between the electron and nucleus, and δ denotes the dirac delta function (5). The left term describes the dipolar interaction, which again depends on the orientation of the molecule in the

magnetic field. The right term gives rise to Fermi contact coupling, and is dependent only on finite, nuclear electron density. Together, these two effects are frequently represented by the hyperfine interaction tensor, or matrix, A. As with the g-tensor, the representation for the A-tensor in the molecule's principal axis system is:

$$A = \begin{pmatrix} A_{pp} & A_{pq} & A_{pr} \\ A_{qp} & A_{qq} & A_{qr} \\ A_{rp} & A_{rq} & A_{rr} \end{pmatrix} \rightarrow A = \begin{pmatrix} A_{pp} & & \\ & A_{qq} & \\ & & A_{rr} \end{pmatrix}$$
(10)

Allowing the hyperfine Hamiltonian to be written more simply as:

$$H_{\text{hyperfine}} = I \cdot A \cdot S \rightarrow H_{\text{hyperfine}} = \left(A_{pp}I_pS_p + A_{qq}I_qS_q + A_{rr}I_rS_r\right) (11)$$

with the A-tensor now containing components representing both the dipolar and fermi contact interactions (5).

2.6 Electron-Electron interactions

While nitroxide spin labels have only a single unpaired electron, the presence of several labels within a single protein, or of labels on nearby proteins, can lead to interactions between electrons. As with the hyperfine interactions there are two main components to electron-electron interactions, an isotropic exchange interaction and a through-space, orientation dependent dipolar interaction. The former will occur in cases where there is significant orbital overlap between the two electrons, which for spin labels would require a very close separation of only a few Angstroms. The resulting exchange coupling is frequently termed Heisenberg exchange, and has the following form:

$$H_{HE} = JS_1 \cdot S_2 = \frac{1}{2}J(S^2 - S_1^2 - S_2^2) = \frac{1}{2}J(S^2 - \frac{3}{2}) \quad (11)$$

where S_1 and S_2 are the spin angular momentum of the first and second spins, respectively, and J is now the exchange energy (5). The result of this exchange function is singlet and triplet states for the coupled spins, with positive J leading to antiparallel orientations of the spins.

The through-space dipolar interaction has a much longer range, and for two electrons has the form:

$$H_{d} = g_{e}^{2} \beta_{e}^{2} \frac{((S_{1} \cdot S_{2})r^{2} \cdot 3(S_{1} \cdot r)(S_{2} \cdot r))}{r^{5}} \quad (12)$$

where S_1 and S_2 are again the spin angular momentum of the first and second spins, and r the distance between them (5). The dipolar interaction will be dealt with in more detail in the discussion of the 4P-DEER experiment.

2.7 Relaxation

The effect of the static magnetic field on the bulk magnetization was discussed in section 2.2. The presence of the static field induces a separation of the Zeeman levels for the electron, resulting in a thermal equilibrium state with more spins in the lower level parallel to the static field. The applied microwave field can then induce transitions between these levels, moving the system out of equilibrium. Of course, after the disturbance stops the system will trend back towards equilibrium. This is governed by two main rates, with corresponding constants T_1 and T_2 . The former, which is also called the spin-lattice or longitudinal relaxation time, describes the return of the z-axis component of the magnetization to equilibrium, and has the following relation:

$$\frac{dM_z}{dt} = \frac{-(M_z - M_{eq})}{T_1}, M_{eq} = \frac{Ng_e^2 \beta_e^2 S(S+1)H_0}{3kT}$$
(13, 14)

where the second expression for M_{eq} is taken from the Curie law (5). The spin-lattice relaxation is usually a mono-exponential decay.

The spin-lattice relaxation has the effect of shortening the time spent in the antiparallel state, returning them to the lower energy parallel condition. It thus has a direct effect on the Zeeman energy for the system. In contrast, T_2 , which is also called the transverse relaxation, does not affect the Zeeman energy but instead describes the loss of coherence in the x and y axes of the magnetization. The transverse relaxation has the relation:

$$\frac{\mathrm{dM}_{\mathrm{x},\mathrm{y}}}{\mathrm{dt}} = \frac{\mathrm{-M}_{\mathrm{x},\mathrm{y}}}{\mathrm{T}_2} \quad (15)$$

Equations 13 and 15 are also known as the Bloch equations for the macroscopic magnetization; introduced by Felix Bloch in 1946 (5).

2.8 Continuous wave Experiments, Broadening, and Lineshapes

To continue, it is useful to consider the conditions of an actual EPR experiment. Continuous wave, or CW, experiments are widely used in the field, and involve recording characteristic lineshapes of the paramagnetic species being studied that are highly sensitive to their local environment. Two examples of CW spectra for nitroxide labels are given in Figure 3.



Figure 3. Examples of CW EPR spectra for (A) fast, and (B) slow motional regimes.

Starting with the spectra in Fig. 3A, it is immediately apparent that the spectrum has three main features, or peaks. In the CW experiment, the applied field H₁ is held constant, and the magnetic field is swept. As noted in section 2.2, an absorbance will occur when the magnitude of the field is equal to $\frac{hv_0}{g\beta_e}$. The presence of the unpaired electron leads to two-state splitting of the Zeeman levels, but this would give a single absorbance peak. The nitroxide spin label has most of its electron density in the p-orbitals of the nitrogen atom, however, which has nuclear spin I=1. This leads to further hyperfine splitting of 2I+1 levels, giving 3 total peaks as seen in this spectrum. Also, the features themselves are derivative lines rather than absorbance peaks. This stems from the use of 100 kHz field modulation in the CW EPR

instrument coupled with phase sensitive detection, which has the effect of recording the derivative of the absorbance phenomena.

Next, the shape of the lines in Fig. 3A is characteristic of a derivative Lorentzian. This indicates the dominance of the transverse relaxation in their decay. In practice, however, there is also a Gaussian contribution from inhomogeneous broadening of the spectra due to unresolved couplings, particularly with other nuclei, that makes the lineshapes a combination of both Lorentzian and Gaussian features (6). This combination is termed a derivative Voigt profile (6). The Lorentzian contribution from the transverse relaxation can be read off the spectra quite easily, as it is inversely proportional to the peak-to-peak height, ΔH_{pp} , of the central line:

$$\frac{1}{T_2} = (\frac{\sqrt{3}}{2})\Delta H_{pp}$$
 (16)

where ΔH_{pp} , is the peak-to-peak magnitude (5). Comparing the spectrum in Fig. 3B to that of Fig. 3A, it is apparent that the lines of the spectra in Fig. 3A are sharp and narrow, while those of Fig. 3B are broadened and of greatly reduced magnitude. Even in the sharp spectrum, however, the peaks are not the same height, with the rightmost peak having significantly reduced amplitude. For lines corresponding to Lorentzian derivative functions, the height scales with the inverse of the width squared, and thus the different peaks, and by extension the two example spectra, must be differentially broadened.

To deal with this, it is necessary to add in the contributions of motion for the spin labels and their covalently bound proteins. EPR experiments are sensitive to motions on the nanosecond timescale, which captures tumbling of the spin probe as well as local conformational rearrangement of the protein backbone, and even protein tumbling for smaller proteins. As several of the effects described in the previous sections were orientation dependent, changes in orientation on the EPR timescale will result in fluctuations in the energy levels and subsequent positions of the transition frequencies for the individual spins. On the bulk level, this would be expected to lead to broadening of the absorbance envelope, and subsequently of the observed derivative spectrum.

The degree of reorientation can be represented by the rotational correlation time, which has the form:

$$\tau_{\rm c} = (6D)^{-1}, D = \frac{kT}{8\pi\eta R^3}$$
 (17)

with τ_c representing the rotational correlation time, D the rotational diffusion constant, and η the viscosity (5). Small values of τ_c (< 1 ns) reflect a short residence time in any given conformation and are common for solution spectra with a high degree of isotropic averaging. This is true for the spectra in Fig. 3A, which is a free MTSL spin label in aqueous conditions. As the rotational correlation time increases, in contrast, there is progressive broadening of the lines. This broadening is described by the following equation:

$$(T_2(M))^{-1} = A + BM + CM^2$$
 (18)

where A, B, and C modulate the linewidths of the spectral lines, and M specifies the transition (5). The A term acts upon all three lines in a nitroxide spectra, and accounts for non-anisotropic factors, including paramagnetic broadening agents in the solution and instrumental uncertainty. The B and C terms, however, must act differently upon each line to give rise to the unequal line heights observed in the sample spectra in Figure 3. For a nitroxide in solution, they have the following relation:

$$(T_2(0)^{-1}\left(\frac{T_2(0)}{T_2(\pm 1)}, 1\right)) = C \pm B$$
 (19)

where $T_2(0)^{-1}$ is the width of the central spectral line, which has transition number M=0 (5). The B and C terms themselves are derivative of the anisotropy in the g-tensor and hyperfine interactions discussed earlier, but for this discussion it is sufficient to consider two simplified cases. The three lines in the nitroxide spectrum, from left to right, have M values of 1, 0, and -1,

respectively. At X-band, the value of B is approximately equal to -C, and so the contributions to the left (lowfield) and center peaks are approximately cancelled out (5). In contrast, the right peak (highfield) will have an additive effect from both terms and will appear to be substantially broader and shorter than the other two peaks. At Q-band, the B term increases in magnitude, and so while the highfield line remains the broadest, the lowfield line will begin to diverge in height from the center line (5).

These highly simplified relations work only for quickly tumbling species in solution. For cases of intermediate exchange, or highly anisotropic or solid systems it is necessary to use more rigorous treatments. The reader is referred to treatments of the Microscopic Order Macroscopic Disorder (MOMD) model, and to a review chapter by Schneider and Freed (7, 8).

Pulsed-EPR

2.9 Intro

In a pulsed-EPR experiment, the magnet again creates a static magnetic field, which is aligned with the z-axis in the laboratory frame. The microwave source, meanwhile, produces linearly polarized microwaves that create a field perpendicular to the static field, along either the x or y-axis. In contrast to the CW experiment, however, the second field does not remain on, but is instead pulsed for discrete time intervals. The behavior of the bulk magnetization, M, in the presence of a static magnetic field was presented in section 2.2. Here, the magnetization will be defined in terms of the magnetic induction, B, with the following relation:

$$M_0 = \frac{B_0}{\mu_0} - H_0$$
 (20)

where H_0 is the magnitude of the static field, and μ_0 the sum of the individual spin magnetic moments (9). The magnetic induction is used in place of the magnetic field for the duration of this pulse EPR section. The static and applied fields are now denoted B_0 and B_1 , respectively. The presence of the static field creates a separation between the Zeeman levels of the affected spins, and transitions can again be induced between them when the applied RF radiation from the B₁ field is matched to the energy separation of the two levels. With B₀ aligned along the +z-axis, the spins will begin an initial precession about the same axis with frequency ω_0 , also termed the Larmor frequency. To simplify the treatment of pulse experiments, the rotating frame, described in section 2.3 is used, where the frame of reference is fixed to a particular frequency of B₁. The former causes the bulk magnetization to be initially stationary in the rotating frame, but the latter makes B₁ time independent. Here, the rotating frame is assumed to be fixed to the B₁ frequency, denoted $\omega_{applied}$.

With this choice of reference, any deviation between the larmor frequency of a group of spins and the B₁ frequency will cause the magnetization to again rotate with a frequency offset, ω_{off} , equal to the difference between the two. Additionally, while the intensity of B₁ is nonzero, it will induce an additional precession about the transverse axis along which the B₁ field is applied. Control over the direction of the B₁ field, and thus over the axis of precession for the magnetization, is produced by changing the phase of the linearly polarized microwaves. In the rotating frame, the direction of B₁ as a function of a phase angle, Φ , is given by:

$$B_{1x} = B_1 \cos \Phi$$
, $B_{1y} = B_1 \sin \Phi$, $B_{1z} = 0$ (21)

If B_1 is held on, the magnetization will thus continue to precess about the transverse axis along which B_1 is applied. But if the field is applied for only a brief period, on the order of tens of nanoseconds, then the magnetization will not have time to fully rotate and the length of such a pulse can be used to control its tip angle as:

$$\angle = \omega_1 t_p$$
 (22)

where \angle is the angle of rotation for the magnetization, ω_1 is the frequency of precession about B₁, and t_p is the pulse length. Pulses are typically named for their angle of rotation, with the most common being the $\pi/2$ pulse, producing a 90° rotation, and the π pulse, which produces a full 180° inversion.

In the simplest case, of the application of a single pulse of some angle \angle which is \neq 180°, the magnetization will be rotated about the chosen transverse axis. After the pulse is finished, the system will continue to precess about B₀, and will eventually relax back to equilibrium. In the rotating frame, the Bloch equations describing the relaxation are:

$$\frac{dM_x}{dt} = -\omega_{off}M_y - \frac{M_x}{T_2}, \quad \frac{dM_y}{dt} = \omega_{off}M_x - \omega_1M_z - \frac{M_y}{T_2}, \quad \frac{dM_z}{dt} = \omega_1M_y - \frac{M_z - M_0}{T_1}$$
(23)

where T_1 and T_2 _{again} represent the spin-lattice and transverse relaxation times, respectively (9). The components of the bulk magnetization will then be described by:

$$M_{x}t = M_{0}\sin(\angle)\sin(\omega_{off}t)e^{\frac{1}{T_{2}}}, M_{x}t = -M_{0}\sin(\angle)\cos(\omega_{off}t)e^{\frac{1}{T_{2}}}$$
 (24)

where it should be noted that in pulsed-EPR, the signal is normally detected in quadrature. Similar to the use of 100 kHz field modulation in CW EPR detection, the output of the microwave resonator in the pulse experiment is mixed with the microwave source, and so the detected signal is technically the offset frequency, ω_{off} . As described in equation 21, in the rotating frame, direction is represented by a phase shift, and the signal components in the x and y-axis are separated by 90°. Generally, this means the overall signal is encoded as a complex number, with the phase adjusted to maximize the signal intensity in the real. This can also be seen above in equation 24, with the exchange of the sin term for cos when moving between the M_x and M_y components. The resulting complex signal, which in this single pulse experiment decays as a pseudo mono-exponential, is called a free induction decay or FID and has the form:

$$V(t) \propto e^{i\omega_{off}t}e^{\frac{1}{T_2}}$$
 (25)

where V(t) will be used for all time-domain signals moving forward (9). The FID is the basis of the majority of detected quantities in pulse-EPR, including the echo, which will be explored in section 2.12.

Compared to CW EPR experiments, which for biological systems are usually performed in aqueous solution and at RT, pulsed experiments typically use frozen, solid phase samples. This presents a variety of additional problems related to relaxation and broadening effects that are explored in more detail in the following two sections.

2.10 Relaxation II

The spin-lattice or longitudinal relaxation process, which is described by T₁, was briefly described in Section 2.7. Longitudinal relaxation changes the overall system energy by changing the spin state of individual electrons, and has three main component processes: spontaneous emission, direct absorption of lattice vibrational energy, and Raman transitions.

The rate of spontaneous emission is dependent on the frequency cubed, with the form:

$$W = \frac{2}{3} \frac{\mu_0 g^2 \beta_e^2 \omega^3}{4\pi \hbar c^3} \quad (26)$$

but even in the GHz region of X and Q-band, it would still take many years for the system to decay back to thermal equilibrium through emission alone (9). Instead, the longitudinal relaxation is dominated in liquids by Brownian motion, which can be described by Redfield theory, where molecular reorientation adjusts the hyperfine, exchange, and spin-spin interaction energies, causing fluctuating local fields, which will induce transitions in spins if they match the Larmor frequency. In solids, meanwhile, longitudinal relaxation is dominated by the transfer of energy from vibrations in the lattice to the spins. This can be direct, where a unit of lattice energy, or phonon, is absorbed by the system, or it can be through a virtual Raman process. Direct absorption dominates at the extremely low temperatures used in liquid helium experiments, typically below 5-10K, and in the intermediate regime used in the DEER experiment, of between 40-80 K, the relaxation will be primarily through Raman processes (9).

The transverse relaxation process, described by T₂, does not change the total system energy, but instead involves exchange of spin-states between different members of the system or ensemble. This is particularly relevant to pulse experiments, where pulses have limited bandwidth and both detection and excitation will affect only a subpopulation of spins in the system. Thus, transfer of the magnetization to unaffected spins will have the affect of making it effectively invisible or decreasing the measured signal intensity.

In liquids, transverse relaxation through spin flip-flops is again dependent on the rate of reorientation and can be described through Redfield Theory where in general, $T_2 \leq T_1$. In solids, rearrangement is much more limited, and many spins may be coupled, with an infinitely coupled approximation sometimes employed. Nuclear spin flip-flops are also possible, causing changes in the hyperfine interaction that again contribute to transverse dephasing. For pulse experiments in frozen samples, nuclear flip-flops via matrix protons can come to dominate longer time relaxation. The limited mobility inherent in frozen samples also brings in additional factors that influence the decay of the transverse magnetization, including spectral and instantaneous diffusion. As a result, T_2 is usually replaced with the phase memory time, T_m , which is related to the decay of spin echos described in section 2.12.

Spectral diffusion is the formal term for the situation described above, where the entire spectrum is not excited by a pulse in an experiment, creating separate pools of affected A spins and unaffected B spins. Energy can be exchanged between the A and B spin populations, and if only the A spins are detectable, this will manifest as an enhancement of the signal decay.

In contrast, instantaneous diffusion describes the fact that in a frozen, solid-phase sample, different A spins affected by a particular pulse are differentially oriented and spaced relative to

each other. This means that the application of the pulse changes the spin-spin dipolar interaction between them and has a subtle resultant affect on the local field, creating additional offsets between spin-packets and resulting in further decay of the transverse signal. The name comes from the very short timeframe of the pulses, which is near instantaneous relative to periods where the pulse is not applied, and the spin system is allowed to precess or evolve.

2.11 Homogeneous and Inhomogeneous Line Broadening

Within a spin system or ensemble, some spins will be similar enough in environment to be considered as sharing the same effective field. In pulse experiments, these groups of spins are termed packets or spin-packets. As described in section 2.8, the base shape of an EPR line for each of these spin-packets is Lorentzian and the lines will be homogeneously broadened, as they all share the same effective field. The overall EPR spectrum, in comparison, is composed of a multitude of these individual packets at different frequencies. An additive set of Lorentzian peaks has an overall Gaussian shape, and is inhomogeneously broadened. Inhomogeneous broadening is much more apparent in transition metal systems and systems where the electron is delocalized, both of which enhance anisotropic effects of the electron and nuclear interactions and the inability to resolve hyperfine couplings in the requisite spectra.

2.12 Pulse Sequences and Echos

Building from the basic concepts of pulse EPR described in Section 2.10, a simple 2-pulse experiment and the behavior of the bulk magnetization is shown in Figure 4.


Figure 4. The behavior of the bulk magnetization in the presence of applied microwave pulses.

Initially, the bulk magnetization vector, M, is aligned with the z-axis parallel with the static field. At some time, t, a $\pi/2$ pulse is then applied, and M is rotated 90° into the transverse xy plane. When the pulse stops, the system continues to precess about the z-axis, although the individual spin packets will carry unique frequencies and thus will begin to travel at different rates in the rotating frame. As time continues, M will begin to lose coherence in the transverse plane and dephase. At this point, a π pulse is applied to rotate M 180°, effectively flipping it. This pulse can also be called a refocusing pulse, as the rate differences of the various spin packets remain constant, meaning that after the flip they now act to bring the various vectors back together, restoring the coherence of M in the xy plane. After coherence is reestablished, the spin packets will continue to move and the overall signal will again decay as they did after the application of the initial $\pi/2$ pulse. The combination of the refocusing and subsequent loss of focus period produces a quasi-exponential rise and fall in the signal, which is called an echo, spin-echo, or Hahn echo. Echos can also be considered as back-to-back FIDs.

In practice, all pulse experiments are created by stringing together sequences of pulses in one or more frequencies. The detectable quantity is either a FID or an echo, but this simple set of tools can result in a multitude of detectable quantities, ranging from relaxation times to local motion to nuclear states to the distance between pairs of excited spins. The following sections describe the Double Electron-Electron Resonance (DEER) experiment, which detects the dipolar correlation between pairs of electron spins, and the factors that affect the experiment's performance.

2.13 The DEER Experiment

The pulse sequence for the 4-pulse DEER experiment used in the majority of the experiments in this work is shown in Figure 5. The 4-pulse experiment is derivative of an original, 3-pulse sequence, with the aim of improving the originals resolvable distance range and signal to noise ratio (SNR). The standard DEER experiment employs pulses in two different frequencies, the observe frequency and the pump frequency. A variant of the technique, the 2+1 experiment,



Figure 5. The pulse sequences and echo positions of the (A) 4-pulse DEER experiment and (B) 5-pulse DEER experiment. requires only a single frequency but is not presented here. In the observe frequency, a series of 3 pulses with fixed separation are applied to an initial population of A-spins. The initial $\pi/2$ pulse rotates the magnetization into the xy plane, after which it is allowed to precess for a time interval t₁. A refocusing π pulse is then applied, which produces a spin-echo whose maximum occurs at a time t₁ after this first π pulse ends. The final refocusing π pulse in the observe frequency is separated from the first by a time t₂, and thus an additional refocused echo appears after this third observe pulse with a maximum at t₂-t₁.

During the second evolution, after the maximum point occurs in the first spin-echo, the dipolar coupling of the A-spins is modulated by applying a pump π pulse in the second frequency. The pump pulse excites a separate group of B-spins, with the change in magnitude of the dipolar interaction influencing the height of the second refocused echo. The magnitude of this effect is time dependent, and so the experiment is repeated many times, with the position of the pump

pulse being stepped through the available time interval t_2 - t_1 during which the spins precess before the second refocusing pulse is applied in the observe frequency.

The time-domain signal obtained from the DEER experiment has a decaying oscillatory form, and is given by the following expression:

$$V(t) = (1 - \lambda (1 - \int_0^1 \cos(\omega_{ee} (1 - 3\cos^2 \theta_i)t) d\cos \theta))B(t), \ \omega_{ee} = \frac{\mu_0 \gamma_e^2 \hbar}{4\pi r^3}$$
(27)

where V(t) is the signal, λ is the inversion frequency, being the fraction of B spins that are coupled to A spins and successfully inverted by the pump pulse, ω_{ee} is the dipolar coupling frequency, θ is the angle between the dipolar coupling vector and the static field, r its distance, and γ_e is the electron gyromagnetic ratio (10, 11). The term B(t) represents the background function contributing to additional signal decay. Typically, the DEER experiment is performed for biradicals, or for proteins with two spin labels attached at different locations. Thus, the desired information is the intramolecular dipolar coupling. The presence of other molecules leads to a significant contribution from intermolecular couplings, however, and so the signal is often represented as a product of the intramolecular form factor F(t) and a background function B(t) as given in equation 28:

$$V(t) = F(t)B(t)$$
 (28)

Determination of the background term is reliant on assumptions regarding the nature of the molecular level organization of a sample. The most common choice involves assuming a homogeneous distribution of hard-sphere particles according to the shell-factorization model, where the distribution is assumed to have fractal dimension d. Such a background creates a stretched-exponential signal decay with the form:

$$B(t) = \exp(-k_{id}t^{\frac{d}{3}})$$
 (29)

where k_{id} is the rate of instantaneous diffusion, and makes the degree of background decay dependent on the spin concentration (9). The value of the fractal dimension d loosely maps to the geometry of common sample conditions, with d≈3 for aqueous or detergent-solubilized proteins and d≈2 for proteins on cellular surfaces or in lipid vesicles. In practice, the dimension varies between values of slightly below 2 up to 4, with values greater than 3 typically indicating violations of the shell-factorization model in the form of crowding or excluded-volume effects (12, 13).

2.14 Data Processing and Extraction of the Intramolecular Distances

An example of the data produced in a DEER experiment, and its subsequent analysis is presented in figure 6. The oscillatory decay form of the time-domain signal is immediately apparent in Fig. 6A, but as mentioned above, it contains information on both the intramolecular interaction of interest and the unwanted intermolecular interactions. Separation of the background signal from the desired intramolecular form factor, and conversion from the time-



Figure 6. Examples of (A) time-domain data V(t), (B) the intramolecular form-factor F(t), and (C) the resulting distance distribution for a 4-pulse DEER experiment.

domain data to a distance distribution can be handled with either a model-free, or model-based approach.

2.15 Preprocessing

The original time-domain signal requires several adjustments before either method can be employed for extraction of the pair-wise distances. First, the signal-acquisition time usually begins before the maximum of the spin-echo is reached, and so the zero-time must be determined. This typically involves either a Gaussian-fit to the initial data points, or a simple selection of the greatest magnitude value in the dataset. Additionally, the end of time-traces for 4-pulse DEER experiments using rectangular pulses typically contains an artifact resulting from the imperfect separation of the observe and pump pulses. This artifact is the result of the first two observe pulses and the overlapping portion of the pump pulse producing an analogue of the 2+1 experiment mentioned briefly at the beginning of this section (14). The 2+1 experiment is a single-frequency variant for the detection of electron-electron coupling, and it manifests as additional oscillations in the data that become more apparent at the end of the time-trace. Fortunately, the effect of the 2+1 artifact can be minimized by subtraction of the final 5-10 points of the trace, or by using Gaussian or other shaped pulses in place of the traditional rectangular pulses during the experiment. Finally, the time-trace is recorded in quadrature, and the data is typically phased using a Hilbert transform to move all of the signal intensity into the real component.

2.16 Model-Free Analysis

Changing between the initial time-trace and the parwise distance distribution is an illposed problem, requiring some method to solve a Fredholm equation of the first kind, with varied possible solutions. The most common method used to deal with this problem is Tikhonov regularization, which has been implemented in software available from the Acert Group at Cornell, and in the widely used DeerAnalysis package by the Jeschke group at ETH Zurich (15, 16). Prior to extraction of the distance distribution, a background function of the stretched-exponential form given in Equation 29 is fit to the data with the fractal dimension being varied, and the resulting equation is subtracted from the time-trace to yield the intramolecular form factor shown in Figure 6B. This can then be used for extraction of the pairwise-distance distribution, as in Figure 6C.

For this case, the Tikhonov functional has the following form:

$$\Phi[P] = \|KP-S\|^2 + \lambda^2 \|LP\|^2 \quad (30)$$

where || || is the Euclidean norm, S is the time-domain data vector with size N, P is the distancedomain solution vector with size M, L is an identity or second-derivative matrix operator, and K is an MxN matrix whose elements contain the discrete approximation for the dipolar interaction between spin-pairs (16). The left-hand side of equation 30 is the residual norm, which is minimized in standard linear regression. Unfortunately, in this case minimizing the residual norm alone produces a solution that is derived mainly from noise and imprecision in the data. Thus, the solution norm in the second term is preceded by a regularization factor, λ , which enforces a degree of smoothness on the solution. The solution to equation 30 can be expressed in terms of the value of the regularization factor as:

$$P_{\lambda} = (K^{T}K + \lambda^{2}L^{T}L)^{-1}K^{T}S \quad (31)$$

but some method must still be employed to select the optimal value of λ (16). The most widely used when fitting DEER data is the L-curve, which is a plot of the solution norm on the y-axis against the residual norm on the x-axis for all tested values of λ . The shape of the curve is always somewhat L shaped, and the corner of the curve is usually selected as the optimum value of λ . Qualitatively, this location represents the point where the agreement between the solution and the data no longer changes rapidly with increasing smoothness of the solution.

Recently, a variety of improvements have been developed for fitting using Tikhonov and related model-free approaches. The program LongDistances by Christian Altenbach at UCLA uses a variant smoothing-factor in place of the classical regularization parameter, which may increase the quality of the resulting solutions. The L-curve method for selection of λ can also be replaced, with Edwards et al. finding that information criterion values, such as the Akaikake information criterion (AIC) or Bayesian information criterion (BIC), as well as cross-validation methods, can all outperform the L-curve in many situations (17). More recently, several

alternatives to Tikhonov regularization were tried, with Ibanez et al. determining that Osher's Bregman-iterated regularization (OBIR) typically performed the best across a dataset of more than 620,000 noisy signals derived from a T4 lysozyme crystal structure (18). Finally, Worswick et al. have produced a feed-forward neural network, DEERNet, which functions as an alternative, general Fredholm solver for these problems (19).

2.17 Model-Based Analysis

In contrast to the model-free methods, DEER distance distributions can also be modeled as a sum of Gaussian components. This approach allows for the background function to be cofit with the distribution. Under this scheme, the form-factor in Figure 6B is produced at the same time as the distance distribution in Figure 6C. This is particularly beneficial in cases where the time-trace is relatively short, making background determination and subtraction before fitting difficult. A simple approach for fitting of n Gaussian components and a homogeneous background is present in the DeerAnalysis package mentioned above, but more rigorous implementations are available in LongDistances and particularly in the proGram DD by Eric Hustedt at Vanderbilt (20). The latter package also allows for adjustment of the background factor to one that accounts for deviations related to excluded volume effects, where the spin-labels are only able to approach to a certain non-zero minimum distance.

As the distribution is modeled as a set of discrete Gaussian components, the selection of the number of peaks can be handled easily by finding the minimum of the AIC or BIC values. This is in sharp contrast to the difficulty in determining the optimal value of λ in the Tikhonov regularization methods (20). Overall fit quality is generally assessed through the value of χ^2 after fitting, with a value near 1 being an ideal fit where the error is explained solely by data noise (20).

Methods

2.18 Plasmids and Strains

Plasmid pAG1 (Figure 7) containing the *btuB* gene was originally provided by the Kadner group at the University of Virginia. *E. coli* K-12 strain RK5016 (*-argH, -btuB, -metE*), and the following strains from the Coli Genetic Stock Center at Yale: strain RI89 (*araD139* Δ (*araABC-leu*)7679 galU galK Δ (*lac*)X74 rpsl thi phoR Δ ara714 leu⁺), strain RI90 (RI89 dsbA:: Kan^r), strain RI317 (RI89 dsbA:: Kan^r), and strain RI179 (RI89 dsbC:: Kan^r), were provided by the Nakamoto lab at the University of Virginia. Top10 cells were purchased from Thermo Fisher Scientific (Waltham, MA).



Figure 7. Sequence map of the pAG1 vector used for BtuB expression in this work. NGS sequencing performed by Applied Biological Materials Inc. (Richmond, BC). Image generated in SnapGene.

2.19 Mutants

BtuB mutants based on the following sites: 6, 74, 90, 188, 288, 384, 510, were generated in the Cafiso lab by Dr. Thushani Nilaweera or previous members. Primers were purchased through Integrated DNA Technologies (Coralville, IA). BtuB mutants based on the following sites: 55, 57, 62, 63, 65, 67, 72, 91, 93, 98, 237, 304, 330, 403, 404, 450, 451, 491, 493, 494, were purchased from Applied Biological Materials Inc. (Richmond, BC, Canada).

2.20 Standard Materials

Mono and disodium phosphate were obtained from Chem-Impex (Wood Dale, IL). Ampicillin and AEBSF were obtained from Cayman Chemical (Ann Arbor, MI). HEPES was obtained from Bio-Basic (Toronto, Ontario, Canada). MES was obtained from GoldBio (St. Louis, MO). Glucose was obtained from Sigma-Aldrich (St. Louis, MO). Ammonium sulfate, sodium citrate, thiamine, methionine, arginine, calcium chloride, magnesium sulfate, and sarkosyl were obtained from Fisher Scientific (Waltham, MA). DNAse was obtained from Applied Biological Materials Inc. (Richmond, Britich Columbia, Canada).

2.21 Nonstandard Materials

The tempo-labeled cyanocobalamin analogue (tempo-B12) was provided by Dr. Benesh Joseph (University of Frankfurt, Germany). The MTSSL spin label was purchased from Cayman Chemical (Ann Arbor, MI). CW EPR and pulse experiments used glass capillaries purchased from Vitrocom (Mountain Lakes, NJ) of the following dimensions: 0.84 mm O.D. x 0.6 mm I.D. for CW experiments, and 1.6 mm O.D. x 1.1 mm I.D. for pulse experiments.

2.22 Preparation of Whole Cell Samples

Preparation of whole *E. coli* cells with spin-labeled, overexpressed BtuB followed a general schema, with a variety of substitutions for: growth time, buffer composition, spin label concentration, number of washes, and length of wash steps. The ranges for each are given in the following text, and specific values will be noted as needed in the following chapters.

Plasmids containing the desired single or double-mutation in the *btuB* gene were transformed into one of the strains above. A single colony was then used to inoculate minimal media (MM, 100 mM phosphate buffer, 8 mM (NH₄SO₄), 2 mM sodium citrate, 200 µg/mL ampicillin, 0.2% w/v glucose, 150 µM thiamine, 3 mM MgSO₄, 300 µM CaCl₂, 0.01% w/v methionine, and 0.01% w/v arginine) precultures, which were grown overnight at 34°C. Precultures were then used to inoculate MM maincultures, which were grown to an optical density (OD) of either 0.3 or 0.6, corresponding to early and mid-log phase growth, respectively. Cells were then collected in 50 mL aliquots and centrifuged at 3260 x g for 10 minutes at 4° C. The resulting cell pellet was resuspended in 10 mL of wash buffer (100 mM HEPES, pH 7 or 100 mM MES, pH 5.5) and MTSSL was added for spin labeling at concentrations ranging from 0.01 to 5 mg / mL. Labeling proceeded in the dark for between 15 minutes and 1 hr, after which the cells were resuspended in wash buffer and incubated either on-ice or at RT for up to 1 hour. Final collection of the cell pellets involved centrifugation at 3260 x g for 6 minutes and subsequent surface washes prior to use. The particular conditions for each experiment will be noted as they appear in later chapters.

2.23 Preparation of Isolated Outer Membranes

Plasmids containing the desired single or double-mutation in the *btuB* gene were transformed into one of the strains above. A single colony was again used to inoculate 10 mL MM precultures, which were grown overnight at 34°C. Precultures were used to ioculate MM maincultures, which were grown for 8 hours. Cells were pelleted at 6,080 x g for 10 minutes and the pellets were resuspended in 10-15 mL of 0.1 M HEPES, pH 8.0 (HEPES buffer), supplemented with 20 μ L of 20 mM AEBSF and 1 μ L of DNase. Cells were disrupted using a French pressure cell, and the cell debris was pelleted out through centrifugation with an SS-34 rotor at 17,210 x g for 20 minutes. The resulting supernatant was then spun at 118,730 x g in a floorstand ultracentrifuge for 60 minutes to pellet the membrane fractions, after which the pellets

were resuspended in HEPES buffer supplemented with 1% sarkosyl. The resuspension was then incubated at 37° C for 30 minutes, followed by a second 60 minute spin at 118,730 x g. The pellet was resuspended in HEPES buffer to a final volume of 5 mL, and 1-2 mg of MTSSL was added for spin labeling, which proceeded for 2 hours in the dark. Following spin labeling, the sample was spun at 125,750 x g for 20 minutes. The supernatant was discarded, and the pellet surface washed 3 times with HEPES buffer. The pellet was resuspended and spun in a tabletop-ultracentrifuge at 156,424 x g for 20 minutes. The pellet was surface washed twice with HEPES buffer, and manually resuspended into the same buffer using a pipette tip. The tabletop spin-wash-resuspend cycle was repeated two or three additional times, after which the pellets were resuspended in minimal volume HEPES buffer and flash frozen in liquid nitrogen for storage.

2.24 Preparation of EPR Samples

For CW samples, approximately 6 μ L of concentrated cell pellet or minimally resuspended OM was loaded into 0.84 mm x 0.6 mm capillaries. The pellet was spun to the bottom of the capillary using a hand-crank centrifuge, and the tubes were loaded into an ER 4123D dielectric resonator.

For DEER experiments, 16 μ L of concentrated cell pellet or minimally resuspended OM was combined with 4 μ L of deuterated glycerol. To test the effect of substrate, some also contained cyanocobalamin, although the total sample volume was kept between 20 and 22 μ L. Samples were loaded into 1.6 mm x 1.1 mm capillaries and flash-frozen either in liquid nitrogen or a dry-ice and isopropanol mixture. The flash-frozen samples were then stored in a -80 freezer until use.

2.25 CW Experiments

All CW experiments were performed on a Bruker EMX spectrometer. Experiments were conducted at RT, with a 100 Gauss sweep-width, 1 Gauss modulation, and 2 mW incident power.

Spectra were recorded either as an additive sum of n scans or as a time-scan, where each successive scan was added row-wise to form a 2d matrix. The separation between scans in each time-scan was marginally greater than the per-scan time of 21 seconds. Phasing and normalization of the data used my own software written in python and leveraging either the matplotlib package or the DASH and Plotly.py libraries by Plotly. Subtraction of free-spin from the spectra used LabVIEW software provided by Dr. Christian Altenbach at UCLA.

2.26 DEER Experiments

All DEER experiments were performed on a Bruker E580 spectrometer operating at Qband with an EN5107D2 dielectric resonator. For experiments detailed in Chapters 2 and 3, the instrument was equipped with a SpinJet AWG, a 10 W solid state amplifier, and experiments were run at 80 K. For the experiments detailed in Chapter 5, the instrument was instead equipped with a 300 W TWT amplifier and a cryogen-free cooling system, which allowed experiments to be performed at 60 K. Most experiments used the standard dead-time free 4-pulse DEER experiment, with an 18 ns $\pi/2$ pulse and 36 ns π pulses. The separation between observe and pump frequencies was 75 MHz. In chapters 3 and 4, all pulses were rectangular.

Data analysis for DEER experiments used one of DeerAnalysis2015, DD version 7.b, or LongDistances version 785 depending on the application. In DeerAnalysis, data were loaded and the phase and start time of the decay were determined automatically in the proGram. The 2+1 pulse artifact was minimized by removing the number of data points required to remove any nonzero oscillations in the imaginary data channel. Typically, this resulted in the removal of 5 or 6 data points. The background start time was determined automatically, but the background dimension was determined manually between values of 2.0 and 3.0 by examining the curvature of the resulting form factor after subtraction. Distance distributions were fit using the standard Tikhonov-regularization options, and the value of the regularization parameter was determined

by selecting either the corner of the L-curve, or one point lower if it significantly improved the visual quality of the fit.

In DD, data were loaded and the initial preprocessing was handled by the software. A total of approximately 50 ns of data was removed to compensate for the 2+1 pulse artifact, which is equivalent to the removal of 5 or 6 data points as in DeerAnalysis. The position, width, and percentage contribution of each Gaussian component were free components in the fit. Additional free components were the background parameters, the modulation depth, and a scaling factor. The number of Gaussian components was picked by manually refitting for 1 to 4 components and selecting the fit with the lowest value of the AIC and BIC.

In LongDistances, data were loaded and the phase and start time were determined automatically in the proGram. 5 to 6 data points were truncated from the end to suppress the 2+1 artifact, as in the DeerAnalysis procedure. The background was fit to a stretched exponential with a quadratic dimension expansion of $B(t) = \exp(b_1 + b_2 t + b_3 t^2)$. Distances were then fit one of two ways. 1. A model free approach where the smoothing factor was picked based on the corner of the L-curve as in DeerAnalysis. 2. A model based approach using Gaussian components. In the model based approach, the initial background subtracting was refined by background cofitting, as in the DD protocol.

2.27 Figure Generation

Figures for CW experiments were generated using my own software written in python, matplotlib, QT 5, and the PYQT python bindings to the QT framework. Figures for DEER experiments were generated in the same way using a different version of the CW proGram, or with one of my web-dashboards running on the Heroku cloud platform, again written in python and the DASH and plotly.py libraries by Plotly. Structure figures were generated using Pymol or UCSF Chimera.

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Wavelet Denoising of Slow-Motional CW EPR Spectra

3.1 Background and Transforms

CW EPR spectra are commonly used for both qualitative lineshape analysis and quantitative comparisons in titrations or other series evaluations. In the former case, the shape of the signal is crucial in determining the environment and thus location of the paramagnetic label. In the latter case, reliable measures of peak height and width are critical to the determination of accurate binding, dissociation, or other constants. In practice, however, all EPR data is convolved with noise, which for many protein EPR samples dominates the spectra. Traditionally, the signal-to-noise ratio (SNR) is enhanced by additive averaging, with successive scans being added together to achieve a square-root n improvement in SNR. Still, the relatively long time-per-scan on commercial hardware (about 21 seconds for the Bruker EMX), and low gain through additive averaging can result in some samples being scanned for many hundreds of scans and thus many hours. Additionally, there is usually a residual underlying contribution to the signal from the resonator cavity in which the sample is held, and its contribution increases with the number of scans. Thus, the determination of alternative ways to improve SNR is highly desirable.

The approach presented here uses wavelet threshold denoising to recover underlying signal traces from noisy EPR data. Wavelet denoising builds upon earlier work in the field of Fourier denoising. Where Fourier transforms provide information on the frequency content of a given signal, the finite basis of wavelet transforms allows the recovery of both frequency and spatial information. Generally, wavelets are basis functions in Hilbert space, which exist in families defined by their mother wavelet, $\psi(t)$. The continuous wavelet transform can be written:

$$CWT = \frac{1}{\sqrt{a}} \int_{-\infty}^{\infty} \psi \frac{t \cdot b}{a} x(t) dt \quad (1)$$

where a denotes dilation and is thus related to frequency, and b denotes translation is thus related to position. For computational purposes, determination of the inner products in (1) is usually handled using the discrete wavelet transform (DWT), first proposed by Mallat in the 1980s (1). In the DWT, the dilation (a) and translation (b) parameters have the form:

$$a = 2^{-j}, b = k^* 2^{-j}$$
 (2)

forming a discrete grid over which the DWT can be computed for integer j and k. The method determined by Mallat for the DWT is a pyramidal algorithm which decomposes the signal into successive approximation and detail arrays with index k for j decomposition levels (1). A schematic representation of the DWT is shown below:



For each decomposition level, the signal is passed through both a low-pass filter and a high-pass filter. The low-pass filter leaves behind low frequency elements, and thus produces an approximation of the underlying signal. The high-pass filter leaves behind high frequency elements that provide the details of the signal and is initially dominated by noise. The signals are then decimated, and the procedure is repeated starting from the low-pass output / approximation from the previous level. This is repeated for j levels, creating a filter bank where the detail coefficients from the high-pass outputs at each level are retained, along with the approximation coefficients from the final transform level.

These filters are in turn derived from transformations of the parent wavelet. The low-pass filters are derived from shifting and scaling of the mother wavelet (wavelet function). The high-pass filters are derived from a corresponding father wavelet (scaling function). The choice of mother wavelet, and thus on the corresponding filter bank, is dependent on the form of a given signal and is often selected through experimentation. The wavelets used in this work are derivatives of the coiflet and biorthogonal families and are shown below in Figure 1.



Figure 1. The wavelet and scaling functions for the wavelets used in this work. (A) The coif3, coif4, and coif5 coiflets. The numbers refer to the number of vanishing moments in the scaling functions. (B and C) the bior2.2, bior2.4, and bior 2.6 biorthogonal wavelets. In this case, different wavelet and scaling functions are used for decomposition and reconstruction of the signal. The numbers refer to the number of vanishing moments in the reconstruction and decomposition scaling functions, respectively.

To illustrate the noise versus signal content of successive levels of detail and approximation coefficients, the results of decomposing a test EPR signal with the DWT and the coif3 wavelet to the j=8 level are shown in Figure 2. The detail coefficients are shown in the left panel, and the approximations are shown in the right. Initially, the details are dominated by high frequency noise, with the approximation becoming successively less noisy as j increases.



Figure 2. The results of decomposing a test EPR signal to j=8 levels with the DWT and coif3 wavelet. The detail coefficients are shown on the left, and approximation coefficients on the right. The level of decomposition increases going down. Initially, the details are dominated by noise, but by the 5th level begin to contain some elements of the underlying signal. By levels 7 and 8, the signal is split between approximations and details

Transitioning from levels 4 to 5, however, the noise begins to vanish from the details, and they instead begin to represent elements of the signal. By levels 7 and 8, the signal is split between the details and approximation. Manipulation of the detail coefficients, such as to remove noise, would thus be most optimal up to level 5 or 6 for this test signal.

While decomposing the signal using the DWT already affords the ability to see the noise content of a signal, the original can also be reconstructed using an inverse transform. For orthogonal wavelets, including the coiflet family, the same wavelet and scaling function can be used for signal decomposition, and subsequent reconstruction. For biorthogonal wavelets, different wavelets are used in decomposition and reconstruction. The numbers refer to the number of vanishing moments in the scaling function and determine the smoothness of the frequency response of the resulting filter bank.

In the simple case where a signal is decomposed for a given wavelet to a level j and then reconstructed using the resulting detail coefficients and jth approximation coefficients, the signal will retain all of its initial noise. In order to achieve signal denoising, it is necessary to determine which detail coefficients correspond to noise and either remove (kill) or reduce (shrink) them prior to signal reconstruction. Typically, this is handled by the selection of a threshold value. Below the threshold value, coefficients are typically shrunk or killed, while above the threshold they may be shrunk or kept. The threshold can either be selected once and used for all decomposition levels, or a new threshold can be selected at each level. Several methods for applying thresholds are given in section 3.2, and for their selection in section 3.3. When detail coefficients are manipulated in this way, their contributions will be absent in the reconstructed signal, and thus removal of all noise-related coefficients would theoretically produce a noiseless output signal.

While the DWT is a powerful tool for signal analysis, it is not translation-invariant. When used for signal denoising, jump discontinuities in the original signal can lead to oscillatory pseudo-Gibbs artifacts which contaminate the reconstructed signal (2). These artifacts are akin to the Gibbs artifacts in Fourier denoising, although reduced in amplitude (2). Jump discontinuities

occur frequently in CW EPR spectra, where they are concentrated at transitions between mobile and immobile components and in the sharp, central line. To deal with these features, complicated thresholding methods are sometimes developed, which was the case for an earlier attempt at signal denoising of primarily fast-motional CW EPR using the DWT (3).

Alternatively, one of several variants of the DWT can be employed, which introduce varying degrees of translation-invariance. This is realized by shifting the data by one point, repeating the denoising process, and then unshifting. The approach is repeated for a given number of shifts, and the results are averaged. In addition to the time domain, the shift/denoise/unshift approach can also be applied to frequency modulations. Averaging of several shifted transforms reduces or removes oscillations at the jump discontinuities and smooths the reconstructed signal, but at the cost of increased computational complexity. Balancing these two factors is achieved by picking DWT variants with a given degree of signal shifting. The simplest is the dual-tree complex wavelet transform (DTCWT), which applies the DWT twice in a dual-tree filter bank (4). If that is insufficient, the use of about 10 to 20 shifts falls under the cycle-spinning designation (2). Finally, the computation of all possible shifts results in a fully translation-invariant transform termed the stationary wavelet transform (SWT) (2). The SWT has a large hit in computation time relative to the DWT, although it has been observed to permit the use of simple thresholding functions and selection algorithms (2). The present work considers only the SWT.

3.2 Wavelet Thresholds

A variety of estimators have been proposed for use as thresholds for the detail coefficients of wavelet transformed signals. The initial, universal threshold estimator is dependent only on the length of the data n, having no dependence on the form of the data. It has the form:

 $t_{universal} = \sqrt{2log(n)}$ (3)

The universal threshold is a conservative estimator, which for most data sizes suppresses greater than 99% of all noise related coefficients (5). This comes at the cost of potentially suppressing signal coefficients, particularly in sharply varying regions such as narrow peaks. Due to this drawback, a variety of softer threshold selection methods have been developed. This work tests the heuristic Stein's unbiased risk estimate (heursure or heurSURE) and MINIMAX thresholds.

The heursure method combines the universal threshold with a second option derived from SURE (6). This allows the threshold to be softer in regions of high SNR, and more conservative in low SNR regions. The SURE threshold, t_{SURE} , is selected from a set of thresholds, t, by:

$$t_{SURE} = \min(SURE(t; x) = \min(n - 2\#\{i: |x_i| \le t\} + \sum_{i=1}^{n} (|x_i| \land t)^2) \quad (4)$$

Where n is the length of the data, # is the cardinality operator, and \land gives the minimum of two elements. Then, the criteria for threshold selection is given by the following:

$$t = \left\{ \frac{t_{universal}}{\min(t_{universal}, t_{SURE})} A < B \\ A \ge B \right\}$$
(5)

Where $A = \frac{(s-n)}{n}$ with s equal to the sum of squares of the detail coefficients and n to the length of the detail coefficients (6). The value of B is given by $(\log_2(n))^{\frac{3}{2}}\sqrt{n}$ with n again being the length of the detail coefficients. As A is dependent on the squares of the coefficients, it is small for levels that contain primarily noise with low SNR. Thus, low SNR conditions use the more conservative universal estimator. SURE and heurSURE thresholds are recomputed at each decomposition level.

Finally, several precomputed thresholds are used that are designed to adhere to MINIMAX risk minimization principles (7). These are typically provided in look-up tables as a function of the length of the data vector, but the simple case of a single threshold is often approximated as:

$$t_{minimax} = 0.3936 + 0.1829log_2(n)$$
 (6)

Where n is the length of the data vector, and $t_{minimax}$ is approximately 2.4 for the signals used here with length n=2048.

3.3 Wavelet Thresholding Methods

The simplest way to remove unwanted detail coefficients in the wavelet transformed signal is through a keep or kill rule, where coefficients below the threshold value are set equal to 0, and above the threshold value are left alone. This scheme is referred to as hard thresholding:

$$d_{jk} = \begin{cases} 0 & \text{if } |d_{jk}| < t \\ d_{jk} & \text{if } |d_{jk}| \ge t \end{cases}$$
(7)

where d_{jk} is the detail coefficient at position k and decomposition level j, and t is the threshold value. Here, hard thresholding is used with the heuristic SURE, MINIMAX, and universal estimator derived threshold values. Alternatively, a shrink or kill rule can be used, where the wavelet coefficients are set to 0 below the threshold and shrunk by the threshold value above the threshold. This is termed soft thresholding, and has the following form:

$$d_{jk} = \begin{cases} 0 & \text{if } d_{jk} \le t \\ d_{jk}\text{-}t & \text{if } d_{jk} > t \\ d_{jk} + t & \text{if } d_{jk} < \text{-}t \end{cases}$$
(8)

Soft thresholding was used only with the universal estimator for the threshold value. The choice between soft and hard thresholding is a balance between bias and variance in the denoised signal. As hard thresholding keeps values above the threshold, it tends to have better performance in signal peaks at the cost of greater variance in response to large fluctuations in the data. These fluctuations are suppressed using soft thresholding, but at the cost of reduced amplitude in the signal peaks.

A variety of methods have been created in an attempt to balance the features of both soft and hard thresholding. Two of these methods, non-negative garrote thresholding and firm thresholding, are presented here. The non-negative garrote thresholding is similar to soft thresholding, with the exception that the shrinkage decreases with the size of the coefficient (8). This is intended to increase its performance in sharp data peaks. Its form is:

$$d_{jk} = \begin{cases} 0 & \text{if } |d_{jk}| \le t \\ d_{jk} - \frac{t^2}{d_{jk}} & \text{if } |d_{jk}| > t \end{cases}$$
(9)

This method was used only with the universal estimator for the threshold value. Alternatively, firm shrinkage introduces a 3-part keep, shrink, or kill rule with 2 thresholds (9). It has the form:

$$d_{jk} = \begin{cases} 0 & \text{if } |d_{jk}| \le t_1 \\ sgn(d_{jk}) \frac{t_2(|d_{jk}| \cdot t_1)}{t_2 \cdot t_1} & \text{if } t_1 < |d_{jk}| \le t_2 \\ d_{jk} & \text{if } |d_{jk}| < \cdot t_2 \end{cases}$$
(10)

Where t_1 and t_2 are now the lower and upper threshold values, respectively. Here, the values of t_1 and t_2 were taken from a literature table for the MINIMAX condition, and had values of 2.737 and 6.939, respectively for n=2048 data points (9).

Finally, as the threshold values presented in section 3.2 are often dependent only on the size of the data, it is necessary to scale them when applying a thresholding method. This requires an estimate of the standard deviation of the noise, which can be determined in several ways. The most common in wavelet thresholding is to use a median-absolute-deviation (MAD) estimator with a scaling factor for the normal distribution of white-noise values (5). It has form:

$$\sigma = \frac{\text{MAD}}{0.6745} \quad (11)$$

where σ can be calculated level independently using just the first level detail coefficients that contain the most noise, or level dependently at each of the j decomposition levels. Here, σ was calculated level independently for each method. It was then multiplied by the threshold values prior to scale them prior to thresholding.

3.4 Description of Method

A total of six test signals were used for this analysis. The four original signals (blocks, bumps, heavisine, and doppler) were generated using the pywavelets python package, which in turn uses the code available in the proGram wavelab (10). The remaining EPR test signals were generated using the multicomponent software by Christian Altenbach, UCLA. The EPR test signals do not represent physical spectra but were selected to mimic multicomponent ensembles with smoothly varying elements that are difficult denoising targets. All analysis used the test

signals at n=2048 data points. The original signals were generated with n=2048 points, but the output of multicomponent has n=512 data points. Thus, the EPR test signals had to be upscaled to n=2048 points, which was accomplished through cubic spline interpolation. The test signals are shown in Figure 3.



Figure 3. Test Signals for Denoising. The signals are (A) blocks, (B) bumps, (C) heavisine, (D) doppler, (E) 1st EPR signal, and (F) 2nd EPR signal. Signals A-D were generated using pywavelets. Signals E and F were generated using Multicomponent.

To generate noisy signals at varying SNR ratios, the initial noise-free test signals were combined with normally distributed arrays of n=2048 points generated using the numpy software package random.normal function. Noise arrays had a mean of 0, and the variance was determined as:

variance =
$$abs(\frac{\sum_{1}^{n} signal^{2}}{SNR_{target}*n})$$
 (12)

where signal is the magnitude of the test signal at point n, and the target SNR is the desired signal-to-noise ratio. The resulting noise arrays were added to the initial data to generate noisy traces for each SNR. This was repeated for 10 trials, resulting in 40 total noisy signals for each of the six test signals. The resulting noisy signals were used for all subsequent wavelet denoising and are shown in Figure 4 for the SNR=200 and 10 cases



Figure 4. Noisy Test Signals for Denoising. The signals are (A) blocks, (B) bumps, (C) heavisine, (D) doppler, (E) 1st EPR signal, and (F) 2nd EPR signal. The lighter gray shows the noise present at SNR=10, while the darker gray shows the noise present at SNR=200. Each spectrum is a representative trace of 10 noisy spectrum generated for each signal and SNR level.

The actual average SNRs of these noisy signals are given in Table 1. There is some deviation from the target SNRs of 200, 100, 50, and 10, but the overall agreement with the targets is good. When performance metrics are presented, they represent the average of the 10 traces for a given combination of parameters.

combination of parameters.

	Signal					
Target SNR	Bumps	Blocks	Heavisine	Doppler	EPR 1	EPR 2
200	201.034	200.790	199.879	201.013	202.536	204.160
100	100.713	102.649	101.062	101.807	101.446	100.429
50	50.474	51.045	50.983	51.013	51.439	51.884
10	11.167	10.998	11.137	10.877	10.947	10.808

Table 1. The actual SNR values for the noisy test signals at target SNRs of 200, 100, 50, and 10. Each value is the average of 10 trials adding white Gaussian noise to the same initial test signal.

The general method for wavelet denoising of CW EPR spectra in the slow-motional regime involved the use of the SWT with a particular wavelet, level of decomposition, threshold value, and thresholding method. Signal deconstruction and reconstruction using the SWT were performed using the python pywavelets package. All data presented here is the top subset of a much larger parameter search. Three coiflets (coif3, coif4, coif5) and three biorthogonal wavelets (bior2.2, bior2.4, bior2.6) are featured in this analysis. Decomposition levels of 5 and 6 were determined to be most useful based on decomposition of the 1st EPR test signal in Fig. 4. The methods used for threshold determination were the universal estimator, the heuristic SURE estimator, and MINIMAX determined estimators. Thresholding methods employed were hard, soft, non-negative garrote, and firm thresholding. Threshold determination and thresholding was handled in python scripts that made use of the numpy and scipy python packages. Plotting used the matplotlib software library.

3.5 Performance of Method

To evaluate the performance of the SWT with a given combination of transform parameters, the SNR, structural similarity index (SSIM, and root-mean-square error (RMSE) were determined for each combination. The SNR in this case is defined as follows:

$$SNR = \frac{\sum_{1}^{n} (x_{denoised}(n))^{2}}{\sum_{i}^{n} (x_{denoised}(n) - x(n))^{2}}$$
(13)

where x_{denoised}(n) is the wavelet transformed signal, and x(n) is the test signal. The SNR and RMSE were computed using functions written in python. The SSIM was computed using a builtin function in the scikit-image module of scipy. The resulting performance metrics are shown in supplementary data tables 1-6. They are organized by wavelet, starting with coif3, and by increasing SNR. The data were first assessed to determine the optimal wavelet for each test signal. For the four abstract signals (blocks, bumps, heavisine, doppler), this involved finding the wavelet corresponding to the combination with the best SNR/SSIM/RMSE. Fortunately, the three parameters show the same trend at higher SNRs, and so the optimal wavelet for each signal was determined based on SNR=200. The chosen wavelets were bior2.4 for bumps and blocks, coif3 for heavisine, and coif5 for doppler. For the EPR signals, it would be more ideal to use a single wavelet for all future data, and so the wavelet was selected that gave the best average performance across both spectra. The selected wavelet for the EPR test signals was coif3. Next, the combinations of threshold selection and thresholding methods were visually analyzed for each signal and the best performing wavelet. These results are shown for decomposition level j=5 in Figures 5-10 on the following pages, and for decomposition level j=6 in Figures S1-6. The figures are arranged vertically in order of increasing SNR moving down, from SNR=10 to SNR=200. The left side shows performance across the whole spectra, while the right side shows performance of a single feature so that the better performing methods can be visually separated. The methods are color coded with the following combinations: hard thresholding with the universal estimator is blue, soft thresholding with the universal estimator is green, non-negative garrote thresholding with minimax thresholds is red, hard thresholding with the heuristic SURE thresholds is orange, hard thresholding with a minimax threshold is brown, and firm thresholding with the universal estimator is purple.

For the blocks signal (Figure 5), the best performance at the single feature level is obtained for the hard+MINIMAX combination, although this comes at the expense of additional oscillations in the flat portions of the spectrum. The next best feature performance is for the hard+universal combination, which has markedly reduced oscillation in the flat portions, and probably represents the best balance of performance. The results are similar for the Bumps signal (Figure 6), although now the firm+universal and hard+universal combinations are very similarly performant. The hard+heurSURE combination falls behind on the bumps signal, strongly underestimating peak heights compared to the other methods. The results for bumps are almost identical to those observed for the heavisine and doppler signals (Figures 7 and 8). In both bases hard+MINIMAX gives the best feature performance at the cost of not fully denoising the signal. Again, the next best performance comes from the firm+universal and hard+universal combinations, with hard+heurSURE being the least performant.



Figure 5. Performance of the SWT at level 5 across 6 different methods for the blocks test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garrote, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. At low SNR, the best performance at feature boundaries is obtained with MINIMAX+hard, but at the cost of a high degree of spurious noise in flat regions. By the SNR 100 trace, most methods catch up, with the universal+hard combination now having the best average performance across the signal.



Figure 6. Performance of the SWT at level 5 across 6 different methods for the bumps test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garrote, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. At low SNR, the best performance at feature boundaries is obtained with MINIMAX+hard, but at the cost of a high degree of spurious noise in flat regions. By the SNR 100 trace, most methods catch up, with the universal+hard and universal+firm combinations now having the best average performance across the signal.



Figure 7. Performance of the SWT at level 5 across 6 different methods for the heavisine test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garrote, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. At low SNR, the best performance at feature boundaries is obtained with MINIMAX+hard, but at the cost of a high degree of spurious noise in flat regions. By the SNR 100 trace, most methods catch up, with the universal+hard and universal+firm combinations now having the best average performance across the signal.



Figure 8. Performance of the SWT at level 5 across 6 different methods for the doppler test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garrote, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. At low SNR, the best performance at feature boundaries is obtained with MINIMAX+hard, but at the cost of a high degree of spurious noise in flat regions. By the SNR 100 trace, most methods catch up, with the universal+hard and universal+firm combinations now having the best average performance across the signal.



Figure 9. Performance of the SWT at level 5 across 6 different methods for the 1st EPR test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garrote, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. Across all SNR values, the universal+hard combination displays the best signal performance, lacking the noisy oscillations still present in the MINIMAX+hard and universal+firm conditions.



Figure 10. Performance of the SWT at level 5 across 6 different methods for the 2nd EPR test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garrote, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. Across all SNR values, the universal+hard combination displays the best signal performance, lacking the noisy oscillations still present in the MINIMAX+hard and universal+firm conditions.

The doppler signal also provides useful validation of all of the methods except for hard+heurSURE. This test signal increases in frequency from right to left. The zoomed region of Figure 8 shows the 5th oscillation from the right, which is higher in frequency and thus narrower than that expected for a free spin component in a typical CW EPR spectrum. For this oscillation, all methods except for hard+heurSURE perform well at capturing the signal features, and so it is unlikely that any tested EPR signals will exceed the frequency response of the SWT methods investigated here.

Moving to the two EPR test signals (Figures 9 and 10), it is apparent that all methods do well at decomposition level j=5 across all tested SNR values. By SNR=100, all except the hard+heurSURE combination produce an almost complete reconstruction of the test signal. The hard+MINIMAX, firm+universal, and hard+universal combinations get slightly closer to the reference signal, but the former two combinations display some residual noise left in the trace. This is true across both EPR test signals, and so the universal+hard combination appears to be the best for use with unknown CW EPR data.

Next, to confirm the conclusion from the visual comparisons and assess which level of decomposition should be selected, the three performance metrics were examined as a function of signal SNR for the EPR test signals and the coif3 wavelet. The results are shown in Figures 11 and 12. Generally, the performance at level 5 is slightly better than at level 6 when measured numerically, although the level 6 results better smooth the baseline, and so the level may be chosen on a case-by-case basis (see Figs S1-5). For both EPR test signals, the greatest performance is obtained for the hard+MINIMAX condition, although as noted above this combination was too soft and did not fully denoise the spectrum. The next best performance, as in the visual comparisons, was given by the firm+universal and hard+universal combinations. Again, the firm+universal combination retained a small degree of noise, and so the hard+universal combination holds as the best combination of numeric performance and full denoising.



Figure 11. Performance of the SWT of the 1st EPR test signal at level 5 (left) and 6 (right) as a function of SNR measured by (A) SNR, (B) SSIM, and (C) RMSE. Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garrote, heuristic SURE+hard, MINIMAX+hard, universal+firm. Overall, the level 5 results are better numerically than those obtained for level 6. The performance of the heuristic SURE+hard combination is particularly poor when measured in terms of SNR and RMSE, with the remaining methods clustering for the low SNR conditions (10 and 50). The MINIMAX+firm condition performs disproportionally well in the SNR metric at high starting SNR, but as noted in the visual comparison figures, this comes at the expense of incomplete signal denoising. This was also the case for the universal+firm threshold. The next best performing combination in all metrics was universal+hard, which was also observed visually.



Figure 12. Performance of the SWT of the 2nd EPR test signal at level 5 (left) and 6 (right) as a function of SNR measured by (A) SNR, (B) SSIM, and (C) RMSE. Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garrote, heuristic SURE+hard, MINIMAX+hard, universal+firm. Overall, the level 5 results are better numerically than those obtained for level 6. The performance of the heuristic SURE+hard combination is particularly poor when measured in terms of SNR and RMSE, with the remaining methods clustering for the low SNR conditions (10 and 50). The MINIMAX+firm condition performs disproportionally well in the SNR metric at high starting SNR, but as noted in the visual comparison figures, this comes at the expense of incomplete signal denoising. This was also the case for the universal+firm threshold. The next best performing combination in all metrics was universal+hard, which was also observed visually.
3.6 Conclusion

Overall, the results presented in this chapter demonstrate that wavelet threshold denoising is applicable to test EPR signals that represent MTSL spin labels in the slow-motion regime. The combination of hard thresholding with a universal estimator of the threshold value was found to best balance performance in terms of signal recovery with full removal of noise coefficients in the transform. Decomposition to level 5 was found to behave the best numerically for test signals with n=2048 points, but level 6 was quite close in performance and may be beneficial when more smoothing of the baseline is desired. Additionally, the coif3 wavelet was found to give very good performance for both tested EPR signals and is likely the best choice for general analysis of EPR signals of this type. This wavelet was also determined to be the optimal choice in an earlier analysis of EPR spectra in the fast-motional regime using the DWT and a custom thresholding function (3). For the remaining chapters of this work, the noisy spectra are presented as an overlay with a denoised signal representing the SWT transform with the coif3 wavelet at level 5 or 6 with hard thresholding and the universal estimator.

3.7 References

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Figure S1. Performance of the SWT at level 6 across 6 different methods for the blocks test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garotte, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. At low SNR, the best performance at feature boundaries is still obtained with MINIMAX+hard at the expense of incomplete denoising, and universal+hard still provides the best balance. Compared to level 5, the level 6 result stays flatter in broad regions, but tends to induce curvature in more narrow regions.



Figure S2. Performance of the SWT at level 6 across 6 different methods for the bumps test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garotte, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. At low SNR, the best performance at feature boundaries is still obtained with MINIMAX+hard at the expense of incomplete denoising, and universal+hard still provides the best balance. Compared to level 5, the level 6 result excellently captures the baseline, but all methods fail to capture the signal peaks.



Figure S3. Performance of the SWT at level 6 across 6 different methods for the heavisine test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garotte, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. At low SNR, the best performance at feature boundaries is still obtained with MINIMAX+hard at the expense of incomplete denoising, and universal+hard still provides the best balance. For this low frequency signal, the level 6 transform provides a generally smoother fit through the data with better visual agreement.



Figure S4. Performance of the SWT at level 6 across 6 different methods for the heavisine test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garotte, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. At low SNR, the best performance at feature boundaries is still obtained with MINIMAX+hard at the expense of incomplete denoising, and universal+hard still provides the best balance. Even at level 6, most methods still capture the 5th oscillation (right side), but heuristic SURE+hard undershoots it completely.



Figure S5. Performance of the SWT at level 6 across 6 different methods for the 1st EPR test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garotte, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. Across all SNR values, the universal+hard combination displays the best signal performance. At level 6, the baseline is almost oscillation free, although this comes at the expense of a small amount of undershoot in the right, highfield line.



Figure S6. Performance of the SWT at level 6 across 6 different methods for the 2nd EPR test signal at SNR of 10 (A), 50 (B), 100 (C) or 200 (D). Methods are color coded as follows (threshold selection + method): universal+hard, universal+soft, universal+garotte, heuristic SURE+hard, MINIMAX+hard, universal+firm. The left panel shows whole trace performance while the right shows a zoomed region indicated by a black arrow. Across all SNR values, the universal+hard combination displays the best signal performance. At level 6, the baseline is almost oscillation free, although this comes at the expense of a small amount of undershoot in the left, lowfield line.

												Sig	inal								
	COIF3	SNR=10		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	d Selection	Leve	ISNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	39.2904	0.7457	0.3876	38.2562	0.7335	0.1128	251.7343	0.9514	0.1953	126.2126	0.9205	0.0263	200.8590	0.9169	0.0002	209.3502	0.9134	0.0002
			6	17.3107	0.7162	0.5657	9.8761	0.6725	0.2054	292.5546	0.9508	0.1813	119.3653	0.9233	0.0268	186.7972	0.9361	0.0002	226.9048	0.9411	0.0002
	Soft	Universal	5	26.0395	0.7154	0.4708	7.0448	0.6219	0.2357	249.0657	0.9525	0.1964	51.2226	0.8888	0.0403	171.3662	0.9171	0.0002	172.6110	0.9122	0.0003
			6	10.9310	0.6824	0.6984	2.3331	0.5050	0.3628	260.7873	0.9498	0.1914	36.0471	0.8821	0.0472	68.0115	0.9246	0.0003	92.6128	0.9281	0.0004
	Garotte	Universal	5	12 25 70	0.7212	0.4548	13.3578	0.6779	0.1792	249.3753	0.9525	0.1963	74.9511	0.9041	0.0336	187.1382	0.9168	0.0002	195.4268	0.9124	0.0002
SW			5	50 9655	0.0917	0.0590	6.0418	0.50/1	0.3073	207.1040	0.9501	0.1092	21 4232	0.9059	0.0501	129.45502	0.9510	0.0002	107 5135	0.9500	0.0003
	Hard	Heur. SUR	E	52 3782	0.7000	0.3344	4 7302	0.5517	0.2759	305 7495	0.9520	0.1775	8 8285	0.0422	0.0922	94271	0.9178	0.0002	6 8258	0.8687	0.0012
			5	78,4501	0.7784	0.2779	75.7177	0.7679	0.0820	135.7663	0.8576	0.2807	145.2872	0.9000	0.0247	137.8284	0.8913	0.0002	132.2939	0.8846	0.0003
	Hard	MINIMAX	6	28.4495	0.7538	0.4492	31.7795	0.7529	0.1226	185.7297	0.8680	0.2530	195.1075	0.9302	0.0211	208.0117	0.9388	0.0002	252.6938	0.9421	0.0002
			5	39.8081	0.7462	0.3841	34.2403	0.7346	0.1180	255.0305	0.9481	0.1944	123.2121	0.9188	0.0265	198.9044	0.9162	0.0002	210.1505	0.9122	0.0002
	Firm	MINIMAX	6	17.2309	0.7162	0.5657	8.9518	0.6695	0.2123	300.1422	0.9465	0.1790	120.0135	0.9229	0.0267	154.2569	0.9398	0.0002	227.7062	0.9411	0.0002
				:								Sig	Inal								
	COIF3	SNR=50		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	d Selection	Leve	ISNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	117.6766	0.8614	0.2260	132.3755	0.8706	0.0621	967.0361	0.9776	0.0998	654.3880	0.9733	0.0115	496.9912	0.9744	0.0001	484.4573	0.9748	0.0002
	mara	onnoroan	6	21.0114	0.7738	0.5177	14.0210	0.7515	0.1754	1106.2114	0.9793	0.0940	644.5249	0.9750	0.0116	398.5812	0.9744	0.0001	437.2156	0.9812	0.0002
	Soft	Universal	5	43.1152	0.8104	0.3682	17.3518	0.7874	0.1572	672.8937	0.9721	0.1194	169.8575	0.9515	0.0224	411.2515	0.9739	0.0001	421.0379	0.9744	0.0002
			6	12.0844	0.7195	0.6679	2.7190	0.5685	0.3391	549.0000	0.9675	0.1322	118.3611	0.9460	0.0266	152.7073	0.9645	0.0002	230.9166	0.9745	0.0002
	Garotte	Universal	5	58.7037	0.8308	0.3171	46.1187	0.8406	0.1016	750.6759	0.9745	0.1132	360.3592	0.9647	0.0155	469.3934	0.9741	0.0001	456.4432	0.9746	0.0002
SW			6	14.2290	0.7312	0.6190	4.5185	0.6366	0.2776	700.2866	0.9719	0.1177	293.9365	0.9629	0.0172	290.0510	0.9694	0.0001	379.2423	0.9795	0.0002
	Hard	Heur. SUR	E ⁵	59.9384	0.8346	0.3138	6.2061	0.6709	0.2520	564.8370	0.9677	0.1301	22.7118	0.8636	0.0598	174.2614	0.9726	0.0002	148.4155	0.9726	0.0003
			6	58.5596	0.8414	0.3163	4.8149	0.6414	0.2731	495.5619	0.9665	0.1394	8.9327	0.7930	0.0918	9.5827	0.9169	0.0007	6.9394	0.9134	0.0012
	Hard	MINIMAX	5	285.0594	0.8784	0.1459	267.4548	0.8961	0.0440	656.8990	0.9395	0.1243	700.6193	0.9634	0.0113	515.2282	0.9706	0.0001	468.2160	0.96/0	0.0002
			5	30.3090	0.81/6	0.3895	47.2000	0.8264	0.1011	052.0107	0.9643	0.0969	646 0729	0.9759	0.0098	407.0101	0.9792	0.0001	250 1519	0.9830	0.0002
	Firm	MINIMAX	6	20 0722	0.6010	0.2290	127.9073	0.8/00	0.0030	1081 2067	0.9766	0.1000	610 2778	0.9735	0.0110	305 6048	0.9741	0.0001	148 4630	0.9744	0.0002
			0	20.5122	0.7094	0.5175	12.2000	0.7430	0.1041	1001.2007	0.9765	0.0343	013.2770	0.9/4/	0.0115	333.0040	0.5744	0.0001	440.4035	0.9617	0.0002
												Sic	Inal								
(OIF3	SNR=100	F	Blocks			Bumps			Heavisine		Sig	inal Doppler			Epr 1			Epr 2		
0	OIF3 S	SNR=100 Selection	E Level S	Blocks	SSIM	RMSE	Bumps SNR	SSIM	RMSE	Heavisine SNR	SSIM	Siç RMSE	ınal Doppler SNR	SSIM	RMSE	Epr 1 SNR	SSIM	RMSE	Epr 2 SNR	SSIN	I RMSE
	OIF3	SNR=100 Selection	E Level S 5 2	Blocks BNR 220.3258	SSIM 0.9077	RMSE 0.1674	Bumps SNR 213.6559	SSIM 0.9082	RMSE 0.0491	Heavisine SNR 2022.6848	SSIM 0.9887	Sig RMSE 0.0694	nal Doppler SNR 1445.0967	SSIM 0.9866	RMSE	Epr 1 SNR 668.1910	SSIM 0.983	RMSE	Epr 2 SNR 775.6943	SSIN 3 0.98	1 RMSE 44 0.0001
1 	COIF3 S Nethod S lard U	SNR=100 Selection Universal	E Level S 5 2 6 2	Blocks BNR 220.3258 20.8872	SSIM 0.9077 0.7849	RMSE 0.1674 0.5179	Bumps SNR 213.6559 13.2258	SSIM 0.9082 0.7620	RMSE 0.0491 0.1792	Heavisine SNR 2022.6848 2128.1522	SSIM 0.9887 0.9893	Sig RMSE 0.0694 0.0675	nal Doppler SNR 1445.0967 1339.6524	SSIM 0.9866 0.9859	RMSE 0.0077 0.0081	Epr 1 SNR 668.1910 513.2964	SSIM 0.983 0.983	RMSE 5 0.0001 3 0.0001	Epr 2 SNR 775.6943 522.1809	SSIN 3 0.98 9 0.98	 RMSE 44 0.0001 67 0.0002
(COIF3 S Iethod S lard U	SNR=100 Selection Universal	Eevel 5 5 2 5 5 5 5	Blocks SNR 220.3258 20.8872 57.4016	SSIM 0.9077 0.7849 0.8569	RMSE 0.1674 0.5179 0.3200	Bumps SNR 213.6559 13.2258 24.4045	SSIM 0.9082 0.7620 0.8422	RMSE 0.0491 0.1792 0.1347	Heavisine SNR 2022.6848 2128.1522 1072.3945	SSIM 0.9887 0.9893 0.9818	Sig <u>RMSE</u> 0.0694 0.0675 0.0944	nal Doppler SNR 1445.0967 1339.6524 316.0377	SSIM 0.9866 0.9859 0.9709	RMSE 0.0077 0.0081 0.0164	Epr 1 SNR 668.1910 513.2964 545.6898	SSIM 0.983 0.983 0.983	RMSE 5 0.0001 3 0.0001 1 0.0001	Epr 2 SNR 775.6943 522.1809 552.0390	SSIN 3 0.98 9 0.98 0 0.98	RMSE 44 0.0001 67 0.0002 37 0.0001
1 	COIF3 S Iethod S lard L	SNR=100 Selection Universal Universal	E Level S 5 2 6 2 5 5 6 1	Blocks SNR 220.3258 20.8872 57.4016 11.9577	SSIM 0.9077 0.7849 0.8569 0.7271	RMSE 0.1674 0.5179 0.3200 0.6702	Bumps SNR 213.6559 13.2258 24.4045 2.6288	SSIM 0.9082 0.7620 0.8422 0.5796	RMSE 0.0491 0.1792 0.1347 0.3433	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356	SSIM 0.9887 0.9893 0.9818 0.9741	Sig RMSE 0.0694 0.0675 0.0944 0.1096	nal Doppler SNR 1445.0967 1339.6524 316.0377 205.8504	SSIM 0.9866 0.9859 0.9709 0.9656	RMSE 0.0077 0.0081 0.0164 0.0202	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126	SSIM 0.983 0.983 0.983 0.974	RMSE 5 0.0001 3 0.0001 1 0.0001 3 0.0002	Epr 2 SNR 775.6943 522.1809 552.0390 313.037	SSIN 3 0.98 9 0.98 0 0.98 1 0.98	RMSE 44 0.0001 67 0.0002 37 0.0001 15 0.0002
	COIF3 S lethod S lard L soft L Sarotte L	SNR=100 Selection Jniversal Jniversal	E Level S 5 2 5 5 5 5 6 1 5 8	Blocks SNR 220.3258 20.8872 57.4016 11.9577 39.7255	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853	Sig 0.0694 0.0675 0.0944 0.1096 0.0839	nal Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694	SSIM 0.983 0.983 0.983 0.974 0.983	RMSE 5 0.0001 3 0.0001 1 0.0001 3 0.0002 3 0.0002	Epr 2 SNR 775.6943 522.1809 552.0390 2 313.037 627.2660	SSIM 3 0.98 9 0.98 0 0.98 1 0.98 0 0.98	RMSE 44 0.0001 67 0.0002 37 0.0001 15 0.0002 40 0.0001
H SWT	COIF3 S lethod S lard L Goft L Garotte L	SNR=100 Selection Jniversal Jniversal Jniversal	Eevel 5 5 2 5 5 5 5 5 6 1 5 8 6 1	Blocks SNR 220.3258 20.8872 57.4016 11.9577 39.7255 14.0322	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853 0.9822	Sig RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907	nal Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573	SSIM 0.983 0.983 0.983 0.974 0.983 0.979	RMSE 5 0.0001 3 0.0001 1 0.0001 3 0.0002 3 0.0001 3 0.0001 3 0.0001 3 0.0001	Epr 2 SNR 775.6943 522.1809 552.0390 2 313.037 627.2660 470.3285	ssiw 3 0.98 3 0.98 3 0.98 3 0.98 3 0.98 3 0.98 3 0.98 3 0.98 3 0.98 3 0.98 3 0.98	RMSE 44 0.0001 67 0.0002 37 0.0001 15 0.0002 40 0.0001 52 0.0002
swT	COIF3 S lethod S lard L Goft L Garotte L	SNR=100 Selection Jniversal Jniversal Jniversal Heur. SURE	Level 5 5 2 5 5 5 6 1 5 8 6 1 5 8 6 1 5 6	Blocks SNR 220.3258 20.8872 57.4016 11.9577 39.7255 14.0322 50.8600	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386 0.8662	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942 6.1961	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853 0.9822 0.9728	Sig RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191	mal Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973	SSIM 0.983 0.983 0.983 0.974 0.983 0.979 0.981	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 775.6943 522.1809 552.0390 2 313.037 627.2660 470.3288 2 153.033	SSIM 3 0.98 9 0.98 0 0.98 1 0.98 0 0.98 5 0.98 5 0.98	RMSE 44 0.0001 67 0.0002 37 0.0001 15 0.0002 40 0.0001 52 0.0002 13 0.0003
swt	COIF3 5 Iethod 5 lard 1 Soft 1 Sarotte 1 lard H	SNR=100 Selection Jniversal Jniversal Jniversal Heur. SURE	Eevel 5 5 2 5 5 5 6 1 5 8 6 1 5 8 6 1 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6	Blocks SNR 220.3258 20.8872 57.4016 11.9577 39.7255 14.0322 50.8600 59.0785	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386 0.8662 0.8551	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3144	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942 6.1961 4.7928	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031 0.6553	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.2732	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 545.4891	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853 0.9822 0.9728 0.9728 0.9696	Sig RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191 0.1323	mal Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679 0.7955	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598 0.0917	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011	SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923	RMSE 0.0001 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002	Epr 2 SNR 775.6943 522.1809 552.0390 2 313.037 627.2660 470.3285 2 153.0335 7 6.9417	SSIM 3 0.98 9 0.98 1 0.98 2 0.98 3 0.98 4 0.98 5 0.98 5 0.98 6 0.98 7 0.98 8 0.98 9<	RMSE 44 0.0001 67 0.0002 37 0.0001 15 0.0002 40 0.0001 52 0.0002 13 0.0003 81 0.0012
r F SWT F	COIF3 S Iethod S Iard L Goft L Garotte L Iard H	SNR=100 Selection Jniversal Jniversal Jniversal Heur. SURE	Level 5 5 2 5 5 2 5 5 5 6 1 5 6 1 5 6 1 5 6 5 6 5 6 5 6 5 6	Blocks SNR 220.3258 20.8872 57.4016 11.9577 39.7255 14.0322 50.8600 59.0785 522.9315 52.9315	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386 0.8662 0.8662 0.8551 0.9188	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3144 0.0998	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942 6.1961 4.7928 428.1358	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031 0.6553 0.9377	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.2732 0.0349	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 545.4891 1353.1443	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853 0.9822 0.9728 0.9696 0.9635	Sig RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191 0.1323 0.0861 0.0861	nal Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476 1472.334	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679 0.7955 0.9809	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598 0.0917 0.0078	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543	SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923 0.982	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 775.6943 522.1809 552.0390 2313.037' 627.2660 470.3283 2153.0333 6.9417 775.5821	SSIM 3 0.98 9 0.98 1 0.98 1 0.98 5 0.98 5 0.98 5 0.98 5 0.98 5 0.91 7 0.97 7 0.97	RMSE 44 0.0001 67 0.0002 37 0.0001 50 0.0002 40 0.0001 52 0.0002 33 0.0003 34 0.0012 38 0.0012
F SWT F	COIF3 S Iethod S Iard L Goft L Garotte L Iard H	SNR=100 Selection Universal Universal Jniversal Heur. SURE MINIMAX	Level 5 5 2 6 2 5 5 5 6 1 5 6 6 1 5 6 6 1 5 6 6 5 5 6 6 5 5 6 6 3 5 6 6 3 5 5 5 6 6 3 5 5 5 6 6 3 5 5 6 5 6 5 6 5 6 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7	Blocks SNR 220.3258 20.8872 57.4016 11.9577 39.7255 4.0322 50.8600 59.0785 522.9315 88.1791 14.084	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386 0.8662 0.8662 0.8551 0.9188 0.8305	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3144 0.0998 0.3889 0.3889	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942 6.1961 4.7928 428.1358 45.2654	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031 0.6553 0.9377 0.8368 0.9311	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.2732 0.0349 0.1029 0.0507	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 545.4891 1353.1443 2448.0742 2045.0712	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853 0.9822 0.9728 0.9696 0.9635 0.9816	Sig RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191 0.1323 0.0861 0.0647 0.0647	mail Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476 1472.3381 2013.1140	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679 0.7955 0.9809 0.9889 0.9889	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598 0.0917 0.0078 0.0066 0.0078	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543 620.1223 501.2025	SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923 0.982 0.982	RMSE 5 0.0001 3 0.0001 3 0.0002 3 0.0001 3 0.0001 3 0.0001 3 0.0001 0 0.0001 0 0.0001 0 0.0001 1 0.0001 5 0.0001	Epr 2 SNR 775.6943 522.1805 552.0396 2313.037 627.2666 470.3288 153.0338 6.9417 775.5827 762.3302 489.048	SSIM 3 0.98 9 0.98 0 0.98 1 0.98 5 0.98 5 0.98 5 0.98 6 0.98 7 0.97 2 0.98	RMSE 44 0.0001 67 0.0002 37 0.0011 15 0.002 40 0.0011 52 0.002 13 0.003 81 0.0012 88 0.0011 79 0.0001
r r swt r r r r	COIF3 S Nethod S lard U soft U Sarotte U lard H lard N	SNR=100 Selection Jniversal Jniversal Heur. SURE VIINIMAX	Level 5 5 2 5 5 5 6 1 5 6 1 5 6 1 5 6 1 5 6 5 5 6 5 6 3 5 6 4 1 5 6 5 6 4 1 5 6 5 6 1 5 6 5 6 1 5 6 5 6 1 5 6 6 1 5 6 6 1 5 6 5 6 1 5 6 6 10 10 10 10 10 10 10 10 10 10 10 10 10	Blocks SNR 220.3258 20.8872 39.7255 44.0322 50.8600 59.0785 522.9315 38.1791 211.0884 po.6297	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386 0.8662 0.8662 0.8551 0.9188 0.8305 0.9188 0.9087 0.9087	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3144 0.0998 0.3889 0.1705	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942 6.1961 4.7928 428.1358 45.2654 200.6697 11.5210	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031 0.6553 0.9377 0.8368 0.9115 0.9756	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.2732 0.0349 0.1029 0.0507 0.4822	Heavisine SNR 2022.6848 2128.1522 1072.3945 1365.8412 1175.0474 670.1873 545.4891 1353.1443 2448.0742 2015.0713 2146.5720	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853 0.9822 0.9728 0.9696 0.9635 0.9816 0.9885 0.9885	Sig RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191 0.1323 0.0861 0.0647 0.0692 0.092	mail Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476 1472.3381 2013.1140 1445.7176 1425.0726	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679 0.7955 0.9809 0.9889 0.9889	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598 0.0917 0.0078 0.0066 0.0077	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543 620.1223 501.3063	SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923 0.982 0.986 0.983	RMSE 0.0001	Epr 2 SNR 775.6943 522.1809 552.0390 2 313.037 627.2660 470.3288 153.0338 6.9417 775.5821 762.3302 488.0483 EFE 14.6	SSIM 3 0.98 9 0.98 1 0.98 5 0.98 5 0.98 6 0.98 7 0.97 2 0.98 3 0.98	RMSE 44 0.0001 67 0.0002 37 0.0011 15 0.002 40 0.0011 52 0.002 13 0.003 81 0.0012 88 0.0001 79 0.0002 60 0.0002
SWT F	COIF3 S lethod S lard U soft U Sarotte U lard H lard M	SNR=100 Selection Jniversal Jniversal Jniversal Heur, SURE VINIMAX	Level 5 2 5 2 5 5 5 5 6 1 5 6 1 5 6 1 5 6 5 5 6 5 6 3 5 6 6 3 5 2 6 3 5 2 6 3 5 2 6 3 5 4 6 3 5 4 6 3 5 4 5 4 5 5 6 5 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	Blocks SNR 220.3258 20.8872 37.4016 11.9577 39.7255 14.0322 50.8600 59.0785 522.9315 38.1791 211.0884 20.6287	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386 0.8662 0.8651 0.84551 0.8305 0.8305 0.9087 0.7760	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3108 0.3144 0.0998 0.3889 0.1705 0.5201	Bumps SNR 213.6559 13.2258 2.44.045 2.6288 73.2369 4.2942 6.1961 4.7928 428.1358 45.2654 200.6697 11.5819	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031 0.6553 0.9377 0.8368 0.9115 0.7553	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.2732 0.0349 0.1029 0.0507 0.1882	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 645.4881 1353.1443 2448.0742 2015.0713 2106.5750	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853 0.9822 0.9728 0.9696 0.9635 0.9816 0.9885 0.9893	Sig RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191 0.1323 0.0861 0.0647 0.0692 0.0678	nal Doppler <u>SNR</u> 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476 1472.3381 2013.1140 1445.5.9751	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679 0.7955 0.9809 0.9889 0.9866 0.9863	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598 0.0917 0.0078 0.0066 0.0077 0.0080	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543 620.1223 501.3063 515.3938	SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923 0.982 0.986 0.983 0.983	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 775.6943 522.1809 552.0390 2313.037 627.2666 470.3288 2153.0338 6.9417 775.5821 762.3302 488.0483 558.1464	SSIM 3 0.98 9 0.98 1 0.98 1 0.98 1 0.98 5 0.98 5 0.98 6 0.98 7 0.97 2 0.98 3 0.98 4 0.98	RMSE 44 0.0001 67 0.0002 37 0.0001 50 0.0002 40 0.0001 52 0.0002 13 0.0003 14 0.0012 15 0.0002 16 0.0001 17 0.0001 18 0.0001 19 0.0002 10 0.0002 10 0.0002
F SWT F	COIF3 5 1ethod 5 1ard 1 5arotte 1 1ard 4 1ard 1 1ard 1 1	SNR=100 Selection Jniversal Jniversal Jniversal Heur. SURE MINIMAX	Level S 5 2 5 2 5 5 6 1 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 6 2	Blocks SNR 220.3258 20.8872 57.4016 11.9577 19.7255 14.0322 50.8600 90.0785 5322.9315 588.1791 211.0884 20.6287	SSIM 0.9077 0.7849 0.8569 0.7271 0.8869 0.7386 0.8662 0.8662 0.8551 0.8662 0.8551 0.8662 0.8551 0.8662 0.8551 0.8662 0.8551 0.8662 0.9188 0.9087 0.7760	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3104 0.33144 0.0998 0.3889 0.1705 0.5201	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942 6.1961 4.7928 428.1358 45.2654 200.6697 11.5819 Bumps	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031 0.6553 0.8368 0.9115 0.7553	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.2732 0.0349 0.1029 0.0507 0.1882	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 545.4891 1353.1443 2448.0742 2015.0713 2106.5750	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853 0.9822 0.9728 0.9696 0.9635 0.9816 0.9885 0.9893	Sig RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191 0.1323 0.0861 0.0647 0.0692 0.0678 Sig	nal Dopper SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8,9476 1472.3381 2013.1140 1445.7176 1355.9751 mal	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679 0.7955 0.9809 0.9889 0.9866 0.9863	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598 0.0917 0.0078 0.0066 0.0077 0.0080	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543 620.1223 501.3063 515.3938	SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923 0.982 0.986 0.983 0.983	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 775.6943 552.3809 552.3900 313.037' 627.2660 470.3288 153.0338 6.9417 775.5823 762.3302 488.0483 558.1464	SSIM 3 0.98 9 0.98 1 0.98 1 0.98 5 0.98 5 0.98 6 0.98 7 0.977 2 0.98 3 0.98 4 0.984	I RMSE 44 0.0001 67 0.0002 37 0.0001 50 0.0002 40 0.0001 52 0.0002 13 0.0003 14 0.0012 15 0.0001 16 0.0001 17 0.0001 18 0.0001 19 0.0002 10 0.0002 10 0.0001
SWT F	COIF3 5 1ethod 5 1ard 1 1ard 1 1 1 1 1 1 1 1 1 1 1 1 1 1	SNR=100 Selection Jniversal Jniversal Heur. SURE MINIMAX MINIMAX SNR=200 Selection	Level S 5 2 5 2 5 5 6 1 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 6 2 6 2 6 2 6 2 6 2 6 2 6 2 6 2 6 2 6 2 6 2 7 2 8 2	Blocks SNR 220.3258 20.8872 57.4016 11.9577 19.7255 14.0322 50.8600 50.0785 522.9315 38.1791 211.0884 20.6287 Blocks SNR	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386 0.7386 0.8662 0.8551 0.9188 0.8305 0.9087 0.9087 0.77760 0.8305	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3104 0.0998 0.33144 0.0998 0.3344 0.03889 0.1705 0.5201	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942 6.1961 4.7928 42.7928 42.7358 45.2654 200.6697 11.5819 Bumps	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6453 0.7031 0.6553 0.9377 0.8368 0.9115 0.7553	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.2732 0.0349 0.1029 0.0507 0.1882 RMSE	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 545.4891 1353.1443 2448.0742 2015.0713 2106.5750 Heavisine	SSIM 0.9887 0.9893 0.9818 0.9741 0.9853 0.9822 0.9728 0.9696 0.9696 0.9865 0.9885 0.9893	RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191 0.1323 0.0861 0.0647 0.0692 0.0678 Sig	nal Dopper SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476 1472.3381 2013.1140 1445.7176 1355.9751 nal Dopper SNP	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679 0.7955 0.9809 0.9889 0.9866 0.9863	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598 0.0917 0.0078 0.0066 0.0077 0.0080	Epr 1 SNR 6668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543 602.1223 501.3063 515.3938 Epr 1 SNP	SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923 0.982 0.986 0.983 0.983	RMSE 0.0001	Epr 2 SNR 775.6943 522.1800 552.0390 2313.037 627.2666 470.3288 153.0338 6.9417 775.5821 762.3302 488.0483 558.1464 Epr 2 SNR	SSIM 3 0.98 4 0.98 5 0.98 6 0.98 7 0.97 2 0.98 3 0.98 4 0.98 5 0.98 6 0.98 7 0.97 2 0.98 4 0.98	RMSE 44 0.0012 37 0.0021 37 0.0011 15 0.0022 40 0.0011 52 0.0021 30 0.0012 38 0.0011 39 0.0012 38 0.0011 39 0.0001 40 0.0002 68 0.0001 40 0.0002
SWT F F F	COIF3 S Iethod S Iard L Soft L Sarotte L Iard H Iard H Iard M Soft L Soft L Iard M Iard M Soft L Iard M Iard M Soft S Iard M Iard <td>SNR=100 Selection Jniversal Jniversal Heur. SURE VIINIMAX VIINIMAX SNR=200 Selection</td> <td>Level 5 5 2 5 5 5 6 1 5 5 6 6 1 5 6 6 5 5 6 6 2 5 5 6 2 5 5 5 5 6 2 5 5 6 2 5 5 6 2 5 5 5 5 6 2 5 5 5 5 6 2 5 5 6 2 2 2 5 5 5 5 6 2 2 2 5 5 5 5 6 2 2 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5</td> <td>Blocks SNR 220.3258 20.8872 57.4016 11.9577 39.7255 50.8600 59.0785 522.9315 88.1791 211.0884 20.6287 Blocks SNR 15.59799</td> <td>SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386 0.8662 0.8551 0.8662 0.8551 0.9188 0.3087 0.7760 SSIM 0.9231</td> <td>RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3104 0.0998 0.33144 0.0998 0.3344 0.03889 0.1705 0.5201 RMSE</td> <td>Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942 6.1961 4.7928 428.1358 45.2654 200.6697 11.5819 Bumps SNR 292.3541</td> <td>SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031 0.6553 0.9377 0.8368 0.9115 0.7553 SSIM</td> <td>RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.2732 0.0349 0.1029 0.0507 0.1882 RMSE 0.0421</td> <td>Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 545.4891 1353.1443 2015.0713 2015.0713 2015.0713 2015.0713 2015.0713 3016.5750 Heavisine SNR</td> <td>SSIM 0.9887 0.9893 0.9741 0.9853 0.9822 0.9728 0.9696 0.9635 0.9816 0.9885 0.9893 SSIM 0.9935</td> <td>RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191 0.1323 0.0861 0.0647 0.0692 0.0678 Sig RMSE 0.0494</td> <td>nal Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476 1472.3381 2013.1140 1445.7176 1355.9751 mal Doppler SNR</td> <td>SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679 0.9889 0.9889 0.9866 0.9863 SSIM</td> <td>RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598 0.0917 0.0078 0.0066 0.0077 0.0080 RMSE</td> <td>Epr 1 SNR 6668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543 620.1223 501.3063 515.3938 Epr 1 SNR 967.6530</td> <td>SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923 0.982 0.986 0.983 0.983 SSIM</td> <td>RMSE 0.0001 RMSE 7</td> <td>Epr 2 SNR 775.6943 522.1806 522.1806 522.0390 2 313.037 627.2666 470.3288 2 153.0338 6.9417 775.5827 762.3300 488.0483 558.1464 Epr 2 SNR 1223.800</td> <td>SSIM 3 0.98 0 0.98 0 0.98 1 0.98 0 0.98 0 0.98 0 0.98 0 0.98 0 0.98 5 0.98 0 0.913 7 0.973 2 0.98 3 0.98 4 0.98 SSIN 32</td> <td>RMSE 44 0.001 67 0.002 15 0.002 15 0.002 15 0.002 13 0.0012 13 0.0013 14 0.0014 15 0.002 16 0.0012 17 0.0014 18 0.0011 140 0.0002 168 0.0001 140 0.0002 158 0.0001 140 0.0002 141 0.0002 142 0.0001</td>	SNR=100 Selection Jniversal Jniversal Heur. SURE VIINIMAX VIINIMAX SNR=200 Selection	Level 5 5 2 5 5 5 6 1 5 5 6 6 1 5 6 6 5 5 6 6 2 5 5 6 2 5 5 5 5 6 2 5 5 6 2 5 5 6 2 5 5 5 5 6 2 5 5 5 5 6 2 5 5 6 2 2 2 5 5 5 5 6 2 2 2 5 5 5 5 6 2 2 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	Blocks SNR 220.3258 20.8872 57.4016 11.9577 39.7255 50.8600 59.0785 522.9315 88.1791 211.0884 20.6287 Blocks SNR 15.59799	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.7386 0.8662 0.8551 0.8662 0.8551 0.9188 0.3087 0.7760 SSIM 0.9231	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3104 0.0998 0.33144 0.0998 0.3344 0.03889 0.1705 0.5201 RMSE	Bumps SNR 213.6559 13.2258 24.4045 2.6288 73.2369 4.2942 6.1961 4.7928 428.1358 45.2654 200.6697 11.5819 Bumps SNR 292.3541	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031 0.6553 0.9377 0.8368 0.9115 0.7553 SSIM	RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.2732 0.0349 0.1029 0.0507 0.1882 RMSE 0.0421	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 545.4891 1353.1443 2015.0713 2015.0713 2015.0713 2015.0713 2015.0713 3016.5750 Heavisine SNR	SSIM 0.9887 0.9893 0.9741 0.9853 0.9822 0.9728 0.9696 0.9635 0.9816 0.9885 0.9893 SSIM 0.9935	RMSE 0.0694 0.0675 0.0944 0.1096 0.0839 0.0907 0.1191 0.1323 0.0861 0.0647 0.0692 0.0678 Sig RMSE 0.0494	nal Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476 1472.3381 2013.1140 1445.7176 1355.9751 mal Doppler SNR	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.8679 0.9889 0.9889 0.9866 0.9863 SSIM	RMSE 0.0077 0.0081 0.0164 0.0202 0.0105 0.0119 0.0598 0.0917 0.0078 0.0066 0.0077 0.0080 RMSE	Epr 1 SNR 6668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543 620.1223 501.3063 515.3938 Epr 1 SNR 967.6530	SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923 0.982 0.986 0.983 0.983 SSIM	RMSE 0.0001 RMSE 7	Epr 2 SNR 775.6943 522.1806 522.1806 522.0390 2 313.037 627.2666 470.3288 2 153.0338 6.9417 775.5827 762.3300 488.0483 558.1464 Epr 2 SNR 1223.800	SSIM 3 0.98 0 0.98 0 0.98 1 0.98 0 0.98 0 0.98 0 0.98 0 0.98 0 0.98 5 0.98 0 0.913 7 0.973 2 0.98 3 0.98 4 0.98 SSIN 32	RMSE 44 0.001 67 0.002 15 0.002 15 0.002 15 0.002 13 0.0012 13 0.0013 14 0.0014 15 0.002 16 0.0012 17 0.0014 18 0.0011 140 0.0002 168 0.0001 140 0.0002 158 0.0001 140 0.0002 141 0.0002 142 0.0001
0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	COIF3 S Iethod S Iard L Sarotte L Iard H Iard L Iard L	SNR=100 Selection Jniversal Jniversal Heur. SURE VINIMAX VINIMAX SNR=200 Selection Jniversal	Level S 5 2 5 2 5 5 6 1 5 5 6 1 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 2 2 5 6 2 5 5 6 2 5 5 6	Blocks SNR 220.3258 20.8872 37.4016 11.9577 39.7255 30.8600 39.0785 322.9315 38.1791 211.0884 00.6287 SNR 135.9799 11.3155	SSIM 0.9077 0.7849 0.8569 0.7271 0.8809 0.3865 0.8651 0.9188 0.9188 0.9188 0.9188 0.9188 0.9188 0.9188 0.9188 0.9188 0.9188 0.9188 0.9188 0.91 0.918 0.91 0.91 0.91 0.91 0.91 0.91 0.91 0.91	RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3108 0.3144 0.0998 0.3144 0.0998 0.3889 0.1705 0.5201 RMSE 0.1187 0.5138	Bumps SNR 213.6559 13.2258 24.4045 2.6288 7.32369 4.2942 6.1961 4.7928 428.1358 45.2654 200.6697 11.5819 Bumps SNR 292.3541 14.2678	SSIM 0.9082 0.7620 0.8422 0.5796 0.8864 0.6463 0.7031 0.6553 0.9377 0.8368 0.9115 0.7553 SSIM 0.9291 0.7706	RMSE 0.0491 0.1792 0.3433 0.0819 0.2828 0.2517 0.2732 0.0349 0.1029 0.0507 0.1882 RMSE 0.0421 0.1738	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 545.4891 1353.1443 2015.0713 2016.5750 Heavisine SNR 3965.4110 4006.7168	SSIM 0.9887 0.9893 0.9741 0.9853 0.9822 0.9728 0.9696 0.9635 0.9816 0.9885 0.9893 SSIM 0.9935 0.9931	Sig RMSE 0.0694 0.0675 0.0944 0.0675 0.0907 0.1191 0.0839 0.0907 0.1191 0.1323 0.0861 0.0647 0.0692 0.0678 Sig RMSE 0.0494 0.0494 0.0496	Inal Doppler SNR 11445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 201.31140 1445.7176 1355.9751 pal Doppler SNR 3046.4523 2353.8329	SSIM 0.9866 0.9859 0.9656 0.9867 0.9783 0.8679 0.7955 0.9809 0.9889 0.9866 0.9863 0.9863 0.9863 0.9919 0.9919	RMSE 0.0077 0.081 0.0105 0.0105 0.0119 0.0598 0.0917 0.0066 0.0077 0.0080 RMSE 0.0053 0.0061	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 9.6011 879.0543 620.1223 501.3063 515.3938 Epr 1 SNR 967.6530 639.6839	SSIM 0.983 0.983 0.974 0.983 0.979 0.981 0.923 0.982 0.983 0.983 0.983 0.988 0.988	RMSE 0.0001 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 RMSE 0.0001 0.0001	Epr 2 SNR 775.6943 522.1809 552.0399 2313.037 627.2660 470.3268 153.0338 6.9417 775.582 762.3302 488.0483 558.1464 Epr 2 SNR 1223.803 672.985 1223.803	SSIM 3 0.98 9 0.98 0 0.98 1 0.98 0 0.98 0 0.98 0 0.98 0 0.98 0 0.98 0 0.98 0 0.98 0 0.98 0.911 0.97 2 0.98 3 0.98 4 0.98 32 0.98 5 0.98	I RMSE 44 0.0001 67 0.0002 37 0.0011 15 0.002 37 0.0011 52 0.0002 38 0.0012 88 0.0011 79 0.0001 68 0.0001 68 0.0001 69 0.0001
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SURE VINIMAX VINIMAX SNR=200 Selection Jniversal	Level S 2 3 </td <td>Blocks SNR 220.3258 20.8872 37.4016 11.9577 39.7255 14.0322 30.8600 39.0785 322.9315 322.9315 322.9315 322.9315 34.1791 21.10884 20.6287 Blocks SNR 35.9799 21.3155 77.6021 12.1343 34.02059</td> <td>SSIM 0.9077 0.7849 0.8509 0.7771 0.7869 0.7386 0.7386 0.7386 0.8305 0.9087 0.9383 0.9080 0.7776 SSIM 0.9323 0.7322 0.8841 0.7323 0.7323</td> <td>RMSE 0.1674 0.5179 0.3200 0.6702 0.2583 0.6218 0.3108 0.3104 0.0998 0.3889 0.1705 0.5201</td> <td>Bumps SNR 213.6559 13.2258 24.4045 2.6288 4.2942 6.1961 4.7928 428.1358 428.1358 428.1358 200.6697 11.5819 Bumps SNR 292.3541 14.2678 32.0694 2.7315 104.9249</td> <td>ssim 0.9082 0.7620 0.8644 0.6453 0.7031 0.6553 0.9377 0.8368 0.9115 0.7553 ssim 0.8291 0.7060 0.8291 0.7506 0.8291 0.75910 0.8090</td> <td>RMSE 0.0491 0.1792 0.1347 0.3433 0.0819 0.2828 0.2517 0.0349 0.0349 0.0507 0.1029 0.0421 0.1138 0.1184 0.0381</td> <td>Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 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0.983 0.974 0.983 0.974 0.982 0.982 0.983 0.988 0.983 0.988 0.988 0.987 0.981</td> <td>RMSE 5 0.000' 1 0.000' 1 0.000' 3 0.000' 1 0.000'</td> <td>Epr 2 SNR 775.6943 522.1806 552.039(2 2313.037 627.266(4 470.3286 153.0336 6.9417 775.5827 762.3302 488.0483 558.1464 Epr 2 SNR 1223.803 672.9854 762.6194 410.9174 933.8033</td> <td>SSIM 3 0.98 0 0.98 0 0.98 1 0.98 5 0.98 6 0.98 7 0.98 8 0.91 7 0.97 2 0.98 3 0.98 4 0.98 5 0.98 4 0.98 4 0.98 4 0.98 4 0.98</td> <td>RMSE 44 0.0001 37 0.0021 37 0.0011 15 0.0022 30 0.0031 31 0.0012 33 0.0013 34 0.0012 35 0.0011 40 0.0022 68 0.0011 40 0.0022 68 0.0001 40 0.0022 69 0.0001 99 0.0001 92 0.0001 93 0.0001 94 0.0001 95 0.0001</td>	Blocks SNR 220.3258 20.8872 37.4016 11.9577 39.7255 14.0322 30.8600 39.0785 322.9315 322.9315 322.9315 322.9315 34.1791 21.10884 20.6287 Blocks SNR 35.9799 21.3155 77.6021 12.1343 34.02059	SSIM 0.9077 0.7849 0.8509 0.7771 0.7869 0.7386 0.7386 0.7386 0.8305 0.9087 0.9383 0.9080 0.7776 SSIM 0.9323 0.7322 0.8841 0.7323 0.7323	RMSE 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0.98 6 0.98 7 0.98 9 0.98 9 0.98 9 0.92 9 0.92 9 0.92 9 0.92 9 0.92 9 0.92 9 0.92 9<</td> <td>RMSE 44 0.001 457 0.002 37 0.001 15 0.002 37 0.001 15 0.002 30 0.003 31 0.002 31 0.003 32 0.001 33 0.001 40 0.002 68 0.001 40 0.002 59 0.001 50 0.002 50 0.0021 50 0.0021 50 0.0021 50 0.0021 51 0.0031 52 0.0011 53 0.0021 54 0.0021 55 0.0011 56 0.0021</td>	Blocks SNR 220.3258 20.8872 37.4016 11.9577 39.7255 14.0322 30.8600 39.0785 322.9315 322.9315 322.9315 31.791 21.10884 20.6287 30.0cks SNR 31.55 31.791 21.3155 31.761 21.1345 31.762 31.1355 31.1	SSIM 0.9077 0.7869 0.7271 0.8569 0.7371 0.8809 0.7386 0.8809 0.7386 0.8501 0.8409 0.7386 0.8561 0.9188 0.8305 0.9037 0.7323 0.7422 0.8841 0.7323 0.7922 0.8411 0.9401 0.8421 0.8431	RMSE 0.1674 0.5779 0.3200 0.6702 0.2583 0.6218 0.3108 0.3108 0.3148 0.3488 0.3488 0.3488 0.3488 0.3488 0.3488 0.3498 0.4705 0.5201 RMSE 0.1187 0.5138 0.27665 0.2063 0.6172 0.3093 0.6172 0.3093 0.6172 0.3133 0.0734 0.3744 0.3734 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0.3734 0.3744 0	Bumps SNR 213.6559 13.2258 24.4045 2.6288 4.2942 6.1961 4.7928 428.1358 428.1358 200.6697 11.5819 Bumps SNR 292.3541 14.2678 32.0694 2.7315 104.9249 4.5561 6.2119 4.8083 638.7912 49.7865	ssim 0.9082 0.7620 0.8424 0.6533 0.8764 0.6643 0.7031 0.6553 0.7766 0.8388 0.9115 0.7653 ssim 0.7921 0.7966 0.89690 0.5910 0.5920 0.6583 0.7145 0.6614 0.6514 0.9070 0.6583 0.7145 0.6144 0.6514 0.9574 0.8480	RMSE 0.0491 0.1792 0.3433 0.2828 0.2517 0.2732 0.0349 0.0290 0.0507 0.0349 0.04020 0.0507 0.1822 RMSE 0.0421 0.1738 0.1184 0.0686 0.2763 0.2514 0.2784 0.0285 0.0285	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1175.0474 670.1873 545.4891 1355.1443 1353.1443 2106.5750 Heavisine SNR 3965.4110 4006.7168 1632.9167 1187.9494 2389.3626 203.6369 732.9354 542.0173 3027.7771 4584.1827	SSIM 0.9887 0.9883 0.9814 0.9833 0.9813 0.9822 0.9833 0.9826 0.9836 0.9836 0.9846 0.9836 0.9836 0.9836 0.9935 0.9935 0.9934 0.9934 0.9935 0.9934 0.9935 0.9934 0.9935 0.9944 0.9954 0.9954 0.9954 0.9954 0.9954 0.9954	Sig RMSE 0.0694 0.0694 0.0697 0.0944 0.0607 0.0839 0.0809 0.0831 0.0863 0.0647 0.0647 0.0647 0.0647 0.0647 0.0647 0.0647 0.0647 0.0647 0.0647 0.0647 0.0646 0.0494 0.0494 0.0494 0.0495 0.0687 0.0489 0.0489 0.0489 0.0489 0.0489 0.0481 0.0482 0.0483 0.0484 0.0484 0.0485 0.0484	nal Doppler SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476 1472.3381 1472.3381 1472.3381 1472.3381 1472.3387 2013.1140 1445.7176 1355.9751 3046.4523 2353.8329 535.1242 293.3397 20.3457 22.8159 8.9632 955.7837 22.8159 8.9632 3004.7534 3004.7534 3004.7534	SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9783 0.9783 0.9889 0.9860 0.9860 0.9880 0.9919 0.9903 0.9736 0.9940 0.9736 0.9736 0.9884 0.9884 0.9844 0.8687 0.7961	RMSE 0.0077 0.0081 0.0164 0.0105 0.0119 0.0598 0.0077 0.0080 0.0077 0.0080 0.0078 0.0076 0.0080 RMSE 0.0053 0.0054 0.0170 0.0074 0.0075 0.0074 0.0074 0.0075 0.0170 0.0074 0.0074 0.0075 0.0074	Epr 1 SNR 668.1910 513.2964 545.6898 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543 620.1223 501.3063 515.3938 Epr 1 SNR 967.6530 639.6839 660.4859 311.8605 770.7496 521.6119 188.633 9.6334 1367.462 963.0752	SSIM 0.983 0.983 0.974 0.983 0.974 0.983 0.979 0.982 0.983 0.983 0.988 0.988 0.988 0.988 0.988 0.988 0.988 0.988 0.985 0.995 0	RMSE 5 0.0001 1 0.0001 2 0.0002 3 0.0002 2 0.0002 1 0.00011 2 0.0002 2 0.00011 2 0.00011 2 0.00011 2 0.00011 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 2 0.00012 3 0.00012 3 0.00012 4 0.00012 4 0.00012 4 0.00012 4 0.00012	Epr 2 SNR 775.6943 522.1806 552.039(2 2313.037 627.266(4 470.3283 6.9417 775.5827 762.302 488.0483 558.1464 Epr 2 SNR 1223.803 672.9854 762.6194 410.9177 933.8033 551.2632 159.7464 6.9445 1365.17 1365.47 1375.47	SSIM 3 0.98 0 0.98 1 0.98 1 0.98 2 0.98 5 0.98 5 0.98 5 0.98 5 0.98 5 0.98 5 0.98 3 0.98 5 0.98 5 0.98 5 0.98 4 0.98 4 0.98 5 0.98 4 0.98 5 0.98 4 0.98 5 0.98 6 0.98 7 0.98 9 0.98 9 0.98 9 0.92 9 0.92 9 0.92 9 0.92 9 0.92 9 0.92 9 0.92 9<	RMSE 44 0.001 457 0.002 37 0.001 15 0.002 37 0.001 15 0.002 30 0.003 31 0.002 31 0.003 32 0.001 33 0.001 40 0.002 68 0.001 40 0.002 59 0.001 50 0.002 50 0.0021 50 0.0021 50 0.0021 50 0.0021 51 0.0031 52 0.0011 53 0.0021 54 0.0021 55 0.0011 56 0.0021
) 3 3 4 7 7 7 7 8 4 4 7 7 8 9 4 4 7 7 7 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	COIF3 5 Istended 5 Istand L ioft L ioft L istance L iard L irrm L ioft L ioarotte L iard L iard L	SNR=100 Selection Jniversal Jniversal Heur. SURE VINIMAX VINIMAX SNR=200 Selection Jniversal Jniversal Heur. SURE VINIMAX	Level S 5 2 5 6 5 6 6 1 6 1 5 6 6 1 6 5 6 1 5 6 5 6 5 6 5 6 5 7 6 1 6 1 6 1 6 1 6 5 6 5 6 5 6 5 6 5 5 4	Blocks SNR 220.3258 20.8872 37.4016 11.9577 39.7255 14.0322 30.8600 39.0765 322.9315 81.791 21.10884 20.6287 Blocks SNR 13.557799 21.3155 77.6021 12.1343 140.2059 14.0294 31.7689 39.6630 1130.4263 39.4177 107.6570	SSIM 0.9077 0.7869 0.7271 0.8569 0.7271 0.8809 0.7386 0.8809 0.7386 0.8809 0.8305 0.9085 0.9087 0.7323 0.7922 0.8841 0.7323 0.7323 0.9105 0.7439 0.9305 0.8411 0.8113 0.9401 0.8392 0.9401 0.8392	RMSE 0.1674 0.1674 0.2503 0.6702 0.2583 0.6218 0.3104 0.3104 0.3188 0.3144 0.0998 0.3889 0.1705 0.5201 RMSE 0.1187 0.5138 0.2754 0.4615 0.2615 0.3899 0.2020 0.2020 0.2020 0.2020 0.3133 0.0203 0.2020 0.3133 0.0203 0.36172 0.3090 0.3133 0.0203 0.3637 0.3744 0.3637 0	Bumps SNR 213.6559 13.2258 24.4045 2.6288 4.2942 6.1961 4.7928 428.1358 428.1358 428.1358 426.564 200.6697 11.5819 Bumps SNR 292.3541 14.2678 32.0694 2.7315 104.9249 4.5561 6.2119 4.5561 6.38.7912 4.97865 293.4173	ssim 0.9082 0.7620 0.8424 0.6533 0.8701 0.6553 0.9377 0.8368 0.9115 0.7553 ssim 0.5910 0.7706 0.5910 0.6514 0.9574 0.8480 0.9355	RMSE 0.0491 0.1792 0.3433 0.0343 0.2517 0.2732 0.0349 0.01029 0.0421 0.1738 0.1424 0.0421 0.0421 0.0421 0.0421 0.0566 0.2763 0.0686 0.02654 0.02854 0.0285 0.0285 0.0426	Heavisine SNR 2022.6848 2128.1522 1072.3945 798.3356 1365.8412 1355.412 1475.0474 670.1873 545.4891 1353.1443 2448.0742 2015.0713 2106.5750 Heavisine SNR 3965.4110 4006.7168 1632.9167 1187.9494 2389.3626 2329.354 542.0173 3027.7711 3645.4121 3027.7712 3848.6653	SSM 0.9887 0.9883 0.9814 0.9833 0.9822 0.9728 0.9635 0.9865 0.9865 0.9838 0.9839 0.9840 0.9830 0.9842 0.9843 0.9935 0.9935 0.9936 0.9937 0.9938 0.9941 0.9944 0.9944 0.9945 0.9946 0.99475 0.9948 0.9948 0.9948 0.9948 0.9948 0.9949 0.9940 0.9941	Sig RMSE 0.0694 0.0694 0.0694 0.0839 0.0809 0.0801 0.0832 0.0839 0.0807 0.1191 0.1323 0.0837 0.0839 0.0807 0.0647 0.0647 0.0647 0.0647 0.0647 0.0494 0.0494 0.0494 0.0495 0.0683 0.0455 0.0684 0.1138 0.1327 0.0566 0.0566	nal Doppier SNR 1445.0967 1339.6524 316.0377 205.8504 790.2273 611.0427 22.7148 8.9476 1472.3381 2013.1140 1445.7176 1355.9751 mal Dopper SNR 3046.4523 255.1242 293.3397 1586.7429 955.7837 22.8159 8.9632 3004.7534 3076.8059 3041.6173	 SSIM 0.9866 0.9859 0.9709 0.9656 0.9807 0.9703 0.8679 0.9803 0.9863 0.9863 0.9863 0.9930 0.9763 0.9803 0.9784 0.9803 0.9784 0.9803 0.9784 0.9803 0.9784 0.9803 0.9784 0.9803 0.9784 0.9803 0.9786 0.9803 0.9786 0.9803 0.9786 0.9804 0.9844 0.9844	RMSE 0.0077 0.0081 0.0164 0.0105 0.0119 0.0598 0.0917 0.0066 0.0077 0.0080 RMSE 0.0053 0.0061 0.0126 0.0174 0.0053 0.0074 0.0053 0.0074 0.0075 0.0074 0.0075	Epr 1 SNR 668.1910 513.2964 545.6098 216.0126 608.0694 398.5573 185.9973 9.6011 879.0543 620.1223 501.3063 515.3938 Epr 1 SNR 967.6530 639.6839 660.4859 311.8605 770.7496 521.6119 188.3633 9.6334 1367.462 963.0752 592.3201	SSIM 0.983 0.974 0.983 0.974 0.981 0.982 0.983 0.983 0.983 0.988 0.988 0.988 0.988 0.988 0.988 0.987 0.981 0.988 0.985 0.995 0.985 0.985 0.985 0.985 0.985 0.985 0.985 0.985 0.985 0.985 0.985 0.985 0.985 0.985 0.985 0.995 0	RMSE 5 0.0001 3 0.00021 1 0.0001 2 0.0001 2 0.0001 1 0.0001 2 0.0001 2 0.0001 2 0.0001 5 0.0001 6 0.0001 0 0.0002 0 0.0001 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 0 0.0002 <	Epr 2 SNR 775.6943 522.1806 552.039(2 2313037 6.9417 775.5821 775.5821 775.5821 775.5821 762.302 488.0483 558.1464 Epr 2 SNR 1223.803 672.9854 762.6194 410.9174 933.8033 551.2633 2159.7463 6.9445 1365.177 1365.1	SSIM 3 0.98 4 0.98 5 0.98 6 0.98 6 0.98 6 0.98 6 0.98 7 0.98 6 0.98 7 0.98 7 0.98 8 0.98 8 0.98 8 0.98 5 0.98 5 0.94 4 0.98 7 0.98 8 0.98 9 0.98 0.92 0.98 0.92 0.98 0.93 0.92 0.94 0.98 0.92 0.98 0.93 0.92	RMSE 44 0.001 67 0.002 37 0.001 15 0.002 37 0.001 52 0.002 30 0.001 31 0.002 32 0.001 34 0.002 35 0.001 36 0.001 37 0.001 30 0.001 31 0.002 32 0.001 33 0.001 34 0.002 35 0.001 36 0.002 37 0.001 38 0.001 37 0.001 38 0.001 39 0.001 318 0.001 318 0.001 318 0.001 319 0.001

Table S1. Performance of the SWT at decomposition levels 5 and 6 with the coif 3 wavelet for 6 thresholding combinations. The tables give the performance of each combination in terms of SNR, SSIM, and RMSE in order of increasing starting SNR (10, 50, 100, 200) of the noisy test signal. Results are presented for the following test signals: blocks, bumps, heavisine, doppler, 1st EPR test signal, and 2nd EPR test signal. Method refers to the thresholding form, while selection refers to the means of calculating the threshold value.

				_			-														
	COIF4	SNR=10		BIOCKS			Bumps			Heavisine			Doppier			Epr 1			Epr 2		
	Metho	d Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	35.9052	0.7388	0.4046	31.4528	0.7140	0.1238	248.2443	0.9506	0.1968	129.0582	0.9207	0.0261	195.8470	0.9164	0.0002	206.0534	0.9123	0.0002
	Halu	Universal	6	16.1175	0.7046	0.5848	7.3690	0.6365	0.2331	282.0648	0.9493	0.1847	120.5438	0.9227	0.0267	162.2021	0.9305	0.0002	216.1024	0.9397	0.0002
			5	25,2813	0 7124	0.4780	6.3290	0 6018	0.2475	246.0888	0 9521	0.1976	52,7927	0 8895	0.0397	165,3036	0 9168	0.0002	165.0094	0 9112	0.0003
	Soft	Universal	6	10.2700	0.7124	0 7171	2,0600	0.0010	0.2024	256 2207	0.03021	0.1021	26 0172	0.0000	0.0467	50 0070	0.0175	0.0002	95 4400	0.0220	0.0004
			6	10.3700	0.0/2/	0./1/1	2.0090	0.4785	0.3624	200.2097	0.9490	0.1931	30.9173	0.0025	0.0407	30.0070	0.91/5	0.0003	00.4192	0.9259	0.0004
	Garotte	e Universal	э	20.7425	0.7170	0.4652	11.3619	0.6543	0.1928	240.3305	0.9521	0.1975	11.4289	0.9046	0.0331	180.3249	0.9164	0.0002	107.0200	0.9114	0.0003
SW	т		6	11.5310	0.6818	0.6822	2.9413	0.5348	0.3332	261.7692	0.9491	0.1911	65.1905	0.9037	0.0358	108.8544	0.9258	0.0002	152.3667	0.9329	0.0003
	Hard	Heur, SURF	5	48.4654	0.7562	0.3489	5.7521	0.5765	0.2621	247.2566	0.9516	0.1972	21.2484	0.8410	0.0619	125.6078	0.9174	0.0002	108.8837	0.9110	0.0003
			6	49.2777	0.7828	0.3443	4.4971	0.5899	0.2826	296.4051	0.9521	0.1802	8.7779	0.7786	0.0926	9.3010	0.8730	0.0007	6.8460	0.8619	0.0012
	Hard		5	72.5885	0.7730	0.2888	67.6204	0.7565	0.0865	134.6387	0.8534	0.2823	143.2566	0.8968	0.0249	138.0696	0.8907	0.0002	131.8611	0.8820	0.0003
	mara		6	24.9435	0.7408	0.4778	24.5838	0.7275	0.1384	183.9663	0.8676	0.2544	192.3958	0.9286	0.0213	191.7769	0.9355	0.0002	250.2723	0.9414	0.0002
			5	36,7563	0.7400	0.3990	28.2232	0.7154	0.1293	251.0934	0.9471	0.1959	126.0477	0.9189	0.0262	195.7465	0.9157	0.0002	207.6875	0.9111	0.0002
	Firm	MINIMAX	6	15 7982	0 7046	0.5891	6 7572	0.6309	0 2395	289 9108	0 9447	0 1823	121 8164	0 9223	0.0266	133 6359	0 9356	0 0002	190 1030	0 9404	0.0003
			0	10.1002	0.7040	0.0001	0.1012	0.0505	0.2000	200.0100	0.5447	0.1020	121.0101	0.5225	0.0200	100.0000	0.5550	0.0002	100.1000	0.3404	0.0000
				_			_					SI	jnai								
	COIF4	SNR=50		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Metho	d Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hord	Universal	5	105.7130	0.8540	0.2386	97.4161	0.8483	0.0723	928.5443	0.9770	0.1018	676.4126	0.9734	0.0113	486.5547	0.9740	0.0001	479.8274	0.9745	0.0002
	Halu	Universal	6	19.0621	0.7511	0.5425	8.7343	0.7006	0.2161	1023.3733	0.9781	0.0975	677.3955	0.9754	0.0113	349.0700	0.9722	0.0001	428.3581	0.9806	0.0002
			5	40,4096	0 8037	0.3805	13,9661	0 7534	0.1738	655.0390	0 9712	0.1210	177.4126	0 9520	0.0219	394.0117	0 9736	0.0001	412,2868	0 9740	0.0002
	Soft	Universal	6	11 3890	0 7020	0.6878	2 2433	0.5200	0.3682	521 1115	0.9664	0 1357	125 3222	0.0468	0.0260	125 6510	0.0587	0.0002	220 1285	0.0731	0.0002
			5	F2 5251	0.7029	0.0070	24 00 10	0.3235	0.1173	705 5065	0.9004	0.1357	377 4470	0.9408	0.0200	123.0010	0.5367	0.0002	461 4661	0.9731	0.0002
	Garotte	e Universal	5	00.0201	0.8225	0.3322	34.0619	0.8114	0.11/2	725.5005	0.9730	0.1151	3/1.44/0	0.9650	0.0152	404.0010	0.9756	0.0001	401.4001	0.9742	0.0002
SW	т		6	13.1786	0./139	0.6424	3.3440	0.5901	0.3145	652.1424	0.9705	0.1218	313.0257	0.9633	0.0167	234.5317	0.9643	0.0002	368.5970	0.9791	0.0002
	Hard	Heur. SURE	5	57.0754	0.8289	0.3215	5.8131	0.6506	0.2601	555.2683	0.9666	0.1312	22.5119	0.8623	0.0601	176.8102	0.9724	0.0002	151.0636	0.9723	0.0003
			6	55.3164	0.8279	0.3252	4.4967	0.6254	0.2818	467.1477	0.9653	0.1435	8.8855	0.7919	0.0922	9.4507	0.9087	0.0007	6.9545	0.9062	0.0012
	Hard	ΜΙΝΙΜΔΥ	5	242.9689	0.8705	0.1583	213.2484	0.8810	0.0492	647.0876	0.9383	0.1251	698.9193	0.9610	0.0113	507.4947	0.9702	0.0001	455.3316	0.9658	0.0002
	mara		6	31.7054	0.7951	0.4271	30.4385	0.7898	0.1243	1064.0682	0.9644	0.0982	911.0589	0.9748	0.0098	471.2778	0.9795	0.0001	510.2059	0.9828	0.0002
	-		5	101.4251	0.8536	0.2433	93.6644	0.8495	0.0733	916.3671	0.9760	0.1025	671.1986	0.9734	0.0114	439.9303	0.9737	0.0001	369.3515	0.9740	0.0002
	Firm	MINIMAX	6	18.8816	0.7466	0.5436	8.1230	0.6921	0.2202	999.0261	0.9772	0.0987	655,7505	0.9752	0.0115	343.9621	0.9718	0.0001	442.9016	0.9816	0.0002
				•																	
	00154	0.15.400					_					Się	gnal								
	COIF4	SNR=100		Blocks		_	Bumps			Heavisine		Sig	gnal Doppler			Epr 1			Epr 2		
	COIF4 Method	SNR=100 Selection	Level	Blocks SNR	SSIM	RMSE	Bumps SNR	SSIM	RMSE	Heavisine SNR	SSIM	Się RMSE	gnal Doppler SNR	SSIM	RMSE	Epr 1 SNR	SSIM	RMSE	Epr 2 SNR	SSIM	RMSE
	COIF4 Method	SNR=100 Selection Universal	Level	Blocks SNR 165.0189	SSIM 0.8969	RMSE 0.1928	Bumps SNR 141.8517	SSIM 0.8864	RMSE 0.0603	Heavisine SNR 1918.3577	SSIM 0.9882	Sig RMSE 0.0711	nal Doppler SNR 1549.5580	SSIM 0.9871	RMSE	Epr 1 SNR 665.2106	SSIM 0.9834	RMSE	Epr 2 SNR 769.7876	SSIM 0.984	RMSE
	COIF4 Method Hard	SNR=100 Selection Universal	Level 5 6	Blocks SNR 165.0189 18.5700	SSIM 0.8969 0.7570	RMSE 0.1928 0.5480	Bumps SNR 141.8517 8.6582	SSIM 0.8864 0.7147	RMSE 0.0603 0.2164	Heavisine SNR 1918.3577 1951.9919	SSIM 0.9882 0.9886	RMSE 0.0711 0.0704	mal Doppler SNR 1549.5580 1530.7926	SSIM 0.9871 0.9871	RMSE 0.0075 0.0076	Epr 1 SNR 665.2106 496.2153	SSIM 0.9834 0.9842	RMSE 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071	SSIM 0.984	RMSE 2 0.0001 7 0.0002
	COIF4 Method Hard	SNR=100 Selection Universal	Level 5 6 5	Blocks SNR 165.0189 18.5700 50.5561	SSIM 0.8969 0.7570 0.8468	RMSE 0.1928 0.5480 0.3408	Bumps SNR 141.8517 8.6582 18.2711	SSIM 0.8864 0.7147 0.8044	RMSE 0.0603 0.2164 0.1542	Heavisine SNR 1918.3577 1951.9919 1025.8273	SSIM 0.9882 0.9886 0.9808	Sig <u>RMSE</u> 0.0711 0.0704 0.0964	mal Doppler SNR 1549.5580 1530.7926 338.2191	SSIM 0.9871 0.9871 0.9717	RMSE 0.0075 0.0076 0.0159	Epr 1 SNR 665.2106 496.2153 528.7430	SSIM 0.9834 0.9842 0.9829	RMSE 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270	SSIM 0.984 0.986 0.983	RMSE 2 0.0001 7 0.0002 5 0.0001
	COIF4 Method Hard Soft	SNR=100 Selection Universal Universal	Level 5 6 5 6	Blocks SNR 165.0189 18.5700 50.5561 11.2151	SSIM 0.8969 0.7570 0.8468 0.7084	RMSE 0.1928 0.5480 0.3408 0.6918	Bumps SNR 141.8517 8.6582 18.2711 2.2336	SSIM 0.8864 0.7147 0.8044 0.5450	RMSE 0.0603 0.2164 0.1542 0.3683	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462	SSIM 0.9882 0.9886 0.9808 0.9732	RMSE 0.0711 0.0704 0.0964 0.1124	mal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200	SSIM 0.9871 0.9871 0.9717 0.9671	RMSE 0.0075 0.0076 0.0159 0.0192	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361	SSIM 0.9834 0.9842 0.9829 0.9700	RMSE 0.0001 0.0001 0.0001 0.0002	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449	SSIM 0.984 0.986 0.983 0.980	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002
	COIF4 Method Hard Soft	SNR=100 Selection Universal Universal	Level 5 6 5 6 5 5	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844	RMSE 0.0711 0.0704 0.0964 0.1124 0.0862	mal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424	SSIM 0.9871 0.9871 0.9717 0.9671 0.9811	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706	SSIM 0.984 0.986 0.983 0.980 0.983	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001
	COIF4 Method Hard Soft Garotte	SNR=100 Selection Universal Universal Universal	Level 5 6 5 6 5 6 5 6	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811	Sig RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938	mal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931	SSIM 0.9871 0.9871 0.9717 0.9671 0.9811 0.9794	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.0112	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681	SSIM 0.984 0.986 0.983 0.980 0.983 0.985	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001 2 0.0002
SWT	COIF4 Method Hard Soft Garotte	SNR=100 Selection Universal Universal	Level 5 6 5 6 5 6 5 6	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058	SSIM 0.8969 0.7570 0.8468 0.8692 0.7084 0.8692 0.7193	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5 7995	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6780	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2320	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811 0.9731	Sig RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.1107	mal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270	SSIM 0.9871 0.9871 0.9717 0.9671 0.9671 0.9811 0.9794	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.0112	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763 0.9763	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156 1583	SSIM 0.984 0.986 0.983 0.980 0.983 0.985	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001 2 0.0002 1 0.0002
SWT	COIF4 Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 6	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.0255	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8595	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4730	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6202	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.3820	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811 0.9721 0.9664	Sig RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.1197 0.1264	mal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 8 9000	SSIM 0.9871 0.9717 0.9671 0.9671 0.9811 0.9794 0.8667	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.0112 0.0601	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 0.4655	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763 0.9763 0.9811	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.0591	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.985 0.981	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001 2 0.0002 3 0.0002 1 0.0002
SWT	COIF4 Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 6 5 6	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 54.9785	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.3256	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6392	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2820	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811 0.9721 0.9684	RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.1197 0.1364	ganal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 8.8999	SSIM 0.9871 0.9871 0.9717 0.9671 0.9811 0.9794 0.8667 0.7944	RMSE 0.0075 0.0159 0.0192 0.0101 0.0112 0.0601 0.0921	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763 0.9763 0.9811 0.9145	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0002 0.0007	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 700 7000	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.985 0.981 0.910	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0003 0.0003 0.0002
SWT	COIF4 Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 5	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 479.7317	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.3256 0.1135	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6392 0.9213	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2820 0.0414	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811 0.9721 0.9684 0.9639	RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.1197 0.1364 0.0863	mal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 8.8999 14760.0339	SSIM 0.9871 0.9871 0.9671 0.9671 0.9811 0.9794 0.8667 0.7944	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.0112 0.0601 0.0921 0.0078	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763 0.9811 0.9145 0.9816	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0007 0.0007	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.985 0.981 0.910 0.910	RMSE 0.0001 0.0002
SWT	COIF4 Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 6 5 6	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 479.7317 30.7671	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8030	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.3256 0.1135 0.4315	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 30.5932	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6392 0.9213 0.9213 0.8044	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2820 0.0414 0.1238	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 2226.6253	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811 0.9721 0.9684 0.9639 0.9796	RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.1197 0.1364 0.0863 0.0679	nal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 8.8999 1476.0339 2033.2418	SSIM 0.9871 0.9717 0.9671 0.9671 0.9811 0.9794 0.8667 0.7944 0.9790 0.9882	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.0112 0.0601 0.0921 0.0078 0.0066	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763 0.9811 0.9145 0.9816 0.9865	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0007 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.910 0.978 0.987	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001 1 0.0003 3 0.0012 2 0.0001 4 0.0001
SWT	COIF4 Method Hard Soft Garotte Hard Hard Firm	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 5 6 5 5 5	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 479.7317 30.7671 163.9634	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8030 0.8986	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.3256 0.1135 0.4315 0.1932	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 30.5932 136.5921	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6392 0.9213 0.8044 0.8884	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2820 0.0414 0.1238 0.0612	Heavisine <u>SNR</u> 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2229 1334.6661 12226.6253 1911.0495	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811 0.9721 0.9684 0.9639 0.9796 0.9786	RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.1197 0.1364 0.0863 0.0679 0.0710	nal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 8.8999 1476.0339 2033.2418 1516.7946	SSIM 0.9871 0.9871 0.9717 0.9671 0.9811 0.9794 0.8667 0.7944 0.9790 0.9882 0.9882	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.0112 0.0601 0.0921 0.0078 0.0066 0.0076	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763 0.9811 0.9145 0.9816 0.9865 0.9833	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.910 0.978 0.987 0.987	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001 1 0.0003 3 0.0012 2 0.0001 4 0.0001 5 0.0001 6 0.0001 7 0.0001 8 0.0002
SWT	COIF4 Method Hard Soft Garotte Hard Hard Firm	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 479.7317 30.7671 163.9634 18.4386	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8030 0.8986 0.7509	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.1135 0.4315 0.1932 0.5482	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 305.0808 305.5932 136.5921 8.0906	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6392 0.9213 0.8044 0.8884 0.7067	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2820 0.0414 0.1238 0.0612 0.2202	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6661 1334.6661 2262.6253 1911.0495 1951.8110	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811 0.9721 0.9684 0.9639 0.9796 0.9880 0.9880 0.9887	RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.1197 0.1364 0.0863 0.0679 0.0710 0.0704	Joppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 1476.0339 2033.2418 1516.7946 1505.0257	SSIM 0.9871 0.9871 0.9671 0.9671 0.9811 0.9794 0.8667 0.7944 0.9790 0.9882 0.9869 0.9871	RMSE 0.0075 0.0159 0.0192 0.0111 0.012 0.0601 0.0921 0.0076 0.0076	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 9.4665 607.8531 519.7587 477.6022	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763 0.9811 0.9145 0.9816 0.9865 0.9833 0.9830	RMSE 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.910 0.978 0.987 0.987 0.983	RMSE 0.0001 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0002 0.0003 0.0002 0.00012 0.00012 0.00013 0.00014 0.00015 0.00017 0.00017 0.0002 0.00017 0.00017 0.00017
SWT	COIF4 Method Hard Soft Garotte Hard Hard Firm	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX	Level 5 6 5 6 5 6 5 5 6 5 5 6 5 6 5 6 5 6	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 54.9785 54.9785 54.9785 163.9634 18.4386	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8030 0.8986 0.7509	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.1135 0.4315 0.1932 0.5482	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 30.5932 136.5921 8.0906	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6392 0.9213 0.8044 0.8884 0.7067	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2820 0.0414 0.1238 0.0612 0.2202	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1951.8110	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811 0.9721 0.9684 0.9639 0.9796 0.9880 0.9880	RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.1197 0.1364 0.0863 0.0679 0.0710 0.0704 Sig	mal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 8.8999 1476.0339 2033.2418 1516.7946 1505.0257 mal	SSIM 0.9871 0.9717 0.9671 0.9811 0.9794 0.8667 0.7944 0.9790 0.9882 0.9869 0.9871	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.0112 0.0601 0.0921 0.0078 0.0066 0.0076	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763 0.9811 0.9145 0.9816 0.9865 0.9833 0.9830	RMSE 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.910 0.978 0.987 0.983 0.986	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001 1 0.0002 1 0.0002 1 0.0003 2 0.00012 2 0.00013 3 0.00014 4 0.00014 5 0.00014 6 0.00024 7 0.00014
SWT	COIF4 Method Hard Soft Garotte Hard Hard Firm	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX	Level 5 5 6 5 5 6 5 5 6 5 5 6 5 6 5 6 5 6 5	Blocks SNR 165.0189 18.5700 50.5561 11.2151 12.8957 57.2058 54.9785 479.7317 30.7671 163.9634 18.4386 Blocks	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8030 0.8986 0.7509	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.1135 0.4315 0.1932 0.5482	Bumps SNR 141.8517 8.6582 18.2711 2.2336 4.9.0371 3.3257 5.7995 4.4739 305.0808 30.5932 136.5921 8.0906 Bumps	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6392 0.9213 0.8044 0.8884 0.7067	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2820 0.0414 0.1238 0.0612 0.2202	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 2226.6253 1911.0495 1951.8110 Heavisine	SSIM 0.9882 0.9886 0.9732 0.9844 0.9841 0.9721 0.9684 0.9639 0.9639 0.9796 0.9880 0.9887	RMSE 0.0711 0.0704 0.1124 0.0862 0.0938 0.1197 0.1364 0.0863 0.0679 0.0710 0.0704 Sig	ganal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 8.8999 1476.0339 2033.2418 1516.7946 1500.5027 mal Doobler	SSIM 0.9871 0.9871 0.9671 0.9671 0.9811 0.9794 0.8667 0.7944 0.9790 0.9882 0.9869 0.9871	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.0112 0.0601 0.0921 0.0078 0.0066 0.0076	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022 Epr 1	SSIM 0.9834 0.9842 0.9700 0.9700 0.9831 0.9763 0.9811 0.9145 0.9816 0.9865 0.9833 0.9830	RMSE 0.0001 0.0001 0.0002 0.0001 0.0002 0.0007 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.910 0.978 0.987 0.983 0.986	RMSE 2 0.0001 7 0.0002 5 0.0011 7 0.0002 8 0.00012 1 0.0003 3 0.0012 2 0.00013 3 0.00012 2 0.00013 3 0.0002 7 0.00014
SWT	COIF4 Method Hard Soft Garotte Hard Hard Firm COIF4	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200	Level 5 5 6 5 5 6 5 5 6 5 6 5 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 7 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 6 6 6 5 6 6 6 6 6 5 6 6 6 6 6 5 6 6 6 5 6 6 6 6 6 6 6 6 5 6	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 54.9785 54.9785 14.9785 163.9634 18.4386 Blocks SNP	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8030 0.8030 0.8986 0.7509 0.8986 0.7509	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.1135 0.4315 0.1932 0.5482	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 30.5932 136.5921 8.0906	SSIM 0.8864 0.7147 0.8044 0.5450 0.6342 0.6392 0.9213 0.8044 0.8884 0.7067	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2820 0.0414 0.1238 0.0612 0.2202	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 1324.6661 1324.6661 1324.6661 1324.6661 1324.6661 1324.6661 1324.8661 1324.8661 1324.8661 S258 1911.045 1951.8110 Heavisine SNP	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9811 0.9721 0.9684 0.9639 0.9796 0.9880 0.9887	Sig 0.0711 0.0704 0.0964 0.0964 0.0938 0.1124 0.0862 0.0938 0.1197 0.1364 0.0863 0.0679 0.0710 0.0704 Sig	ymail Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 8.8999 1476.0339 2033.2418 1516.7946 1505.0257 mail Doppler SNP	SSIM 0.9871 0.9871 0.9671 0.9671 0.9811 0.9794 0.8667 0.7944 0.9790 0.9882 0.9869 0.9871	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.0112 0.0601 0.0921 0.0076 0.0076	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022 Epr 1 SNP	SSIM 0.9834 0.9842 0.9829 0.9700 0.9831 0.9763 0.9811 0.9145 0.9816 0.9865 0.9833 0.9830	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2 SNP	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.910 0.978 0.987 0.983 0.986	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001 1 0.0002 1 0.00012 2 0.000112 2 0.00011 3 0.00012 4 0.00001 5 0.00001 6 0.00002 7 0.00001
SWT	COIF4 Method Hard Soft Garotte Hard Hard Firm COIF4 Method	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection	Level 5 5 6 5 5 6 6 5 6 6 5 6 6 5 6 6 7 6 8 7 8 8	Blocks SNR 165.0189 18.5700 50.5561 12.8957 57.2058 54.9785 479.7317 30.7671 163.9634 18.4386 Blocks SNR	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8030 0.8986 0.7509 SSIM	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.1135 0.4315 0.1932 0.5482	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 305.0808 305.0828 136.5921 8.0906 Bumps SNR	SSIM 0.8864 0.7147 0.8044 0.8565 0.6044 0.6392 0.9213 0.8044 0.8884 0.7067 SSIM	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2820 0.0414 0.1238 0.0612 0.2202 RMSE	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 1324.6661 1324.6623 1911.0495 1951.8110 Heavisine SNR	SSIM 0.9882 0.9886 0.9808 0.9732 0.9844 0.9631 0.9684 0.9639 0.9684 0.9639 0.9796 0.9880 0.9887 0.9887	RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.1197 0.1364 0.0863 0.0679 0.0710 0.0704 Sig RMSE	mai Doppler SNR 1549,5580 1549,5580 1550,7226 338,2191 229,4200 848,5424 694,5931 225,270 8,8999 1476,0339 2033,2418 1516,7946 1505,0257 mai Doppler SNR	SSIM 0.9871 0.9871 0.9717 0.9671 0.9811 0.9794 0.8667 0.7944 0.9790 0.9882 0.9869 0.9871 SSIM	RMSE 0.0075 0.0076 0.0159 0.0192 0.0101 0.00112 0.0001 0.0078 0.0066 0.0076 RMSE	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR	SSIM 0.9834 0.9842 0.9700 0.9831 0.9763 0.9811 0.9145 0.9816 0.9865 0.9833 0.9830 SSIM	RMSE 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2 SNR	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.910 0.978 0.987 0.983 0.986 SSIM	RMSE 2 0.0001 7 0.0002 5 0.0001 2 0.0002 3 0.00012 1 0.0002 2 0.00012 1 0.00013 2 0.00017 3 0.0002 7 0.0001 RMSE 0.0002
SWT	COIF4 Method Hard Soft Garotte Hard Firm COIF4 Method Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal	Level 5 5 6 6 5 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 6 6 6 7 6 6 6 6 7 7 8 8 8 8 8 8 8 8 8 8 8 8 8	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 479.7317 30.7671 163.9634 18.4386 Blocks SNR 206.61629 (10.0007)	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8030 0.9106 0.8030 0.9106 0.8030 0.9106 0.8030 0.9106 0.8030 0.9106 0.8030 0.9106 0.9106 0.8030 0.9106 0.9100 0.8030 0.9100 0.8030 0.9100 0.8030 0.9100 0.8030 0.9100 0.8030 0.91000 0.91000 0.91000 0.91000 0.91000 0.91000 0.91000 0.91000 0.91000 0.910000 0.910000 0.9100000 0.9100000000000000000000000000000000000	RMSE 0.1928 0.5480 0.3408 0.2828 0.6477 0.3205 0.3256 0.1135 0.3256 0.1135 0.4315 0.1932 0.5482	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 305.0808 30.5932 136.5921 8.0906 Bumps SNR	SSIM 0.8864 0.7147 0.8044 0.5450 0.6565 0.6044 0.6392 0.9213 0.8044 0.8884 0.7067 SSIM 0.9014	RMSE 0.0603 0.2164 0.1542 0.3094 0.3148 0.2600 0.0414 0.1238 0.0612 0.2202 RMSE 0.0534	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1951.8110 Heavisine SNR 3586.3914	SSIM 0.9882 0.9886 0.9732 0.9844 0.9811 0.9721 0.9684 0.9683 0.9796 0.9880 0.9887 0.9887 SSIM	RMSE 0.0711 0.0704 0.0964 0.1124 0.0938 0.1197 0.1364 0.0863 0.0679 0.0710 0.0704 Sig RMSE 0.0522 0.0522	ganal Doppler SNR 1549-5580 1530.7926 38.2191 229.4200 848-5424 694.5931 22.5270 1476.0339 2033.2418 1516.50257 mail Doppler SNR 3291.0501	SSIM 0.9871 0.9717 0.9671 0.9717 0.9794 0.8667 0.7944 0.9790 0.9882 0.9869 0.9871 SSIM 0.9924 0.9024	RMSE 0.0075 0.0159 0.0192 0.0101 0.0112 0.0066 0.0076 0.0076 0.0076 0.0078 0.0076 0.0076 0.0076 0.0076 0.0076	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564	SSIM 0.9834 0.9842 0.9700 0.9831 0.9763 0.9816 0.9845 0.9845 0.9833 0.9830 SSIM	RMSE 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0007 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 763.7388 743.2160 501.3694 550.7523 Epr 2 SNR 1242.776 027.074 1242.776	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.910 0.978 0.987 0.983 0.986 0.987 0.988 0.988 0.988 0.988 0.988 0.988 0.988 0.988 0.988	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001 2 0.0002 1 0.0001 2 0.0001 3 0.0012 0 0.0001 3 0.0002 7 0.0001 RMSE 9 0.0001
SWT	COIF4 Method Hard Soft Garotte Hard Hard Firm COIF4 Method Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 6 6 5 6 6 6 5 6 6 6 6 6 6 6 7 6 6 6 6	Blocks SNR 165.0189 165.0561 11.2151 74.6356 12.8957 57.2058 54.97855 54.97855 54.97855 54.97855 54.97855 5	SSIM 0.8969 0.7570 0.8468 0.7084 0.8092 0.86925 0.8393 0.9106 0.8393 0.9106 0.8393 0.9106 0.83986 0.7509 SSIM F 0.9200 0.7551 0.27651 0.	RMSE 0.1928 0.1928 0.5480 0.3408 0.8918 0.8918 0.8918 0.6477 0.3225 0.3256 0.34315 0.1932 0.5482 RMSE 1.510 0.55429 1.510	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 305.932 136.5921 8.0906 Bumps SNR 179.5064 8.6574	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6392 0.9213 0.8044 0.7067 SSIM 0.9014 0.7199	RMSE 0.0603 0.2164 0.1542 0.3083 0.0994 0.3148 0.2600 0.2820 0.2420 0.2020 RMSE 0.0534 0.2164	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1095.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1951.8110 Heavisine SNR 3586.3914 3469.7197	SSIM 0.9882 0.9886 0.9888 0.9732 0.9844 0.9639 0.9796 0.9880 0.9880 0.9887 SSIM 0.9927 0.9920	Ski RMSE 0.0711 0.0704 0.0964 0.1124 0.0662 0.01197 0.0364 0.0667 0.0670 0.0710 0.0704 Sk RMSE 0.0522 0.0530	genal Doppler SNR 1549.5580 1553.7526 338.2191 229.4200 848.5424 694.5931 225.270 8.8999 1476.0339 2033.2418 1516.7946 1516.7946 Doppler SNR 2291.0501 299.5079	SSIM 0.9871 0.9871 0.9671 0.9671 0.9811 0.9790 0.9882 0.9882 0.9882 0.9887 0.9887 0.9887	RMSE 0.0075 0.0076 0.0159 0.0192 0.0112 0.0001 0.0921 0.0076 0.0076 0.0076 RMSE 0.0051 0.0055	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564 619.3798	SSIM 0.9834 0.9842 0.9829 0.9703 0.9763 0.9831 0.9763 0.9811 0.9145 0.9816 0.9865 0.9833 0.9830 SSIM 0.9886 0.9886 0.9886	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2 SNR 1242.776 637.5076	SSIM 0.984. 0.986 0.983 0.980 0.983 0.983 0.983 0.983 0.983 0.983 0.983 0.983 0.983 0.983 0.983 0.986 0.987 0.986 SSIM 9 0.992	RMSE 2 0.0001 7 0.0002 5 0.0001 6 0.0002 8 0.0001 1 0.0002 8 0.0001 10 0.0002 10 0.0001 2 0.0001 3 0.0002 7 0.0001 RMSE 9 0.0001
SWT	COIF4 Method Hard Soft Garotte Hard Hard Firm COIF4 Method Hard Soft	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal	Level 5 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 7 7 2 2 7 6 7 7 6 7 7 7 7 7 7 7 7 7 7	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.97855 54.97855 54.97855 54.978555 54.97855555555555555	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.8692 0.8393 0.8595 0.8393 0.9106 0.8303 0.9106 0.8303 0.9106 0.8303 0.9106 0.8303 0.9106 0.8303 0.9106 0.8303 0.9106 0.8303 0.9106 0.8303 0.9106 0.9106 0.9107 0.91	RMSE 0.1928 0.5480 0.6918 0.6918 0.2828 0.4025 0.3205 0.3225 0.3205 0.3205 0.3205 0.3205 0.3205 0.3205 0.3205 0.3408 0.4315 0.1350 0.5429 0.3056	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 4.4739 305.0808 30.5932 136.5921 8.0906 Bumps SNR 179.5064 8.6574 21.0388	SSIM 0.8864 0.7147 0.8044 0.5450 0.63565 0.6044 0.6789 0.9213 0.9213 0.8044 0.8884 0.7067 SSIM 0.9014 0.7199 0.8260	RMSE 0.0603 0.2164 0.1542 0.3683 0.3683 0.2600 0.2820 0.0414 0.1238 0.0612 0.2202 RMSE 0.0534 0.2164 0.2164	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 1324.6661 1324.6651 1911.0495 1951.8110 Heavisine SNR 3586.3914 3586.3914 1533.5635	SSIM 0.9882 0.9886 0.9308 0.9732 0.9844 0.9311 0.9721 0.9684 0.9720 0.9880 0.9880 0.9887 SSIM 0.9227 0.9927 0.9927	Ski RMSE 0.0711 0.0704 0.0964 0.1124 0.0862 0.0938 0.197 0.1364 0.0863 0.0710 0.3647 0.0710 Ski RMSE 0.0522 0.0522 0.0530 0.0789 0.0789	mai Doppler SNR 1549,5580 1543,7262 338,2191 229,4200 848,5424 694,5931 225,270 8,8999 1476,0339 2033,2418 1516,7946 1516,7946 1516,7946 3291,0501 3291,0501	SSIM 0.9871 0.9871 0.9717 0.9671 0.9794 0.9790 0.9882 0.9869 0.9889 0.9887 0.9889 0.9871 SSIM 0.9924 0.9924	RMSE 0.0075 0.0076 0.0102 0.0101 0.00101 0.0001 0.0001 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0005 0.0121	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564 619.3798 644.5811	SSIM 0.9834 0.9822 0.9700 0.9700 0.9763 0.9763 0.9763 0.9811 0.9763 0.9816 0.9885 0.9833 0.9830 0.9830 0.9830 0.9886 0.9886 0.9886 0.9886	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 501.3694 Epr 2 SNR 1242.776 637.5076 758.7242	SSIM 0.984 0.986 0.983 0.980 0.983 0.983 0.983 0.983 0.983 0.983 0.983 0.986 SSIM 9 0.985 0.985	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 8 0.0001 1 0.0002 2 0.0001 3 0.00012 2 0.0001 7 0.0001 7 0.0001 7 0.0001 8 0.0002 7 0.0001 9 0.0001 1 0.0001 2 0.0001
SWT	COIF4 Method Hard Soft Garotte Hard Firm COIF4 Method Hard Soft	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal Universal	Level 5 5 6 5 5 6 5 6	Biocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 479.7317 30.7671 163.9634 18.4386 Biocks SNR SNR S 266.1629 (9.0007 (122.8888 (11.3790))	SSIM 0.8869 0.7570 0.8468 0.8468 0.7084 0.8692 0.7193 0.8395 0.8393 0.8395 0.8303 0.9106 0.8330 0.9106 0.8330 0.9106 0.8330 0.9106 0.8330 0.92000 0.92000 0.920000000000	RMSE 0.1928 0.5480 0.3408 0.6918 0.2828 0.02828 0.02828 0.0477 0.3205 0.3255 0.3255 0.3255 0.3255 0.4315 0.1351 0.5422 1.1510 0.5429 1.3056 2.06880	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 30.5932 136.5921 8.0906 Bumps SNR 179.5064 8.6574 21.0388 2.2401	SSIM 0.8864 0.7147 0.8044 0.7467 0.8565 0.6044 0.6392 0.6392 0.8384 0.7067 SSIM 0.7090 0.8384 0.7067 SSIM 0.8200 0.8251	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.2420 0.0414 0.1238 0.0612 0.2202 RMSE 0.2024 0.2202	Heavisine SNR 1918.3577 1951.9919 1925.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1951.8110 Heavisine SNR 3386.3914 3469.7197 1533.6535 1088.6471	SSIM 0.9882 0.9886 0.9808 0.9722 0.9844 0.9721 0.9684 0.9796 0.9807 0.9887 0.9880 0.9881 0.9796 0.9880 0.9881 0.9982 0.9982 0.9982 0.9982 0.9920 0.9873	Skip RMSE 0.0711 0.0704 0.0964 0.0102 0.09364 0.0107 0.1364 0.06803 0.0679 0.0710 0.1364 0.0704 Skip RMSE 0.0530 0.0530 0.0789 0.0530 0.0937	gamal Doppler SNR 1549,5580 15530,7926 382,2191 229,4200 848,5424 694,5931 22,5270 1476,0339 2033,2418 1516,7946 1505,0257 mal Doppler SNR 3291,0501 2969,5079 384,0959 38,3716	SSIM 0.9871 0.9871 0.9717 0.9671 0.9671 0.9671 0.9671 0.9794 0.9794 0.9882 0.9882 0.9882 0.9882 0.9887 0.99874 0.9924 0.9924 0.9910	RMSE 0.0075 0.0076 0.0122 0.0159 0.0122 0.0101 0.0121 0.0076 RMSE 0.0055 0.0121 0.0121	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564 619.3798 644.5811 265.2068	SSIM 0.9834 0.9829 0.9829 0.9700 0.9831 0.9763 0.9838 0.9831 0.910 0.9831 0.9833 0.9833 0.9845 0.9836 0.9838 0.98884 0.9878 0.9878	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2 SNR 1242.776 637.5076 758.7222 393.7376	SSIM 0.984 0.986 0.983 0.983 0.983 0.983 0.983 0.986 0.987 0.987 0.986 SSIM 9 0.986 0.990 0.992	RMSE 2 0.0001 7 0.0002 3 0.0012 2 0.0001 2 0.0001 3 0.0012 2 0.0001 3 0.0012 3 0.0001 RMSE RMSE 9 0.0001 2 0.0001 3 0.0002 3 0.0002
SWT	COIF4 Method Hard Soft Garotte Hard Hard Firm COIF4 Method Hard Soft	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal Universal	Level 5 5 6 5 5 6 5 6	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 479.7317 30.7671 163.9634 18.4386 SNR	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8393 0.910 0.920 0.9	RMSE 0.1928 0.5480 0.3408 0.2528 0.6418 0.2828 0.6417 0.3205 0.3205 0.3205 0.3205 0.3205 0.3205 0.3205 0.3205 0.3205 0.3205 0.1932 0.5482 0.5409 0.5429 0.2266 0.2266 0.2266 0.22	Bumps SNR 141.8517 8.6582 143.2711 2.2336 49.0371 3.3257 5.7995 305.0808 30.5932 136.5921 8.0906 Bumps SNR 179.5064 8.6574 21.0388 2.2401 59.3675	SSIM 0.8864 0.7147 0.8044 0.63865 0.6044 0.6392 0.9213 0.8044 0.7067 SSIM 0.9014 0.7199 0.8260 0.8260 0.8290 0.8290 0.8290 0.8290 0.8513 0.8514	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3148 0.2600 0.0414 0.1238 0.0612 0.2202 RMSE 0.0534 0.2164 0.1439 0.3678 0.3678 0.3678	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1229.1846 1035.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1951.8110 Heavisine SNR 3586.3914 369.7197 1533.5635 1088.6471 203.7026	SSIM 0.9882 0.9886 0.9732 0.9844 0.981 0.9732 0.9844 0.9634 0.9639 0.9688 0.9639 0.9684 0.9639 0.9927 0.9797 0.9790	Ski RMSE 0.0711 0.0701 0.0964 0.01124 0.0964 0.1124 0.0963 0.1124 0.0862 0.0370 0.0710 0.0704 Ski RMSE 0.0522 0.0530 0.0789 0.09937 0.0937	ganal Doppler SNR 1549-5580 1530.7926 338.2191 229.4200 848.5424 694.5931 22.5270 1476.0339 2033.2418 1516.7946 1505.0527 gmal Doppler SNR 3291.0501 2964.0959 338.3716 1742.3873	SSIM 0.9871 0.9871 0.9717 0.9671 0.9671 0.9671 0.9974 0.9869 0.9882 0.9882 0.9882 0.9884 0.9924 0.9924 0.9924 0.9910 0.9974	RMSE 0.0075 0.0076 0.0101 0.0159 0.0101 0.012 0.0010 0.0076 RMSE 0.0051 0.0051 0.0051 0.0051 0.0121 0.0159	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564 614.3798 644.5564 614.3798 644.5564 614.3798 761.7111	SSIM 0.9834 0.9829 0.9829 0.9700 0.9831 0.9763 0.9811 0.9455 0.9833 0.9830 0.9830 0.9830 0.9830 0.9838 0.9838 0.9886 0.9888 0.9888 0.9878 0.9783 0.9787	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 743.2160 501.3694 550.7523 Epr 2 SNR 1242.776 637.5076 758.7242 393.7376 940.2266 940.2266	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.981 0.983 0.985 0.981 0.983 0.985 0.986 SSIM 0.986 0.986 0.986 0.986 0.986 0.986	RMSE 2 0.0001 7 0.0002 5 0.0012 0 0.002 2 0.0002 2 0.0002 2 0.0002 2 0.0002 2 0.0001 3 0.0002 2 0.0001 RMSE 9 9 0.0001 2 0.0001 2 0.0001 3 0.0002
SWT	COIF4 Method Hard Soft Garotte Hard Firm COIF4 Method Hard Soft Garotte	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal Universal Universal Universal	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 6 6 6 7 7 8 6 6 6 6 7 7 8 8 8 7 8 8 8 7 8 8 8 8 8 8 8 8 8 8 8 8 8 8	Blocks SNR 165.0189 165.0189 165.0561 11.2151 74.6356 12.8957 57.2058 54.9785 479.7317 30.7671 163.9634 18.4386 SNR 2006 20.2658 11.3790 102.5536 102.5536	SSIM 0.8969 0.7570 0.7570 0.7570 0.8468 0.7084 0.8692 0.7193 0.8393 0.8393 0.9106 0.8300 0.9306 0.7094 0.8030 0.8030 0.9106 0.2000 0. 0.2001 0. 0.7651 0. 0.77144 0. 0.8958 0. 0.8958 0.	RMSE 0.1928 0.1928 0.5480 0.5480 0.3408 0.6918 0.8477 0.3205 0.3256 0.1135 0.4315 0.1932 0.5482 0.5450 0.5452 0.5510 0.5452 0.5680 0.22466 0.6880 0.24066 0.2406 6.6427	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 30.5932 136.5921 8.0906 Bumps SNR 179.5064 8.6574 21.0388 2.2401 59.3675 53.3399	SSIM 0.8864 0.7147 0.8044 0.5450 0.6044 0.6392 0.8044 0.7067 SSIM 0.8044 0.7067 SSIM 0.8044 0.7067 SSIM 0.8044 0.7057	RMSE 0.0603 0.2164 0.3164 0.342 0.3483 0.0994 0.3148 0.2600 0.2820 0.0414 0.2202 RMSE 0.0534 0.2164 0.1429 0.3678 0.3678 0.3141	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 2226.6253 1951.8110 Heavisine SNR 3586.3914 3469.7197 1533.5635 1088.471 2203.7026	SSIM 0.9882 0.9808 0.9308 0.9308 0.941 0.9732 0.9844 0.9731 0.9629 0.9638 0.9639 0.9639 0.9639 0.9634 0.9639 0.9639 0.9630 0.9880 0.9927 0.9920 0.9323 0.9977 0.9920 0.9321 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920 0.9920	Ski RMSE 0.0711 0.0704 0.0964 0.1124 0.0863 0.01124 0.0863 0.0679 0.0663 0.0710 0.0704 Ski 0.0522 0.0522 0.0530 0.0730 0.0661 0.0661 0.0730	mai Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 225.270 8.8999 1476.0339 2033.2418 1516.7946 1516.7946 1516.7946 1516.7946 302.270 mai Doppler SNR 23291.0501 23291	SSIM 0.9871 0.9717 0.9671 0.9671 0.9794 0.9671 0.9794 0.9794 0.9794 0.9821 0.9859 0.9850 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9857	RMSE 0.0076 0.0192 0.0101 0.0192 0.0101 0.0192 0.0076 0.0076 0.0076 0.0076 0.0076 0.0078 0.0078 0.0078 0.0078 0.0078 0.0071 0.0088	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 9.4665 19.7587 477.6022 Epr 1 SNR 946.5564 619.3798 644.5811 265.2068 761.7111 468.0640	SSIM 0.9834 0.9829 0.9700 0.9829 0.9700 0.9829 0.9810 0.9816 0.9846 0.9846 0.9883 0.9884 0.9884 0.9884 0.9884 0.9884	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2 SNR 1242.7766 637.5076 758.7242 393.7376 940.2266 536.7975	SSIM 0.984 0.986 0.983 0.980 0.983 0.980 0.981 0.981 0.982 0.983 0.983 0.983 0.986 0.987 0.988 0.986 0.986 0.986 0.986 0.986 0.986 0.986 0.986	RMSE 0.0001 7 0.0021
SWT	COIF4 Method Hard Soft Garotte Hard Hard COIF4 Method Hard Soft	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal Universal Universal	Level 5 5 6 5 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6	Biocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 75.2058 54.9785 479.7317 30.7671 163.9634 18.4386 SNR 2 266.1629 (19.0007 32.8888 (11.3790 (13.1446 (13.1446 (13.0444) (13.044)	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8393 0.9106 0.8393 0.9106 0.8393 0.9106 0.8393 0.9106 0.8393 0.9106 0.8030 0.9200 0.8986 0.8030 0.9200 0.8030 0.9200 0.803 0.920 0.803 0.920 0.803 0.920 0.803 0.920 0.803 0.920 0.803 0.920 0.803 0.920 0.803 0.920 0.920 0.920 0.0 0.803 0.920 0.0 0.80 0.920 0.0 0.80 0.920 0.92 0.92 0.92 0.92 0.92 0.92 0.	RMSE 0.1928 0.1928 0.5480 0.5480 0.3408 0.6918 0.2828 0.6477 0.3205 0.3256 0.3256 0.4135 0.4315 0.4315 0.4315 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5450 0.5426 0.5450 0.5426 0.5468 0.52466 0.64827 3.3166	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 30.5932 136.5921 8.0906 Bumps SNR 179.5064 8.6574 21.0388 2.2401 59.3675 3.3399 5.8083	SSIM 0.8864 0.7147 0.8044 0.5450 0.8365 0.6044 0.6789 0.6392 0.9213 0.8044 0.7067 SSIM 0.7097 0.8260 0.7199 0.8260 0.6719 0.8266	RMSE 0.0603 0.2164 0.3683 0.0994 0.3148 0.2000 0.2820 0.0414 0.2820 0.0412 0.2820 0.0414 0.1238 0.0612 0.2020 RMSE 0.0534 0.2164 0.3678 0.0900 0.3141 0.2598	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 0195.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1951.8110 Heavisine SNR 3586.3914 3469.7197 1533.5635 1088.6471 2203.7026 1806.4823 726.7183	SSIM 0.9882 0.9886 0.9732 0.9844 0.9712 0.9684 0.9712 0.9684 0.9721 0.9684 0.9721 0.9684 0.9721 0.9684 0.9726 0.9880 0.9786 0.9920 0.99	Ski RMSE 0.0711 0.0701 0.0704 0.0964 0.0863 0.1124 0.0863 0.0130 0.0663 0.0700 Ski RMSE 0.0522 0.0522 0.0530 0.0789 0.0937 0.0663 0.0730 0.0730 0.0143	gamal Doppler SNR 1549.5580 1549.5580 1530.7226 338.2191 229.4200 848.5424 694.5931 225.270 8.8999 1476.0339 2033.2418 1516.7946 1505.0257 mal Doppler SNR 3291.0501 2696.5079 584.0959 338.3716 1742.3873 1144.4846 22.6263	SSIM 0.9871 0.9671 0.9671 0.9671 0.9671 0.9671 0.9671 0.9671 0.9671 0.9671 0.9671 0.9671 0.9790 0.9821 0.9824 0.9924 0.9924 0.9924 0.9924 0.9924 0.9826 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9924 0.9826 0.9827 0.9857 0.8675	RMSE 0.0075 0.0076 0.0159 0.0101 0.012 0.0101 0.012 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0055 0.0121 0.0058 0.0071 0.0080	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564 619.3798 644.5811 265.2068 761.7111 468.0640 191.9570	SSIM 0.9834 0.9842 0.9829 0.9700 0.9811 0.9816 0.9863 0.9830 0.9830 0.9883 0.9884 0.9886 0.9884 0.9886 0.9884 0.9885	RMSE 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2 SNR 1242.776 635.5076 758.7242 393.7376 940.2266 536.7975	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.910 0.978 0.987 0.983 0.986 0.986 0.986 0.986 0.986 0.986 0.986 0.986	RMSE 2 0.0001 7 0.0002 5 0.001 7 0.0022 2 0.0012 2 0.0022 2 0.0012 2 0.0012 2 0.0011 7 0.00011 8 0.0002 7 0.00011 1 0.00012 2 0.00011 2 0.00012 3 0.00022 2 0.00011 3 0.00022 3 0.00021 2 0.00011
SWT	COIF4 Method Hard Soft Garotle Hard Hard Hard Soft Garotle Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal Universal Universal Universal Heur. SURE	Level 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 5 6 5 6 5	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 479.7317 30.7671 163.9634 18.4386 Blocks SNR 206.1629 (19.0007 (102.5536 (13.1446 (10.55.274) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.55.254) (10.555.254) (10.555.254) (10.555.254) (10.555.254) (10.555) (10.555.254) (10.555.254) (10.555.254) (10.555) (10.555.254) (10.555) (10.555) (10.555)	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8393 0.9106 0.9207	RMSE 0.1928 0.5480 0.5480 0.6918 0.6477 0.2828 0.6477 0.3256 0.3256 0.4315 0.1335 0.4315 0.13482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.5482 0.6880 1.2066 0.68427 1.21646 0.64277 1.3186 0.31866 1.3244	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 5.7995 305.0808 30.5932 136.5921 8.0906 Bumps SNR 179.5064 8.6574 2.2401 59.3675 3.3399 5.8083 4.4763	SSIM 0.8864 0.7147 0.8044 0.8545 0.6042 0.6392 0.9213 0.8044 0.7677 SSIM 0.9014 0.7920 0.8513 0.8746 0.6382 0.6392	RMSE 0.0603 0.2164 0.1542 0.3148 0.3148 0.3148 0.3148 0.0633 0.0604 0.1238 0.0612 0.20202 RMSE 0.0534 0.2164 0.3143 0.3678 0.05344 0.2598 0.3141 0.2589	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1951.8110 Heavisine SNR 3586.3914 3469.7197 1533.5635 1088.6471 2203.7026 1806.4823 726.7183 506.9860	SSIM 0.9882 0.9308 0.9372 0.9444 0.967 0.9684 0.9732 0.9844 0.9639 0.9684 0.9684 0.9684 0.9684 0.9689 0.9680 0.9880 0.9927 0.9928 0.9929 0.992	RMSE 0.0711 0.0704 0.0964 0.0964 0.0968 0.0930 0.0700 0.0704 0.0364 0.0522 0.0530 0.0704 8 RMSE 0.0522 0.0530 0.0709 0.0704 0.0522 0.0530 0.0704 0.0522 0.0530 0.0704 0.0522 0.0530 0.0704 0.0704 0.0704 0.0522 0.0530 0.0704 0.0704 0.01373	ganal Doppler SNR 1549,5580 1530,7926 382,2191 229,4200 848,5424 694,5931 22,5270 1476,0339 2033,2418 1516,7946 1505,0257 mal Doppler SNR 3291,0501 2969,5079 584,0959 383,3716 1742,3873 1144,4846 22,62633 8,9155	SSIM 0.9871 0.9971 0.9671 0.9671 0.9671 0.9790 0.9882 0.9894 0.9790 0.9882 0.9894 0.9924 0.9924 0.9924 0.9886 0.9924 0.9924 0.9886 0.9825 0.9826 0.9826 0.9827	RMSE 0.0075 0.0159 0.0192 0.0101 0.0110 0.012 0.0071 0.0075 0.0121 0.0055 0.0159 0.0159 0.0051 0.0159 0.0159 0.0051 0.0051 0.0052 0.0051 0.0051 0.0052	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564 619.3798 644.5811 265.2068 761.7111 468.0640 191.9570 9.4962	SSIM 0.9842 0.9829 0.9700 0.9829 0.9700 0.9831 0.9145 0.9845 0.9843 0.9886 0.9884 0.9886 0.9884 0.9884 0.9884 0.9884 0.9884	RMSE 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2 SNR 1242.776 637.5076 758.7242 393.7376 940.2266 536.7975 162.7804 6.9598	SSIM 0.984 0.986 0.983 0.980 0.983 0.985 0.981 0.982 0.983 0.986	RMSE 2 0.0001 7 0.0002 5 0.0012 2 0.0021 2 0.0002 3 0.0022 2 0.0012 2 0.0012 2 0.0011 7 0.0001 8 0.0022 9 0.0001 1 0.0001 2 0.0001 3 0.0002 2 0.0001 3 0.0002 3 0.0002 4 0.0014
SWT	COIF4 Method Hard Soft Garotte Hard Firm COIF4 Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal Universal Universal Heur. SURE	Level 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 6 5 5 6 7 6 8 7 6 8 7 8 8 7 8 8 7 8 8 8 8 8 8	Blocks SNR 165.0189 165.0189 165.0561 11.2151 74.6356 12.8957 57.2058 54.97855 54.97855 54.97855 54.97855 54.97855	SSIM 0.8969 0.7570 0.8468 0.7084 0.8692 0.7193 0.8595 0.8393 0.9106 0.8030 0.8030 0.8080 0.8080 0.8080 0.8080 0.8986 0.7509 0.8750 0.8750 0.8750 0.8896 0.7744 0.8895 0.7744 0.8958 0.2744 0.8958 0.27440000000000000000000000000000000000	RMSE 0.1928 0.1928 0.5480 0.5480 0.3408 0.6918 0.6918 0.2828 0.6477 0.3205 0.3256 0.1355 0.1355 0.1355 0.5482 RMSE : 0.5429 : 0.5429 : 0.3066 : 0.42406 : 0.42406 : 0.24406 : 0.3244 : 0.3244 : 0.3246 : 0.3244 : 0.4247 : 0.3244 : 0.3244 : 0.8427 : 0.3244 : 0.8427 : 0.8428 :	Bumps SNR 141.8517 145.77	SSIM 0.8864 0.7147 0.8044 0.7457 0.8044 0.5450 0.6392 0.6392 0.6392 0.9213 0.8844 0.7067 SSIM 0.9513 0.8264 0.6424 0.7067 0.8264 0.9014 0.7199 0.8263 0.6424 0.6406 0.6108 0.6846 0.6428	RMSE 0.0603 0.2164 0.1542 0.3683 0.0994 0.3620 0.2820 0.0414 0.2600 0.2820 0.0414 0.2600 0.2620 RMSE 0.0612 0.0534 0.2164 0.3678 0.3678 0.3678 0.0900 0.3141 0.2898 0.2819	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1486 1095.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1951.8110 Heavisine SNR 3586.3914 3469.7197 1533.6635 1088.6471 2203.7026 1806.4823 726.7183 506.9860 2904.2741	SSIM 0.9882 0.9808 0.9808 0.9808 0.9380 0.9381 0.9684 0.9380 0.9380 0.9380 0.9380 0.9380 0.9380 0.9380 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9387 0.9388 0.9390 0.93906 0.93906 0.93906 0.93906 0.93907 0.93906 0.93906 0.93906 0.93906 0.93907 0.93906 0.93906 0.94907	Ski 0.0711 0.0704 0.0964 0.0704 0.0964 0.1124 0.0838 0.1197 0.0338 0.1197 0.0384 0.0661 0.06522 0.0661 0.0661 0.0730 0.1143 0.3730	ganal Doppler SNR 1549.5580 1530.7926 338.2191 229.4200 848.5424 694.5931 122.5270 8.8999 1316.7946 1516.7946 1516.7946 SDR 2291.0501 2969.5079 58.0571 1742.3873 11	SSIM 0.9871 0.9871 0.9671 0.9717 0.9611 0.9794 0.9794 0.9794 0.9869 0.9869 0.9869 0.9869 0.9870 0.9824 0.9924 0.9924 0.9924 0.9924 0.9924 0.9857 0.98850 0.98857 0.98857 0.98857	RMSE 0.0075 0.0076 0.0159 0.0142 0.0061 0.0122 0.0061 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0071 0.0055 0.0121 0.0054 0.0071 0.0071 0.0071 0.0072 0.0071 0.0071 0.0072 0.0071 0.0074 0.0075 0.0071 0.0071 0.0071 0.0071 0.0071 0.0072 0.0073 0.0074	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 9.4665 9.4665 9.4665 519.7587 477.6022 Epr 1 SNR 946.5564 619.3798 644.5811 265.2668 761.7111 468.0640 191.9570 9.4962	SSIM 0.9834 0.9829 0.9700 0.9811 0.9763 0.9811 0.9145 0.9833 0.9830 0.9833 0.9830 0.9833 0.9838 0.9838 0.98844000000000000000000000000000000000	RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2 SNR 1242.776 637.5076 758.7242 393.7376 940.2266 536.7975 162.7804 6.9598 1340.329	SSIM 0.984 0.986 0.986 0.980 0.980 0.981 0.982 0.981 0.983 0.986 0.983 0.983 0.986 0.987 0.988 0.986 0.986 0.988 <td>RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 1 0.0001 2 0.0001 3 0.0012 2 0.0001 3 0.0002 7 0.0001 2 0.0001 3 0.0002 2 0.0001 3 0.0002 2 0.0001 3 0.0002 4 0.0012</td>	RMSE 2 0.0001 7 0.0002 5 0.0001 7 0.0002 1 0.0001 2 0.0001 3 0.0012 2 0.0001 3 0.0002 7 0.0001 2 0.0001 3 0.0002 2 0.0001 3 0.0002 2 0.0001 3 0.0002 4 0.0012
SWT	COIF4 Method Hard Soft Garotle Hard Firm COIF4 Method Hard Garotle Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal Universal Heur. SURE MINIMAX	Level 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 5 5 5 6 5 5 7 6 5 5 7 6 6 5 5 7 6 7 6 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	Blocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 479.7317 30.7671 163.9634 183.468 SNR 2 266.1629 (11.3790 (13.1446 58.0444 (55.5274 (13.306) (13.1446 (13.1446) (13.146) (13.16) (13.16) (13.16) (13.16) (13.16) (13.16) (13.16)	SSIM 0.8969 0.7570 0.8468 0.7684 0.7570 0.8468 0.7684 0.7193 0.8595 0.8393 0.9106 0.8393 0.9106 0.8030 0.3030 0.7590 0.8395 0.8030 0.3030 0.7561 0.3920 0.8956 0.8920 0.8920 0.0020 0.8920 0.0020 0.8920 0.0200 0.8920 0.02000 0.8920 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000 0.89200 0.02000	RMSE 0.1928 0.5480 0.3408 0.6477 0.3205 0.3256 0.3256 0.4315 0.5482 0.5482 0.51510 0.5482 0.1510 0.5482 0.3056 0.3056 0.41510 0.5482 0.5482 0.31510 0.6487 0.3244 0.3244 0.3425	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 4.4739 305.0808 30.5932 136.5921 36.594 8.0966 Bumps SNR 2.2401 59.3675 3.3399 5.8083 4.4763 397.1334 1.0022	SSIM 0.8864 0.7147 0.8044 0.5450 0.6044 0.8565 0.6044 0.8320 0.8047 0.8047 0.8320 0.9213 0.8044 0.8884 0.7067 SSIM 0.7199 0.8260 0.5131 0.6408 0.6408 0.6408 0.6404 0.6408 0.6404 0.6408 0.6408 0.6408 0.8432	RMSE 0.0603 0.2164 0.1542 0.3148 0.3148 0.3148 0.2202 0.0612 0.2202 RMSE 0.0534 0.0544 0.1449 0.3678 0.0904 0.3441 0.2598 0.3411 0.2598 0.3421	Heavisine SNR 1918.3577 1951.9919 1025.8273 758.1462 1289.1486 1095.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1911.0495 1951.8110 Heavisine SNR 3586.3914 3586.3914 3586.3914 2203.7026 1806.4823 726.7183 506.9860 2994.2724 1904.2825 1904.8423 1904.4823 1906.4825 1906.4825 1906.4856 1906.4856 1906.4856 1906.4856 1906.4856 1906.4856 1906.4	SSIM 0.9882 0.9808 0.9808 0.9808 0.9808 0.9808 0.9808 0.9811 0.9684 0.9721 0.9684 0.9796 0.9880 0.9920 0.99207 0.99206 0.99207 0.99207 0.99208 0.99209 0.99209 0.99209 0.99209 0.99209 0.99209 0.99209 0.99209 <t< td=""><td>RMSE 0.0711 0.0704 0.0964 0.0704 0.0964 0.1127 0.0302 0.0710 0.0704 Ste 0.0704 0.0710 0.0710 0.0710 0.0710 0.0710 0.0710 0.0710 0.0710 0.0710 0.0720 0.0730 0.0733 0.0730 0.0743</td><td>mai Doppler SNR 1549,5580 1543,7262 338,2191 229,4200 848,5424 694,5931 225,270 8,8999 1476,0339 2033,2418 1516,7946 746,0359 2033,2418 1516,7946 739 3291,0501 2669,5079 584,0959 338,3716 1742,3873 1144,4846 22,6263 8,9155</td><td> SSIM 0.9871 0.9871 0.9871 0.9871 0.9871 0.9744 0.9790 0.9882 0.9871 0.9871 0.9871 0.9924 0.9826 0.9826 </td><td>RMSE 0.0075 0.0076 0.0159 0.0102 0.0112 0.0071 0.0021 0.0071 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0051 0.0052 0.0088 0.0080 0.0052 0.0054</td><td>Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564 619.3798 644.5811 265.2068 761.7111 468.0640 91.9570 9.4962 1370.8620</td><td>SSIM 0.9834 0.9829 0.9700 0.9831 0.9763 0.9811 0.9816 0.9863 0.9833 0.9830 0.9884 0.9886 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9842 0.9855 0.9842 0.9855 0.9842 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9854 0.9854 0.9855 0.9854 0.9855 0.9854 0.9855 0.9854 0.98550000000000000000000000000000000000</td><td>RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001</td><td>Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 550.7523 Epr 2 SNR 1242.7766 637.5076 758.7242 393.7376 940.2266 536.7975 537.7976 536.7975 537.7975 537</td><td>SSIM 0.984 0.986 0.983 0.986 0.983 0.983 0.983 0.981 0.9100 0.978 0.983 0.983 0.983 0.986 </td><td>PMSE 2 0.0001 3 0.0012 5 0.002 3 0.0012 2 0.0022 1 0.0022 2 0.0012 2 0.0012 1 0.0001 2 0.0001 3 0.0002 5 0.0002 3 0.0002 3 0.0002 4 0.0001</td></t<>	RMSE 0.0711 0.0704 0.0964 0.0704 0.0964 0.1127 0.0302 0.0710 0.0704 Ste 0.0704 0.0710 0.0710 0.0710 0.0710 0.0710 0.0710 0.0710 0.0710 0.0710 0.0720 0.0730 0.0733 0.0730 0.0743	mai Doppler SNR 1549,5580 1543,7262 338,2191 229,4200 848,5424 694,5931 225,270 8,8999 1476,0339 2033,2418 1516,7946 746,0359 2033,2418 1516,7946 739 3291,0501 2669,5079 584,0959 338,3716 1742,3873 1144,4846 22,6263 8,9155	 SSIM 0.9871 0.9871 0.9871 0.9871 0.9871 0.9744 0.9790 0.9882 0.9871 0.9871 0.9871 0.9924 0.9826 0.9826 	RMSE 0.0075 0.0076 0.0159 0.0102 0.0112 0.0071 0.0021 0.0071 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0051 0.0052 0.0088 0.0080 0.0052 0.0054	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564 619.3798 644.5811 265.2068 761.7111 468.0640 91.9570 9.4962 1370.8620	SSIM 0.9834 0.9829 0.9700 0.9831 0.9763 0.9811 0.9816 0.9863 0.9833 0.9830 0.9884 0.9886 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9884 0.9885 0.9842 0.9855 0.9842 0.9855 0.9842 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9844 0.9855 0.9854 0.9854 0.9855 0.9854 0.9855 0.9854 0.9855 0.9854 0.98550000000000000000000000000000000000	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 550.7523 Epr 2 SNR 1242.7766 637.5076 758.7242 393.7376 940.2266 536.7975 537.7976 536.7975 537.7975 537	SSIM 0.984 0.986 0.983 0.986 0.983 0.983 0.983 0.981 0.9100 0.978 0.983 0.983 0.983 0.986	PMSE 2 0.0001 3 0.0012 5 0.002 3 0.0012 2 0.0022 1 0.0022 2 0.0012 2 0.0012 1 0.0001 2 0.0001 3 0.0002 5 0.0002 3 0.0002 3 0.0002 4 0.0001
SWT	COIF4 Method Hard Soft Garotte Hard Hard COIF4 Method Hard Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal Universal Universal Heur. SURE	Level 5 5 6 5 6 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 5 5 6 7 7 7 7	Biocks SNR 165.0189 18.5700 50.5561 11.2151 74.6356 12.8957 57.2058 54.9785 479.7317 30.7671 163.9634 18.4386 Biocks SNR S 266.1629 (19.0007 (22.8888 (11.3790 (13.1446 (55.5274 (41.7390 (11.8306 (11.836	SSIM 0.8969 0.7570 0.8468 0.7570 0.8468 0.7084 0.8692 0.8393 0.9106 0.8395 0.9106 0.8393 0.9106 0.8395 0.9106 0.8395 0.9106 0.9200 0.9.755 0.9.7755 0.9.755 0	RMSE 0.1928 0.5480 0.6481 0.6491 0.6491 0.2626 0.3205 0.3256 0.3256 0.3256 0.3256 0.3256 0.3315 0.5482 2.8486 0.5482 0.5482 0.5482 0.5486 0.5486 0.6427 0.3166 0.3244 0.0848 4.2522	Bumps SNR 141.8517 8.6582 18.2711 2.2336 49.0371 3.3257 5.7995 4.4739 305.0808 30.5932 136.5921 8.0906 Bumps SNR 179.5064 8.6574 21.0388 2.2401 59.3675 3.3399 5.8083 3.4763 397.1334 31.0093 14.0010	SSIM 0.8864 0.7147 0.8044 0.5450 0.8565 0.6044 0.6789 0.6392 0.8243 0.8884 0.7067 SSIM 0.9014 0.7199 0.5513 0.8746 0.6008 0.6896 0.6896 0.6433 0.9391 0.8120	RMSE 0.0603 0.2164 0.1542 0.3148 0.3148 0.3148 0.2202 0.0612 0.2202 RMSE 0.02164 0.2164 0.2164 0.2164 0.2164 0.2164 0.2164 0.22164 0.22164 0.22164 0.22164 0.22598 0.22598 0.22598 0.22598	Heavisine SNR 1918.3571 1951.9319 1025.8273 758.1462 1289.1846 1095.7672 663.2329 513.6680 1334.6661 2226.6253 1911.0495 1951.8110 Heavisine SNR 3586.3914 3469.7197 1203.7026 1806.4823 726.7183 2094.2741 4294.2586 2584.2586	SSIM 0.9882 0.9886 0.9732 0.9844 0.9732 0.9844 0.9732 0.9887 0.9684 0.9721 0.9880 0.9786 0.9880 0.9920 0.9820 0.9822 0.9822 0.9822 0.9922	Ski RMSE 0.0711 0.0704 0.0704 0.0704 0.0862 0.0304 0.0404 0.0404 0.0504 0.0704 Ski 0.0520 0.0504 0.0522 0.05030 0.0504 0.05030 0.0504 0.05030 0.01143 0.03703 0.03704	gynal Doppler SNR 1549,5580 1549,2580 1549,226 338,2191 229,4200 848,5424 694,5931 225,270 8,8999 1476,0339 2033,2418 1516,7946 1505,0257 mal Doppler SNR 3291,0501 2969,5079 338,3716 1742,3873 1144,4846 22,6263 3095,58261 30365,8261 3294,1020	 SSIM 0.9871 0.9871 0.9671 0.9671 0.9671 0.9790 0.9882 0.9869 0.9924 0.9924 0.9924 0.9924 0.9867 0.8675 0.7951 0.9881 0.9941 	RMSE 0.0075 0.0159 0.01010 0.0120 0.01101 0.0121 0.0076 0.0076 0.0076 0.0054 0.0055 0.0051 0.0052 0.0053 0.0054 0.0050 0.0052 0.0054 0.0054 0.0054 0.0054	Epr 1 SNR 665.2106 496.2153 528.7430 180.6361 598.9911 338.7550 189.0535 9.4665 866.0724 607.8531 519.7587 477.6022 Epr 1 SNR 946.5564 619.3798 761.7111 265.2068 761.7111 265.2068 761.7111 265.2068 761.7111 265.2068 761.7111 265.2068 761.7111 265.2068 761.7111 265.2068 761.7111 265.2078 71.7088 71.708 70.708 708	SSIM 0.9834 0.9829 0.9700 0.9829 0.9700 0.9811 0.9145 0.9846 0.9830 0.9830 0.9880 0.9884 0.9884 0.9884 0.9884 0.9884 0.9884 0.9884 0.9884 0.9884 0.9884 0.9884 0.9174	RMSE 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001	Epr 2 SNR 769.7876 515.8071 542.0270 299.7449 621.2706 460.9681 156.1583 6.9581 762.7388 743.2160 501.3694 550.7523 Epr 2 SNR 1242.776 637.5076 758.7242 393.7376 940.2266 536.7575 162.7804 140.2268 1340.328 1340.328 1243.031 1450.175	SSIM 0.984 0.986 0.983 0.983 0.981 0.981 0.982 0.983 0.983 0.986 SSIM 9.0985 0.996 0.9963 0.996 0.9962 0.986 0.9962 0.986 0.9862 0.9862 0.9862 0.9863 0.9910 0.9864 0.9862 0.9865 0.9862 0.9862 0.9862 0.9863 0.9910 0.9864 0.9862 0.9865 0.9862 0.9862 0.9862 0.9863 0.9914 0.9864 0.9862 0.9865 0.9862 0.9864 0.9862 0.9865 0.9862 0.9864 0.9864 0.9864 0.9864 0.9974 0.9868 0.9974 0.9868	RMSE 2 0.0001 7 0.0002 5 0.0012 2 0.0002 2 0.0003 3 0.0012 2 0.0001 7 0.0002 2 0.0001 7 0.0001 8 0.0002 9 0.0001 1 0.0001 2 0.0001 2 0.0001 3 0.0002 2 0.0001 3 0.0002 2 0.0001 3 0.0002 4 0.0011 4 0.0021

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Table S2. Performance of the SWT at decomposition levels 5 and 6 with the coif 4 wavelet for 6 thresholding combinations. The tables give the performance of each combination in terms of SNR, SSIM, and RMSE in order of increasing starting SNR (10, 50, 100, 200) of the noisy test signal. Results are presented for the following test signals: blocks, bumps, heavisine, doppler, 1st EPR test signal, and 2nd EPR test signal. Method refers to the thresholding form, while selection refers to the means of calculating the threshold value.

6

 18.8438
 0.7580
 0.5435
 8.1359
 0.7136
 0.2194
 3484.5952
 0.9926
 0.0530
 2811.3139
 0.9924
 0.0056
 630.7379
 0.9882
 0.0001
 733.3395
 0.9904
 0.0001

												Sig	gnal								
	COIF5	SNR=10		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
			5	34 2653	0 73/17	0.4137	26 8285	0 6003	0 1335	245 9187	0 9502	0 1977	128 7084	0 0203	0.0261	191 2331	0.0158	0.0002	203 0394	0 0115	0.0002
	Hard	Universal	6	45.0400	0.7347	0.0044	0.0200	0.0555	0.0470	075 4000	0.0002	0.1070	440.0055	0.0200	0.0201	140.0045	0.0150	0.0002	200.0001	0.0115	0.0002
			0	15.0199	0.6943	0.6044	0.4241	0.6158	0.2470	275.1030	0.9489	0.1672	116.9055	0.9216	0.0269	142.0215	0.9259	0.0002	203.5526	0.9377	0.0002
	Soft	Universal	5	24.8930	0.7107	0.4818	5.8059	0.5851	0.2575	244.0497	0.9517	0.1984	53.5512	0.8896	0.0395	160.7549	0.9165	0.0002	158.7573	0.9105	0.0003
			6	9.9325	0.6649	0.7326	1.9378	0.4627	0.3937	252.6133	0.9485	0.1945	37.0567	0.8817	0.0467	52.0234	0.9116	0.0003	79.7137	0.9203	0.0004
	Garotte	Universal	5	26.1201	0.7147	0.4708	9.9980	0.6346	0.2047	244.2450	0.9517	0.1984	78.3631	0.9044	0.0329	175.1535	0.9161	0.0002	181.1042	0.9107	0.0003
0.40	Galotte	Universal	6	10.8641	0.6732	0.7021	2.6420	0.5149	0.3488	257.4440	0.9487	0.1928	65.0523	0.9029	0.0359	94.4455	0.9207	0.0003	140.7925	0.9304	0.0003
5001			5	46.9546	0 7533	0.3544	5.5259	0 5642	0.2673	245.0180	0 9512	0.1982	21,1133	0 8401	0.0621	125.6039	0 9171	0.0002	109.2518	0 9103	0.0003
	Hard	Heur. SURE	6	47 2757	0.7765	0 3513	4 2865	0.5705	0.2890	290 4076	0.0512	0 1820	8 7356	0.0101	0.0930	9 1625	0.9657	0.0008	6 8465	0.9567	0.0012
			-	41.2101	0.7703	0.0010	4.2000	0.3793	0.2000	400.4750	0.9313	0.1020	444.0004	0.7778	0.0000	400.0004	0.8037	0.0000	400 0404	0.8307	0.0012
	Hard	MINIMAX	5	69.2139	0.7688	0.2954	60.7254	0.7438	0.0911	133.4758	0.8534	0.2826	141.6631	0.8957	0.0250	136.3864	0.8902	0.0002	133.8481	0.8825	0.0003
			6	22.7022	0.7308	0.4993	20.3301	0.7048	0.1512	193.8519	0.8764	0.2443	193.5711	0.9281	0.0213	190.3413	0.9361	0.0002	251.1743	0.9416	0.0002
	Firm	MINIMAX	5	35.2917	0.7365	0.4070	24.0394	0.6994	0.1394	248.5419	0.9468	0.1969	126.7758	0.9186	0.0261	192.3381	0.9153	0.0002	204.5309	0.9104	0.0002
			6	14.6904	0.6949	0.6094	5.7426	0.6080	0.2568	284.4572	0.9456	0.1838	121.0155	0.9214	0.0267	103.4059	0.9344	0.0003	136.0136	0.9420	0.0004
				:								Sic	nal								
	00157			Disales			D			l la avria in a		0.5	Demular			Eng 4			F== 0		
	COIFS	3NR-50		DIUCKS			Builips			neavisitie			Doppier								
	Method	Selection	Levei	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	97.2119	0.8483	0.2485	75.8932	0.8289	0.0815	904.2523	0.9767	0.1031	680.0136	0.9732	0.0113	477.4955	0.9737	0.0001	470.7685	0.9741	0.0002
			6	17.7688	0.7335	0.5605	7.4277	0.6762	0.2312	969.5799	0.9773	0.1003	669.9741	0.9749	0.0114	312.0494	0.9706	0.0001	430.7919	0.9812	0.0002
	Soft	Universal	5	38.6942	0.7994	0.3888	11.5997	0.7247	0.1891	642.5065	0.9705	0.1221	179.4286	0.9517	0.0218	378.2160	0.9733	0.0001	402.0949	0.9737	0.0002
	0011	Universal	6	10.8805	0.6908	0.7034	2.0773	0.5124	0.3808	505.0368	0.9658	0.1378	123.0495	0.9455	0.0262	108.4300	0.9546	0.0002	209.7058	0.9716	0.0002
			5	50.2765	0 8170	0.3426	26.2768	0 7861	0.1323	707.6754	0 9730	0.1165	380.3814	0 9647	0.0151	439.9448	0 9735	0.0001	444.5478	0 9739	0.0002
	Garotte	Universal	6	12 4 0 9 1	0.7012	0.6610	2 9566	0 5692	0 3312	624 6830	0.0605	0 1245	304 8056	0.0620	0.0170	202 3280	0.0612	0 0002	358 5973	0.0796	0.0002
SWT			-	55 4044	0.7012	0.0010	5.5000	0.3083	0.0012	E 40 2240	0.9093	0.1240	00-1540	0.9020	0.00170	477 0000	0.5013	0.0002	454 7020	0.9780	0.0002
	Hard	Heur. SURE	5	55.1914	0.8244	0.3209	5.5970	0.6361	0.2051	049.0010	0.9660	0.1319	22.3043	0.8613	0.0004	177.2000	0.9722	0.0002	101.7930	0.9720	0.0003
			0	53.0417	0.8170	0.3319	4.3225	0.6161	0.2073	450.5415	0.9643	0.1463	0.0400	0.7912	0.0925	9.3063	0.9018	0.0007	0.9509	0.9008	0.0012
	Hard	MINIMAX	5	219.8947	0.8658	0.1664	173.0495	0.8658	0.0545	641.7667	0.9378	0.1259	708.8202	0.9603	0.0113	505.0913	0.9703	0.0001	463.3897	0.9659	0.0002
			6	28.0883	0.7797	0.4518	24.2321	0.7673	0.1384	1042.0788	3 0.9640	0.0991	942.9292	0.9753	0.0096	451.6910	0.9791	0.0001	497.8094	0.9823	0.0002
	Firm	MINIMAX	5	93.2296	0.8477	0.2537	70.9052	0.8305	0.0839	890.7495	0.9754	0.1040	675.1045	0.9733	0.0113	441.8430	0.9734	0.0001	377.4904	0.9737	0.0002
			6	17 4738	0 7300	0.5633	6 7 5 3 6	0 6652	0 2383	0/0 1075	0.0702	0 1012	642 7466	0.0745	0.0117	214 4057	0 0704	0.0001	435.6191	0.0012	0.0002
			0	11.4100	0.7500	0.0000	0.1 000	0.0032	0.2000	545.1515	0.9763	0.1012	043.7100	0.9745	0.0117	314.4037	0.5704	0.0001		0.9013	0.0002
			0	11.4700	0.7500	0.0000	0.1000	0.0032	0.2000	545.1575	0.9763	Sig	inal	0.9745	0.0117	314.4037	0.9704	0.0001		0.3613	0.0002
	COIF5	SNR=100	0	Blocks	0.7300	0.0000	Bumps	0.0032	0.2000	Heavisine	0.9763	Sig	jnal Doppler	0.9745	0.0117	Epr 1	0.3704	0.0001	Epr 2	0.5815	0.0002
	COIF5 Method	SNR=100 Selection	Level	Blocks	SSIM	RMSE	Bumps	SSIM	RMSE	Heavisine	SSIM I	Sig	jnal Doppler SNR	SSIM	RMSE	Epr 1	SSIM	RMSE	Epr 2 SNR	SSIM	RMSE
	COIF5 Method	SNR=100 Selection	Level	Blocks SNR 138 5960	SSIM	RMSE	Bumps SNR	SSIM 0.8632	RMSE	Heavisine SNR 1833 9204	SSIM 1	Sig	043.7100 jnal Doppler SNR 1576.0468	0.9745 SSIM	RMSE	Epr 1 SNR 657 0315	SSIM	RMSE	Epr 2 SNR 770 7123	SSIM 0.9841	RMSE
	COIF5 Method Hard	SNR=100 Selection Universal	Level	Blocks SNR 138.5960	0.7300 SSIM 0.8895 0.7383	RMSE 0.2098	Bumps SNR 99.0651 7.5524	0.8632 0.8632	RMSE 0.0718	Heavisine SNR 1833.9204	0.9763 SSIM I 0.9876 0	0.1012 Sig RMSE 1 0.0728	043.7100 Jnal Doppler SNR 1576.0468 1534 1732	0.9745 SSIM 0.9872	RMSE 0.0074	Epr 1 SNR 657.0315 458 5849	0.9704 SSIM 0.9833 0.9828	RMSE 0.0001	Epr 2 SNR 770.7123	0.9813 SSIM 0.9841	RMSE
	COIF5 Method Hard	SNR=100 Selection Universal	Level	Blocks SNR 138.5960 17.6176 46.3927	SSIM 0.8895 0.7383	RMSE 0.2098 0.5618 0.3557	Bumps SNR 99.0651 7.5524 13.8861	0.8632 0.6927 0.7671	RMSE 0.0718 0.2294	Heavisine SNR 1833.9204 1845.3986	SSIM 0.9876 0.9880 0.9880	0.1012 Sig	043.7100 jnal Doppler SNR 1576.0468 1534.1732 346.0324	0.9745 SSIM 0.9872 0.9871 0.9717	RMSE 0.0074 0.0076 0.0158	Epr 1 SNR 657.0315 458.5849 512.8109	0.9704 SSIM 0.9833 0.9828	RMSE 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110	0.9813 0.9841 0.9862	RMSE 0.0001 0.0002
	COIF5 Method Hard Soft	SNR=100 Selection Universal Universal	Level 5 6 5	Blocks SNR 138.5960 17.6176 46.3927	SSIM 0.8895 0.7383 0.8398	RMSE 0.2098 0.5618 0.3557	Bumps SNR 99.0651 7.5524 13.8861	0.8632 0.8632 0.6927 0.7671	RMSE 0.0718 0.2294 0.1747	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146	0.9763 SSIM 0.9876 0.9880 0.9800 0.9800	Sig Sig SMSE 9 0.0728 0.0723 0.0979 0.1145	inal Doppler SNR 1576.0468 1534.1732 346.0324	0.9745 SSIM 0.9872 0.9871 0.9717 0.9664	RMSE 0.0074 0.0076 0.0158	Epr 1 SNR 657.0315 458.5849 512.8109	0.9704 SSIM 0.9833 0.9828 0.9827	RMSE 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110	0.9813 0.9841 0.9862 0.9833 0.9706	RMSE 0.0002 0.0002 0.0002 0.0002
	COIF5 Method Hard Soft	SNR=100 Selection Universal Universal	Level 5 6 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929	0.8895 0.7383 0.8398 0.6953	RMSE 0.2098 0.5618 0.3557 0.7052	Bumps SNR 99.0651 7.5524 13.8861 2.0960	0.8632 0.6927 0.7671 0.5299	RMSE 0.0718 0.2294 0.1747 0.3788	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146	0.9763 SSIM 0.9876 0 0.9880 0 0.9800 0 0.9725 0	0.1012 Sig 0.0728 0.0723 0.0979 0.1145	inal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804	0.9745 SSIM 0.9872 0.9871 0.9717 0.9664 0.9011	RMSE 0.0074 0.0076 0.0158 0.0192	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728	0.9704 SSIM 0.9833 0.9828 0.9827 0.9669	RMSE 0.0001 0.0001 0.0001 0.0002	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089	0.9813 0.9841 0.9862 0.9833 0.9796	RMSE 0.0001 0.0002 0.0002 0.0002
	COIF5 Method Hard Soft Garotte	SNR=100 Selection Universal Universal Universal	Level 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368	0.8632 0.6927 0.7671 0.5299 0.8261	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945	0.9763 SSIM 0 0.9876 0 0.9880 0 0.9880 0 0.9800 0 0.9836 0 0.9836 0	Sig 2.0728 0.0728 0.0723 0.0979 0.1145 0.0879 8	inal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308	0.9745 SSIM 0.9872 0.9871 0.9717 0.9664 0.9811	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419	0.9833 0.9828 0.9827 0.9669 0.9829	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429	0.9813 0.9841 0.9862 0.9833 0.9796 0.9836	RMSE 0.0001 0.0002 0.0002 0.0002 0.0001
SWT	COIF5 Method Hard Soft Garotte	SNR=100 Selection Universal Universal Universal	Level 5 6 5 6 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368 3.0027	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808	0.9763 SSIM 0.9876 0.9880 0.9800 0.9836 0.9803 0.9803 0.9803 0.9803 0.9803 0.9803 0.9803 0.9803 0.9803 0.9803 0.9803 0.9803 0.9876 0.9876 0.9880	Sig RMSE 3 0.0728 0.0728 0.0979 0.1145 0.0879 0.0963 0.0963	mal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 687.3909	SSIM 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095	0.9813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9848	RMSE 0.0002 0.0001 0.0002 0.0002 0.0002 0.0001 0.0002
SWT	COIF5 Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 6 5 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368 3.0027 5.5730	0.8632 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572	SSIM I 0.9876 0 0.9880 0 0.9800 0 0.9803 0 0.9803 0 0.9803 0 0.9803 0 0.9803 0 0.9716 0	Sig RMSE 3 0.0728 0 0.0728 0 0.0728 0 0.0729 3 0.0979 3 0.0	mal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 687.3909 22.3787	ssim 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.8658	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536	0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578	0.9813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9848 0.9809	RMSE 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0003
SWT	COIF5 Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 6 5 6 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3324	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368 3.0027 5.5730 4.2975	0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265	SSIM I 0.9876 0 0.9876 0 0.9880 0 0.9800 0 0.9725 0 0.9836 0 0.9836 0 0.9803 0 0.9716 0 0.9677 0	Sig 20.0728 0.0723	nal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 687.3909 22.3787 8.8594	SSIM 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.8658 0.7937	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603 0.0924	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9074	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0007	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554	0.9813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9848 0.9809 0.9053	RMSE 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0003 0.0012
SWT	COIF5 Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 5 6 5 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280 0.9048	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3324 0.1235	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368 3.0027 5.5730 4.2975 219.8949	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.2876	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118	SSIM I 0.9876 0 0.9880 0 0.9800 0 0.9803 0 0.9803 0 0.9803 0 0.9803 0 0.9803 0 0.9803 0 0.9803 0 0.9677 0 0.9636 0	Sig 20.0728 0.0723	1043.7100 inal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 1481.9069	SSIM 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.8658 0.7937 0.9782	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603 0.0924 0.0078	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9074 0.9816	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0007 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529	SSIM 0.9841 0.9862 0.9833 0.9796 0.9836 0.9848 0.9809 0.9053 0.9779	RMSE 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0003 0.0012 0.0001
SWT	COIF5 Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280 0.9048 0.9048 0.7883	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3324 0.1235 0.4546	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.2876 0.0485 0.1343	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845	SSIM I 0.9876 0 0.9880 0 0.9800 0 0.9800 0 0.9800 0 0.9800 0 0.9803 0 0.9803 0 0.9803 0 0.9803 0 0.9716 0 0.9636 0 0.9763 0	Sig RMSE 3 0.0728 0.0723 0.0723 0.0773 0.0773 0.0773 0.0773 0.0879 0.0867 0.0867 0.0867	043.7100 jnal Doppler SNR 1576.0468 1534.1732 346.0324 283.804 865.2308 887.3909 22.3787 8.8594 1481.9069 2074.5236	SSIM 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.8658 0.7937 0.9782 0.9885	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603 0.0924 0.0078 0.0065	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 593.1300	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9074 0.9816 0.9861	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0007 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125	5.9813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9848 0.9809 0.9053 0.9779 0.9874	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001
SWT	COIF5 Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 5 6 5 5 6 5 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555 137.6594	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280 0.9048 0.7883 0.8909	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3224 0.1235 0.4546 0.2107	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.8654	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.2876 0.0485 0.1343 0.0736	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230	SSIM I 0.9876 0 0.9880 0 0.9800 0 0.9800 0 0.9800 0 0.9800 0 0.9803 0 0.9803 0 0.9803 0 0.9803 0 0.9705 0 0.9636 0 0.9763 0 0.9764 0 0.9876 0	Sig RMSE 3 0.0728 0.0723 0.0723 0.0723 0.0979 0.0879 0.0867 0.0867 0.0867 0.0681 0.0681 0.0725	043.7100 jnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 1481.9069 2074.5236 1533.4767	SSIM 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.8658 0.7937 0.9782 0.9885 0.9885	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603 0.0924 0.0078 0.0065 0.0075	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 588.1419 300.7501 189.7503 9.3197 859.7482 593.1300 532.0710	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9074 0.9809 0.9074 0.9816 0.9831	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195	SSIM 0.9841 0.9862 0.9833 0.9796 0.9836 0.9848 0.9809 0.9053 0.9779 0.9874 0.9836	RMSE 0.0001 0.0002 0.0002 0.0002 0.0001 0.0002 0.0003 0.0012 0.0001 0.0001 0.0002
SWT	COIF5 Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555 137.6594 17.2810	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280 0.9048 0.7883 0.8909 0.7346	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3224 0.1235 0.4546 0.2107 0.5653	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.8654 0.8654 0.6822	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.0485 0.1343 0.0736 0.2356	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 1325.9118 1332.7230 1842.4255	SSIM I 0.9876 0 0.9880 0 0.9880 0 0.9725 0 0.9836 0 0.9836 0 0.9836 0 0.9716 0 0.9677 0 0.9636 0 0.9796 0 0.9881 0	Sig SMSE 9 0.0728 0.0728 0.0723 0.0979 0.0963 0.0867 0.0867 0.0867 0.0867 0.0867 0.0867 0.0725 0.0724	043.7100 jnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 1481.9069 2074.5236 153.4767 1489.8284	SSIM 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.8658 0.7937 0.9782 0.9885 0.9885 0.9869 0.9871	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603 0.0924 0.0078 0.0075 0.0077	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9074 0.9816 0.9861 0.9831 0.9831	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0007 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472	0.9813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9848 0.9809 0.9053 0.9779 0.9874 0.9836 0.9884	RMSE 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0003 0.0012 0.0001 0.0001 0.0002 0.0002
SWT	COIF5 Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555 137.6594 17.2810	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280 0.9048 0.7083 0.9048 0.7883 0.9048 0.7346	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3224 0.1235 0.4546 0.2107 0.5653	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.7850 0.8654 0.6822	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.0485 0.1343 0.0736 0.2356	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255	SSIM I 0.9876 0 0.9876 0 0.9880 0 0.9725 0 0.9836 0 0.9725 0 0.9836 0 0.9716 0 0.9636 0 0.97636 0 0.9636 0 0.97636 0 0.9881 0	Sig 2010728 0.0728 0.0723 0.0723 0.0979 0.0963 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09724 0.09725 0.09725 0.09724 0.09725 0.09725 0.09725 0.09724 0.09725 0.097555 0.097555 0.09755 0.09755 0.09755 0.097555 0.097555 0.	043.7160 ipnal Doppler DSNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 867.3909 22.3787 8.8594 1481.9069 2074.5236 1533.4767 1489.8284 mal	SSIM 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.8658 0.7937 0.9782 0.9885 0.9885 0.9889 0.9871	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603 0.0924 0.0078 0.0075 0.0077	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9074 0.9816 0.9861 0.9831 0.9821	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0007 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 617.0429 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472	5.9813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9836 0.9809 0.9053 0.9779 0.9874 0.9856 0.9864	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002
SWT	COIF5 Method Hard Soft Garotte Hard Hard Firm	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 52.6838 405.9475 27.6555 137.6594 17.2810 Blocks	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280 0.9048 0.7883 0.8909 0.7346	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.324 0.1235 0.4546 0.2107 0.5653	Bumps SNR 99.0651 7.5524 13.8861 2.0960 33.7368 3.0027 219.8949 25.7596 93.9431 6.9172 Bumps	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.8654 0.6822	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.0485 0.1343 0.0736 0.2356	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine	SSIM I 0.9876 0 0.9880 0 0.9880 0 0.9836 0 0.9803 0 0.9803 0 0.9876 0 0.9836 0 0.9803 0 0.9636 0 0.9636 0 0.9876 0 0.9881 0	Sig Sig Sig Sig Sig Sig Sig Sig	043.7160 ipnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 223.3787 8.8594 1481.9069 2074.5236 1533.4767 1489.8284 ijnal Doobeler	SSIM 0.9872 0.9871 0.9717 0.9664 0.9788 0.9788 0.9788 0.9782 0.9855 0.9869 0.9871	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603 0.0924 0.0078 0.0075 0.0077	Epr 1 SNR 657.0315 458.5849 512.8109 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9074 0.9816 0.9831 0.9821	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2	SSIM 0.9841 0.9862 0.9833 0.9796 0.9836 0.9848 0.9809 0.9053 0.9779 0.9874 0.9836 0.9886	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0012 0.0001 0.0001 0.0002 0.0002
SWT	COIF5 Method Hard Soft Garotte Hard Hard Firm COIF5 Method	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection	Level 5 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 52.6838 405.9475 27.6555 137.6594 17.2810 Blocks SNR	ssim 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280 0.9048 0.7883 0.8909 0.7346	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3224 0.1235 0.4546 0.2107 0.5653 RMSE	Bumps SNR 99.0651 7.5524 13.8661 2.0960 33.7368 3.0027 2.5.730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.8654 0.6822	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.0485 0.1343 0.0736 0.2356 RMSE	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine SNR	SSIM I 0.9876 0 0.9880 0 0.9880 0 0.9836 0 0.9836 0 0.9836 0 0.9806 0 0.9806 0 0.9806 0 0.9876 0 0.9636 0 0.9876 0 0.9881 0 SSIM 0	Signature (Construction) (Constructi	043.7160 inal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 687.3909 22.3787 8.8594 1481.9069 1481.9069 1481.9069 1489.8284 inal Doppler SNR	 SSIM 0.9872 0.9871 0.9664 0.9718 0.8658 0.7937 0.9782 0.9885 0.9869 0.9871 SSIM 	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603 0.0924 0.0078 0.0075 0.0077 RMSE	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 533.1300 532.0710 445.4389 Epr 1 SNR	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9074 0.9816 0.9831 0.9831 0.9821 SSIM	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 RMSE	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR	0.9813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9848 0.9809 0.9053 0.9779 0.9874 0.9836 0.9884 SSIM	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0002 0.0002 0.0002 0.0002
SWT	COIF5 Method Hard Soft Garotte Hard Hard Firm COIF5 Method	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection	Level 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 52.6838 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155	551M 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8280 0.8280 0.9048 0.8280 0.9048 0.7883 0.8909 0.7346	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.324 0.1235 0.4546 0.2107 0.5653 RMSE 0.1700	Bumps SNR 99.0651 7.5524 13.8861 2.0960 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.6823 0.6610 0.6283 0.9016 0.7850 0.8654 0.6822 SSIM 0.8790	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.0485 0.1343 0.0736 0.2356 RMSE 0.0672	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 2179.5845 1322.7230 1842.4255 Heavisine SNR	SSIM I 0.9876 0 0.9880 0 0.9800 0 0.9836 0 0.9836 0 0.9836 0 0.9836 0 0.9715 0 0.9836 0 0.9716 0 0.9636 0 0.9636 0 0.9636 0 0.9881 0 SSIM 0	Sig Sig Sig Sig Sig Sig Sig Sig	043,7160 jnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 1481.9069 2074.5236 1533.4767 1489.8284 jnal Doppler SNR	SSIM 0.9872 0.9871 0.964 0.9811 0.9788 0.8658 0.7937 0.9782 0.9885 0.9869 0.9871 SSIM 0.9925	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0603 0.0924 0.0078 0.0075 0.0077 RMSE 0.0051	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 593.1300 455.4829 Epr 1 SNR Epr 1 SNR 9.3197 859.7482 593.1300 455.4839 Epr 1 SNR 9.3197 859.7482 532.0710 445.4389 Epr 1 SNR 9.386651	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9074 0.9816 0.9831 0.9831 0.9821 SSIM	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 448.1095 157.1578 6.9554 757.7529 719.1125 535.7472 Epr 2 SNR 1225.7255	0.9813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9888 0.9809 0.9053 0.9779 0.9874 0.9874 0.9886 0.9864 SSIM	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0002 0.0002 RMSE 0.0001
SWT	COIF5 Method Hard Soft Garotte Hard Hard Firm COIF5 Method Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal	Level 5 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6338 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155 17.6176 17.8176 17.8176 17.8176 17.8176 17.6555 17.6554 17.6554 17.2810 20.62155 17.7855 17.7855 17.78554 17.7857474 17.78574 17.78574 17.78574 17.78574	551M 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280 0.9048 0.90	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3245 0.1235 0.4546 0.2107 0.5653 RMSE 0.17000 0.5787	Bumps SNR 99.0651 7.5524 13.8661 2.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.9016 0.7850 0.8654 0.6822 SSIM 0.8770	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.0485 0.1343 0.0736 0.2356 RMSE 0.0672 0.2307	Heavisine SNR 1833,9204 1845,3986 994,1497 730,2146 1237,5945 1039,2808 658,1572 493,7265 1325,9118 2179,5845 1322,7230 1842,4255 Heavisine SNR 3365,2407 3365,2407 3240,7524	SSIM I 0.9876 0 0.9880 0 0.9880 0 0.9725 0 0.9716 0 0.9836 0 0.9766 0 0.9776 0 0.9636 0 0.9766 0 0.9831 0 0.9881 0 0.9881 0 0.9821 0	Signed States St	043.7160 inal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 88594 1481.9069 2074.5236 1533.4767 1489.8284 inal Doppler SNR 3348.3633 3304.2408	0.9745 SSIM 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.9788 0.9783 0.9783 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9925 0.9025	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0063 0.0075 0.0075 0.0077 RMSE 0.0051 0.0051	Epr 1 SNR 657.0315 458.5849 512.8109 512.8109 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.6280	SSIM 0.9833 0.9828 0.9827 0.9669 0.9829 0.9745 0.9809 0.9816 0.9861 0.9881 0.9881 0.9821 SSIM 0.9888 0.9878	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 522.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 615.6406	0.9813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9836 0.9848 0.9053 0.9073 0.9874 0.9886 0.98864 0.98864 0.98899 0.98999	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0011 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001
SWT	COIF5 Method Hard Soft Garotte Hard Hard Firm COIF5 Method Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155 17.8817 25.6994 17.2817 26.9944 208.2155 17.817 26.9944 208.2155 208.21	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8549 0.8280 0.9048 0.7088 0.9048 0.7883 0.8909 0.7346 SSIM 0.9134 0.9134 0.92617	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3240 0.4546 0.2107 0.5653 RMSE 0.1705 0.3240 0.5567	Bumps SNR 99.0651 7.5524 13.8861 3.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.6240	SSIM 0.8632 0.6927 0.7671 0.5857 0.6610 0.5857 0.6610 0.6283 0.9016 0.7850 0.8654 0.6822 SSIM 0.8790 0.6972 0.7850	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.26326 0.2486 0.0485 0.03356 RMSE 0.0672 0.2356	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6710	SSIM I 0.9876 0 0.9800 0 0.9800 0 0.9800 0 0.9836 0 0.9836 0 0.9836 0 0.9836 0 0.9716 0 0.9636 0 0.9766 0 0.9881 0 SSIM 0 0.9921 0 0.9921 0	Signature 2 Signat	043,7160 ipnal Doppler SNR 1576,0468 1534,1732 346,0324 228,3804 865,2308 88794 1481,9069 2074,5236 1533,4767 1488,8284 ipnal Dopper SNR 3348,3633 3001,9109 202,2157	SSIM 0.9872 0.9871 0.9717 0.9664 0.9782 0.9783 0.9782 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9871 SSIM 0.9925 0.9925 0.9825	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0665 0.0077 RMSE 0.0051 0.0051 0.0110	Epr 1 SNR 657.0315 458.5849 512.8109 512.8109 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 638.615 578.5280	SSIM 0.9833 0.9828 0.9827 0.9669 0.9745 0.9809 0.9744 0.9816 0.9861 0.9861 0.9881 0.9821 SSIM 0.9821	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 75.0259	5.5813 0.9841 0.9862 0.9833 0.9796 0.9836 0.9836 0.9809 0.9053 0.9779 0.9874 0.9836 0.9864 5.51M 0.9899 0.9899	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 RMSE 0.0001 0.0001 0.0001 0.0001
SWT	COIF5 Method Hard Soft Garotte Hard Firm COIF5 Method Hard Soft	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal	Level 5 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155 17.8817 55.8884 10.0279	SSIM 0.8895 0.7383 0.8398 0.8393 0.6953 0.8608 0.7059 0.8280 0.9048 0.7383 0.8909 0.7346 SSIM 0.9134 0.7459 0.8134 0.7459	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.3007 0.3265 0.3244 0.2107 0.5653 RMSE 0.1700 0.5687 0.3284 0.3265	Bumps SNR 99.0651 7.5524 13.8661 3.0027 5.5730 4.2975 219.8949 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0000	SSIM 0.8632 0.8632 0.6927 0.7671 0.5297 0.8261 0.5857 0.6610 0.6833 0.9016 0.7850 0.8654 0.68624 SSIM 0.8694 0.8790 0.6972 0.7859 0.7859	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.0485 0.1343 0.0736 0.2356 RMSE	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6719	SSIM I 0.9876 0 0.9800 0 0.9800 0 0.9725 0 0.9836 0 0.9803 0 0.9803 0 0.9716 0 0.9636 0 0.9636 0 0.9636 0 0.9716 0 0.9636 0 0.9876 0 0.9881 0 SSIM 0 0.9921 0 0.9827 0 0.9827 0	Single Control (Control (Contro) (Contro) (Contro) (Contro) (Contro) (Contro) (Contro) (Contr	043.7160 inal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 228.3804 228.3804 228.3804 228.3804 228.3804 223.787 8.8594 1481.9069 22.3787 8.8594 1481.9069 1489.8284 inal Doppler SNR 3348.3633 3001.9109 503.1572 347.2005	SSIM 0.9872 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.9885 0.9372 0.9885 0.9885 0.9885 0.93871 SSIM 0.9255 0.9925 0.9312	RMSE 0.0074 0.0076 0.0175 0.0192 0.0100 0.0112 0.0603 0.0603 0.0074 0.0005 0.0075 RMSE 0.0051 0.0054 0.0154 0.0154	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 509.1419 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 598.0227	SSIM 0.9833 0.9828 0.9828 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9809 0.9809 0.9804 0.9816 0.9821 0.9821 SSIM 0.9885 0.9878 0.9877	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 737.2026	SSIM 0.9841 0.9862 0.9833 0.9796 0.9838 0.9836 0.9836 0.9836 0.9836 0.9838 0.9809 0.9830 0.9899 0.9899 0.9899 0.9899	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0002 0.0003 0.0004 0.0005 0.0006 0.0007 0.0008 RMSE 0.0001 0.0001
SWT	COIFS Method Hard Soft Garotte Hard Firm COIFS Method Hard Soft	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 10.7929 12.2687 55.0778 52.6638 405.9475 17.6555 137.6594 17.2810 Blocks SNR 208.2155	SSIM 0.8895 0.7383 0.8398 0.6953 0.8508 0.7059 0.8508 0.7059 0.8800 0.9048 0.7833 0.7833 0.7833 0.7346 SSIM 0.9134 0.9134 0.73459	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3245 0.3265 0.3246 0.2107 0.5653 RMSE 0.4546 0.2107 0.5653 RMSE 0.1230 0.5587 0.3239 0.7024 0.7204	Bumps SNR 99.0651 7.5524 13.8861 2.0960 3.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909	SSIM 0.8632 0.6927 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.8654 0.8854 0.8652 SSIM 0.8654 0.8790 0.8670 0.8790 0.7859 0.7859 0.5351	RMSE 0.0718 0.2294 0.1747 0.3788 0.184 0.3287 0.2652 0.2652 0.2652 0.2652 0.2656 0.3287 0.3287 0.3287 0.3256 RMSE 0.0652 0.2307 0.1676 0.3792	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1322.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6719 1021.0333	SSIM I 0.9876 0 0.9880 0 0.9800 0 0.9725 0 0.9836 0 0.9803 0 0.9836 0 0.9836 0 0.9836 0 0.9836 0 0.9677 0 0.9676 0 0.9876 0 0.9881 0 SSIM 0 0.9921 0 0.9924 0 0.9876 0 0.9785 0	Single Control (Control (Contro) (Control (Contro) (Contro) (Contro) (Contro) (Contro) (Contr	043.7160 jnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 867.3909 22.3787 8.8594 1481.9069 2074.5236 1533.4767 1489.8284 jnal Doppler SNR 3348.3633 3001.9109 503.1572 347.0005	SSIM 0.9872 0.9872 0.9871 0.970 0.9664 0.9811 0.9788 0.9864 0.9811 0.9782 0.9871 0.9858 0.9871 0.9859 0.9871 0.9852 0.9871 0.9925 0.9925 0.9925 0.9921	RMSE 0.0074 0.0076 0.0192 0.0192 0.0192 0.0192 0.0192 0.0400 0.012 0.051 0.0051 0.0054 0.019 0.017	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 593.1300 455.3489 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387	SSIM 0.9833 0.9828 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9809 0.9745 0.9809 0.9745 0.9816 0.9881 0.9821 0.9851 0.9821 0.9851 0.9828 0.9878 0.98878 0.9877 0.9759 0.9759	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 632.5089 617.0429 448.1095 157.1578 6.9554 757.7529 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889	SSIM 0.9841 0.9841 0.9841 0.9862 0.9836 0.9796 0.9836 0.9848 0.9809 0.9848 0.9809 0.9874 0.9864 0.9864 0.9864 0.9864 0.9899 0.9899 0.9899 0.9899 0.9899 0.9899	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0001 0.0001 0.0001 0.0002
SWT	COIFS Method Hard Soft Garotte Hard Hard Firm COIFS Method Hard Soft Garotte	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal	Level 5 6	Blocks SNR 138.5960 17.6176 46.3927 46.3927 12.2687 55.0778 52.6338 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155 17.8817 55.58884 10.9178 86.2422	SSIM 0.8895 0.7383 0.8398 0.8398 0.86953 0.8608 0.7559 0.8549 0.8280 0.9048 0.7383 0.8309 0.7346 SSIM 0.9134 <td>RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3244 0.1235 0.4546 0.2107 0.5653 RMSE 0.3239 0.7524 0.2329</td> <td>Bumps SNR 99.0651 7.5524 13.8661 2.0960 33.7368 3.0027 5.5730 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844</td> <td>SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5289 0.6820 0.610 0.6830 0.9016 0.7850 0.8364 0.8790 0.6379 0.67859 0.7859 0.7859 0.7859 0.6970 0.6351 0.8361 0.7859</td> <td>RMSE 0.0718 0.0294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.1433 0.0356 0.3433 0.0356 0.2356 RMSE 0.0672 0.0676 0.2307 0.1676 0.3792 0.1141 0.3207</td> <td>Heavisine SNR 1835,39204 1845,3986 994,1497 730,2146 1237,5945 1039,2808 658,1572 493,7265 1325,9118 2179,5845 1832,7230 1842,4255 Heavisine SNR 3365,2407 3210,7574 1476,6719 1021,0333 2096,9345</td> <td>SSIM 0.9876 0.9876 0.9876 0.9800 0.9800 0.9725 0.9836 0.9726 0.9803 0.9726 0.9803 0.9726 0.9803 0.9767 0.9636 0.9636 0.9636 0.96376 0.96376 0.9887 0.9887 SSIM 0.9921 0.9887 0.9921 0.9785 0.9785 0.9786 0.9786</td> <td>Signa Control 2 Signa Control</td> <td>043.7160 gnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 228.3804 885.94 885.94 1481.9069 2074.5236 1533.4767 1489.8284 gnal Doppler SNR 3348.3633 3001.9109 303.1572 347.0005 1794.9305 1794.9316</td> <td>SSIM 0.9872 0.9872 0.9871 0.9707 0.9664 0.9684 0.9684 0.9788 0.9685 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9982 0.9885 0.9925 0.9925 0.9921 0.9925 0.9931 0.9753 0.9753 0.9753</td> <td>RMSE 0.0074 0.0076 0.0158 0.0192 0.0192 0.0192 0.0400 0.012 0.053 0.0924 0.0075 0.0075 0.0075 0.0077 RMSE 0.0054 0.0119 0.0156 0.0070</td> <td>Epr 1 SNR 657.0315 458.5849 512.8109 512.8109 300.7501 189.7565 9.3197 659.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304</td> <td>SSIM 0.9833 0.9828 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9821 0.9831 0.9831 0.9828 0.9837 0.9878 0.9877 0.9875 0.9878 0.9878 0.9878</td> <td>RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001</td> <td>Epr 2 SNR 770.7123 501.2712 522.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162</td> <td>SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9836 0.9898 0.9803 0.9854 0.9889 0.9889 0.9889 0.9889 0.9895</td> <td>RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002</td>	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3244 0.1235 0.4546 0.2107 0.5653 RMSE 0.3239 0.7524 0.2329	Bumps SNR 99.0651 7.5524 13.8661 2.0960 33.7368 3.0027 5.5730 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844	SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5289 0.6820 0.610 0.6830 0.9016 0.7850 0.8364 0.8790 0.6379 0.67859 0.7859 0.7859 0.7859 0.6970 0.6351 0.8361 0.7859	RMSE 0.0718 0.0294 0.1747 0.3788 0.1184 0.3287 0.2652 0.2876 0.1433 0.0356 0.3433 0.0356 0.2356 RMSE 0.0672 0.0676 0.2307 0.1676 0.3792 0.1141 0.3207	Heavisine SNR 1835,39204 1845,3986 994,1497 730,2146 1237,5945 1039,2808 658,1572 493,7265 1325,9118 2179,5845 1832,7230 1842,4255 Heavisine SNR 3365,2407 3210,7574 1476,6719 1021,0333 2096,9345	SSIM 0.9876 0.9876 0.9876 0.9800 0.9800 0.9725 0.9836 0.9726 0.9803 0.9726 0.9803 0.9726 0.9803 0.9767 0.9636 0.9636 0.9636 0.96376 0.96376 0.9887 0.9887 SSIM 0.9921 0.9887 0.9921 0.9785 0.9785 0.9786 0.9786	Signa Control 2 Signa Control	043.7160 gnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 228.3804 885.94 885.94 1481.9069 2074.5236 1533.4767 1489.8284 gnal Doppler SNR 3348.3633 3001.9109 303.1572 347.0005 1794.9305 1794.9316	SSIM 0.9872 0.9872 0.9871 0.9707 0.9664 0.9684 0.9684 0.9788 0.9685 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9982 0.9885 0.9925 0.9925 0.9921 0.9925 0.9931 0.9753 0.9753 0.9753	RMSE 0.0074 0.0076 0.0158 0.0192 0.0192 0.0192 0.0400 0.012 0.053 0.0924 0.0075 0.0075 0.0075 0.0077 RMSE 0.0054 0.0119 0.0156 0.0070	Epr 1 SNR 657.0315 458.5849 512.8109 512.8109 300.7501 189.7565 9.3197 659.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304	SSIM 0.9833 0.9828 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9829 0.9821 0.9831 0.9831 0.9828 0.9837 0.9878 0.9877 0.9875 0.9878 0.9878 0.9878	RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001	Epr 2 SNR 770.7123 501.2712 522.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162	SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9836 0.9898 0.9803 0.9854 0.9889 0.9889 0.9889 0.9889 0.9895	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002
SWT	COIFS Method Hard Soft Garotte Hard Firm COIFS Method Hard Soft Garotte	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal	Level 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155 17.8117 55.8884 10.9178 86.2422 12.4543	SSIM 0.8895 0.7383 0.8398 0.8398 0.8398 0.8539 0.8649 0.7059 0.8549 0.8280 0.9048 <td>RMSE 0.2098 0.5618 0.3557 0.3007 0.6636 0.3242 0.1235 0.4546 0.2107 0.5653 RMSE 0.1700 0.5887 0.3704 0.2107 0.3244 0.1700 0.5553</td> <td>Bumps SNR 99.0651 7.5524 13.8661 3.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844 2.9911</td> <td>SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.9654 0.6622 SSIM 0.6872 0.7850 0.7850 0.5351 0.5351</td> <td>RMSE 0.0718 0.2294 0.1747 0.3788 0.1344 0.3287 0.2652 0.2876 0.0485 0.0485 0.03356 RMSE 0.0672 0.2356 0.1676 0.3792 0.1114</td> <td>Heavisine SNR 1833.9204 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6719 1021.0333 2096.9345 1658.1665</td> <td>SSIM I 0.9876 0 0.9806 0 0.9800 0 0.9803 0 0.9725 0 0.9836 0 0.9767 0 0.9636 0 0.9766 0 0.9767 0 0.9676 0 0.9786 0 0.9881 0 SSIM 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9986 0</td> <td>Signal Constraints of the second seco</td> <td>043,7160 ipnal Doppler SNR 1576,0468 1534,1732 346,0324 228,3804 865,2308 88794 1655,2308 88794 1633,4767 1488,8284 ipnal Doppler SNR 3348,3633 3001,9109 603,1572 347,0005 1794,9318 1173,6201</td> <td>SSIM 0.9872 0.9872 0.9871 0.9707 0.9664 0.9685 0.9685 0.9788 0.9782 0.9885 0.9382 0.9825 0.9825 0.98857 0.9885</td> <td>RMSE 0.0074 0.0074 0.0076 0.0158 0.0192 0.0100 0.0192 0.0070 0.0078 0.0075 0.0075 0.0075 0.0077 RMSE 0.0051 0.0054 0.0156 0.0156 0.0176 0.0156 0.0175</td> <td>Epr 1 SNR 657.0315 458.5849 512.8109 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774</td> <td>SSIM O.9833 O.9823 O.9827 O.9829 O.9829 O.9829 O.9829 O.9829 O.9840 O.9840 O.9841 O.9881 O.9881 O.9885 O.9878 O.98820 O.9820 <tho.9820< th=""> <!--</td--><td>RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001</td><td>Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939</td><td>SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9838 0.9894 0.9853 0.9874 0.9874 0.9874 0.9874 0.9879 0.9874 0.9899 0.9899 0.9895 0.9889 0.9855 0.9888</td><td>RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0002</td></tho.9820<></td>	RMSE 0.2098 0.5618 0.3557 0.3007 0.6636 0.3242 0.1235 0.4546 0.2107 0.5653 RMSE 0.1700 0.5887 0.3704 0.2107 0.3244 0.1700 0.5553	Bumps SNR 99.0651 7.5524 13.8661 3.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844 2.9911	SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.9654 0.6622 SSIM 0.6872 0.7850 0.7850 0.5351 0.5351	RMSE 0.0718 0.2294 0.1747 0.3788 0.1344 0.3287 0.2652 0.2876 0.0485 0.0485 0.03356 RMSE 0.0672 0.2356 0.1676 0.3792 0.1114	Heavisine SNR 1833.9204 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6719 1021.0333 2096.9345 1658.1665	SSIM I 0.9876 0 0.9806 0 0.9800 0 0.9803 0 0.9725 0 0.9836 0 0.9767 0 0.9636 0 0.9766 0 0.9767 0 0.9676 0 0.9786 0 0.9881 0 SSIM 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9986 0	Signal Constraints of the second seco	043,7160 ipnal Doppler SNR 1576,0468 1534,1732 346,0324 228,3804 865,2308 88794 1655,2308 88794 1633,4767 1488,8284 ipnal Doppler SNR 3348,3633 3001,9109 603,1572 347,0005 1794,9318 1173,6201	SSIM 0.9872 0.9872 0.9871 0.9707 0.9664 0.9685 0.9685 0.9788 0.9782 0.9885 0.9382 0.9825 0.9825 0.98857 0.9885	RMSE 0.0074 0.0074 0.0076 0.0158 0.0192 0.0100 0.0192 0.0070 0.0078 0.0075 0.0075 0.0075 0.0077 RMSE 0.0051 0.0054 0.0156 0.0156 0.0176 0.0156 0.0175	Epr 1 SNR 657.0315 458.5849 512.8109 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774	SSIM O.9833 O.9823 O.9827 O.9829 O.9829 O.9829 O.9829 O.9829 O.9840 O.9840 O.9841 O.9881 O.9881 O.9885 O.9878 O.98820 O.9820 O.9820 <tho.9820< th=""> <!--</td--><td>RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001</td><td>Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939</td><td>SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9838 0.9894 0.9853 0.9874 0.9874 0.9874 0.9874 0.9879 0.9874 0.9899 0.9899 0.9895 0.9889 0.9855 0.9888</td><td>RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0002</td></tho.9820<>	RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939	SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9838 0.9894 0.9853 0.9874 0.9874 0.9874 0.9874 0.9879 0.9874 0.9899 0.9899 0.9895 0.9889 0.9855 0.9888	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0002
SWT	COIFS Method Hard Soft Garotte Hard Firm COIFS Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155 17.8817 55.8884 10.9178 86.2422 12.4543 55.9466	SSIM 0.8895 0.7883 0.8398 0.8095 0.7833 0.8608 0.7059 0.8640 0.9048 0.9048 0.9048 0.9048 0.9048 0.7833 0.88909 0.7346 0.7833 0.8909 0.7346 0.9134 0.7459 0.8617 0.7616 0.8859 0.7122 0.8650 0.7122 0.8620 0.7422 0.8620 0.9144 0.9144 0.9144 0.9144 0.9144 0.9144 0.9144 0.9144 0.9144 0.9144 0.9144 0.7122 0.8650 0.9122 0.8650 0.9122 0.8650 0.9122 0.8650 0.9122 0.8650 0.9122 0.8650 0.9122 0.8650 0.9122 0.8650 0.9122 0.8650 0.9122 0.8650 0.9122 0.8650 0.9122 </td <td>RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3264 0.3244 0.1235 0.4546 0.1230 0.4546 0.1230 0.5653 RMSE 0.1700 0.5587 0.3244</td> <td>Bumps SNR 99.0651 7.5524 13.8661 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844 2.9911 5.6148</td> <td>SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.7850 0.8654 0.6822 0.8654 0.6872 0.7850 0.8654 0.6792 0.7850 0.8790 0.5351 0.8431 0.8431 0.8431 0.5910 0.5718 0.5910 0.5718 0.5910 0.5911 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.591</td> <td>RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2876 0.0485 0.04650000000000000000000000000000000000</td> <td>Heavisine SNR 1833.9204 1843.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 1232.59118 1832.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6719 1021.0333 2096.9345 1658.1665 722.0750</td> <td>SSIM I 0.9876 0 0.9880 0 0.9880 0 0.9725 0 0.9836 0 0.9836 0 0.9716 0 0.9636 0 0.9636 0 0.9636 0 0.9881 0 9881 0 9881 0 9.9876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99878 0 0.98888 0 0.98888 0<!--</td--><td>Single Single Single<</td><td>043,7160 ipnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 1481.9069 1533.4767 1489.8284 inal Doppler SNR 3348.3633 3001.9109 503.1572 347.0005 1794.9318 1173.6201 22.4769</td><td>SSIM 0.9872 0.9872 0.9872 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.9865 0.9869 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9925 0.9821 0.9925 0.9811 0.9753 0.9856 0.88666 0.9857</td><td>RMSE 0.0074 0.0076 0.0192 0.0100 0.0112 0.0065 0.0075 0.0065 0.0051 0.0054 0.0150 0.0151 0.0054 0.0150 0.0051 0.0054 0.0156 0.0070</td><td>Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774 192.9850</td><td>SSIM 0.9833 0.9823 0.9829 0.9827 0.9829 0.9827 0.90745 0.9809 0.90745 0.9801 0.9821 0.9831 0.9821 0.9885 0.9885 0.9877 0.9775 0.9878 0.9878 0.9887 0.9885 0.9824</td><td>RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001</td><td>Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939 163.6533</td><td>SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9833 0.9796 0.9848 0.9809 0.9874 0.9874 0.9874 0.9889 0.9899 0.9899 0.9899 0.9895 0.9885 0.9885</td><td>RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001</td></td>	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3264 0.3244 0.1235 0.4546 0.1230 0.4546 0.1230 0.5653 RMSE 0.1700 0.5587 0.3244	Bumps SNR 99.0651 7.5524 13.8661 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844 2.9911 5.6148	SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.7850 0.7850 0.8654 0.6822 0.8654 0.6872 0.7850 0.8654 0.6792 0.7850 0.8790 0.5351 0.8431 0.8431 0.8431 0.5910 0.5718 0.5910 0.5718 0.5910 0.5911 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.5910 0.591	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2876 0.0485 0.04650000000000000000000000000000000000	Heavisine SNR 1833.9204 1843.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 1232.59118 1832.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6719 1021.0333 2096.9345 1658.1665 722.0750	SSIM I 0.9876 0 0.9880 0 0.9880 0 0.9725 0 0.9836 0 0.9836 0 0.9716 0 0.9636 0 0.9636 0 0.9636 0 0.9881 0 9881 0 9881 0 9.9876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99876 0 0.99878 0 0.98888 0 0.98888 0 </td <td>Single Single Single<</td> <td>043,7160 ipnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 1481.9069 1533.4767 1489.8284 inal Doppler SNR 3348.3633 3001.9109 503.1572 347.0005 1794.9318 1173.6201 22.4769</td> <td>SSIM 0.9872 0.9872 0.9872 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.9865 0.9869 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9925 0.9821 0.9925 0.9811 0.9753 0.9856 0.88666 0.9857</td> <td>RMSE 0.0074 0.0076 0.0192 0.0100 0.0112 0.0065 0.0075 0.0065 0.0051 0.0054 0.0150 0.0151 0.0054 0.0150 0.0051 0.0054 0.0156 0.0070</td> <td>Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774 192.9850</td> <td>SSIM 0.9833 0.9823 0.9829 0.9827 0.9829 0.9827 0.90745 0.9809 0.90745 0.9801 0.9821 0.9831 0.9821 0.9885 0.9885 0.9877 0.9775 0.9878 0.9878 0.9887 0.9885 0.9824</td> <td>RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001</td> <td>Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939 163.6533</td> <td>SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9833 0.9796 0.9848 0.9809 0.9874 0.9874 0.9874 0.9889 0.9899 0.9899 0.9899 0.9895 0.9885 0.9885</td> <td>RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001</td>	Single Single<	043,7160 ipnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 1481.9069 1533.4767 1489.8284 inal Doppler SNR 3348.3633 3001.9109 503.1572 347.0005 1794.9318 1173.6201 22.4769	SSIM 0.9872 0.9872 0.9872 0.9872 0.9871 0.9717 0.9664 0.9811 0.9788 0.9865 0.9869 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9885 0.9925 0.9821 0.9925 0.9811 0.9753 0.9856 0.88666 0.9857	RMSE 0.0074 0.0076 0.0192 0.0100 0.0112 0.0065 0.0075 0.0065 0.0051 0.0054 0.0150 0.0151 0.0054 0.0150 0.0051 0.0054 0.0156 0.0070	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774 192.9850	SSIM 0.9833 0.9823 0.9829 0.9827 0.9829 0.9827 0.90745 0.9809 0.90745 0.9801 0.9821 0.9831 0.9821 0.9885 0.9885 0.9877 0.9775 0.9878 0.9878 0.9887 0.9885 0.9824	RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939 163.6533	SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9833 0.9796 0.9848 0.9809 0.9874 0.9874 0.9874 0.9889 0.9899 0.9899 0.9899 0.9895 0.9885 0.9885	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001
SWT	COIFS Method Hard Soft Hard Hard Firm COIFS Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal Universal Heur. SURE	Level 5 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 10.7929 12.2687 55.0778 52.6838 405.9475 17.6555 137.6594 17.2810 Blocks SNR 208.2155 17.8817 55.8884 10.9178 86.2422 12.4543 55.9466 53.3230	SSIM 0.8895 0.7383 0.8398 0.6953 0.8608 0.7059 0.8608 0.9048 0.7833 0.8909 0.7346 SSIM 0.7346 0.9134 0.7459 0.817 0.7016 0.8120 0.7122 0.8680 0.8850	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3265 0.3202 0.3203 0.3264 0.2107 0.5653 RMSE 0.1700 0.5587 0.3239 0.7624 0.6598 0.3244 0.3244 0.3244	Bumps SNR 99.0651 7.5524 13.8861 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844 2.9911 2.9911 4.2951	SSIM 0.8632 0.6822 0.7671 0.7671 0.75299 0.8261 0.5299 0.8261 0.5857 0.6610 0.6283 0.9016 0.6283 0.9016 0.8654 0.6852 0.8654 0.8654 0.8654 0.8654 0.8790 0.8551 0.8790 0.5351 0.8431 0.59110 0.54110 0.5418 0.6718	RMSE 0.0718 0.2794 0.1747 0.3788 0.3788 0.3788 0.0485 0.0485 0.0485 0.0485 0.0485 0.0485 0.0485 0.0485 0.0485 0.0483 0.02356 RMSE 0.0672 0.1104 0.3292 0.1114 0.3292 0.2643 0.2643 0.2643	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine SNR 3265.2407 3210.7574 1476.6719 1021.0333 2096.9345 1658.1665 722.0750 483.3397	SSIM 0.9876 0.9800 0.9880 0.9800 0.9880 0.9725 0.9836 0.9716 0.9836 0.9636 0.9776 0.9636 0.9636 0.9746 0.9636 0.9636 0.9786 0.9881 0.9881 SSIM 0.99914 0.9914 0.99914 0.9925 0.99016 0.9785 0.99785 0.9968 0.97436 0.97673 0.9673	Single Single<	043,7160 ipnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 865.2308 867.3909 22.3787 8.8594 1481.9069 2074.5236 1533.4767 1489.8284 inal Doppler SNR 33348.3633 3001.9109 603.1572 347.0005 1794.9318 1173.6201 22.2.4769 8.8749	SSIM 0.9872 0.9872 0.9871 0.9702 0.9871 0.9702 0.9811 0.9788 0.9842 0.9859 0.9855 0.9859 0.9869 0.9850 0.9871 0.9852 0.9925 0.9925 0.9925 0.9857 0.9857 0.9857 0.9857 0.9857 0.8666 0.7944 0.8664	RMSE 0.0074 0.0076 0.0158 0.0192 0.0100 0.0112 0.0663 0.0075 0.0065 0.0077 RMSE 0.0051 0.0054 0.0054 0.0054 0.0054 0.0065 0.0054 0.0054 0.0054 0.0065 0.0066 0.0062	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 659.7482 539.1419 300.7501 189.7536 9.3197 859.7482 533.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774 192.9850 9.3476	SSIM 0.9833 0.9828 0.9829 0.9699 0.9745 0.9809 0.9745 0.9809 0.9745 0.9861 0.9821 0.9811 0.9821 0.9812 SSIM 0.9851 0.9878 0.9878 0.9878 0.9878 0.9878 0.9878 0.9829 0.9854 0.9820 0.9854	RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001	Epr 2 SNR 770.7123 501.2712 522.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939 163.6533 6.9562	 SSIM 0.9841 0.9841 0.9862 0.9836 0.9796 0.9836 0.9809 0.9809 0.9874 0.9864 0.9864 0.9864 0.9864 0.9864 0.9864 0.9864 0.9864 0.9865 0.9885 0.9886 0.9862 0.9886 0.9852 0.9888 0.9862 0.9856 0.9852 0.9852 0.9852 0.9852 0.9852 0.9852 0.9852 0.9852 0.9854 	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0003 0.0004
SWT	COIFS Method Hard Soft Garotte Hard Firm COIFS Method Hard Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6338 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155 17.8817 55.58884 10.9178 86.2422 12.4543 55.9466 53.3230 692.8110	SSIM 0.8895 0.7383 0.8398 0.8608 0.7059 0.8520 0.8408 0.7059 0.8549 0.8280 0.9048 0.7833 0.8309 0.7346 0.9134 0.7914 0.7016 0.8659 0.7016 0.8650 0.7012 0.8630 0.8350 0.8350 0.9261	RMSE 0.2098 0.5618 0.5657 0.3557 0.7052 0.3007 0.6636 0.3265 0.3204 0.3324 0.1700 0.5653 RMSE 0.1700 0.1507 0.5653 0.1507 0.5329 0.7024 0.2619 0.3244 0.3304 0.3304 0.3304 0.3304 0.3304	Bumps SNR 99.0651 7.5524 13.8661 2.0960 33.7368 3.0027 5.5730 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844 2.9911 5.61458 266.1092	SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5299 0.8261 0.5293 0.610 0.5857 0.6283 0.9016 0.7850 0.8780 0.6872 0.8790 0.6375 0.6318 0.6318 0.6318	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2672 0.2676 0.02876 0.02876 0.02876 0.02356 RMSE 0.3792 0.1114 0.3292 0.1676 0.3792 0.1676 0.3792 0.1676 0.3792 0.1679 0.2643 0.22870 0.2870 0.2870	Heavisine SNR 1833,9204 1845,3986 994,1497 730,2146 1237,5945 1039,2808 658,1572 493,7265 1325,9118 2179,5845 1832,7230 1842,4255 Heavisine SNR 3365,2407 3210,7574 1476,6719 1021,0333 2096,9345 1658,1665 722,0750 483,3397	SSIM I 0.9876 0 0.9876 0 0.9800 0 0.9800 0 0.9725 0 0.9836 0 0.9725 0 0.9836 0 0.9716 0 0.9636 0 0.9636 0 0.9881 0 SSIM 0 0.9881 0 0.9921 0 0.9887 0 0.9988 0 0.9785 0 0.9886 0 0.9787 0 0.9868 0 0.9784 0 0.9874 0 0.9873 0 0.9874 0 0.9873 0 0.9873 0 0.9873 0 0.9873 0 0.9873 0 0.9873 0 0.9873 0 </td <td>Sign Sign RMSE 4 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0993 - 0.09963 - 0.0663 - 0.0664 - 0.0533 - 0.0654 - 0.0664 - 0.0664 - 0.0653 - 0.0664 - 0.06653 - 0.0664 - 0.0667 - 0.0674 - 0.0674 - 0.0674 - 0.1147 - 0.0572 -</td> <td>043.7100 ipnal Dopopler SNR 1576.0468 1534.1732 346.0324 865.2308 887.3909 22.3787 8.8594 1481.9069 2074.5236 1533.4767 1489.8284 ipnal Doppler SNR 3348.3633 3001.9109 303.1572 347.0005 1794.9318 1173.6201 22.4769 8.8749 2994.5495</td> <td>SSIM 0.9872 0.9872 0.9871 0.9707 0.9674 0.9811 0.9768 0.9852 0.9869 0.9782 0.9885 0.9869 0.9871 SSIM 0.9925 0.9921 0.9953 0.9753 0.9753 0.8686 0.9753 0.9753 0.8666 0.9753 0.8771 0.8686 0.9753 0.9753 0.9753 0.9754 0.9753</td> <td>RMSE 0.0074 0.0075 0.0192 0.0192 0.0192 0.0192 0.0192 0.0100 0.0112 0.0024 0.0025 0.0077 RMSE 0.0051 0.0051 0.0192 0.0195</td> <td>Epr 1 SNR 657.0315 458.5849 512.8109 512.8109 300.7501 189.7536 9.3197 659.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774 192.9850 192.476 1362.3670</td> <td>SSIM 0.9833 0.9828 0.9629 0.9629 0.9745 0.9807 0.9024 0.9816 0.9821 0.9821 SSIM 0.9885 0.9885 0.9877 0.9758 0.98880 0.9758 0.9829 0.9758 0.9102 0.9885 0.9102</td> <td>RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001</td> <td>Epr 2 SNR 770.7123 501.2712 522.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939 163.6533 6.9562 1325.9304</td> <td>SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9833 0.9796 0.9836 0.9803 0.9053 0.9053 0.9874 0.9884 0.9889 0.9886 0.9889 0.9885 0.9888 0.9888 0.9888 0.9888 0.9888 0.9888 0.9888</td> <td>RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002</td>	Sign Sign RMSE 4 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0723 - 0.0993 - 0.09963 - 0.0663 - 0.0664 - 0.0533 - 0.0654 - 0.0664 - 0.0664 - 0.0653 - 0.0664 - 0.06653 - 0.0664 - 0.0667 - 0.0674 - 0.0674 - 0.0674 - 0.1147 - 0.0572 -	043.7100 ipnal Dopopler SNR 1576.0468 1534.1732 346.0324 865.2308 887.3909 22.3787 8.8594 1481.9069 2074.5236 1533.4767 1489.8284 ipnal Doppler SNR 3348.3633 3001.9109 303.1572 347.0005 1794.9318 1173.6201 22.4769 8.8749 2994.5495	SSIM 0.9872 0.9872 0.9871 0.9707 0.9674 0.9811 0.9768 0.9852 0.9869 0.9782 0.9885 0.9869 0.9871 SSIM 0.9925 0.9921 0.9953 0.9753 0.9753 0.8686 0.9753 0.9753 0.8666 0.9753 0.8771 0.8686 0.9753 0.9753 0.9753 0.9754 0.9753	RMSE 0.0074 0.0075 0.0192 0.0192 0.0192 0.0192 0.0192 0.0100 0.0112 0.0024 0.0025 0.0077 RMSE 0.0051 0.0051 0.0192 0.0195	Epr 1 SNR 657.0315 458.5849 512.8109 512.8109 300.7501 189.7536 9.3197 659.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774 192.9850 192.476 1362.3670	SSIM 0.9833 0.9828 0.9629 0.9629 0.9745 0.9807 0.9024 0.9816 0.9821 0.9821 SSIM 0.9885 0.9885 0.9877 0.9758 0.98880 0.9758 0.9829 0.9758 0.9102 0.9885 0.9102	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001	Epr 2 SNR 770.7123 501.2712 522.9110 282.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939 163.6533 6.9562 1325.9304	SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9833 0.9796 0.9836 0.9803 0.9053 0.9053 0.9874 0.9884 0.9889 0.9886 0.9889 0.9885 0.9888 0.9888 0.9888 0.9888 0.9888 0.9888 0.9888	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	COIFS Method Hard Soft Garotte Hard Firm COIFS Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155 17.8817 55.8884 10.9178 86.2422 12.4543 55.9466 53.3230 692.8110 28.3074	SSIM 0.8895 0.7383 0.8395 0.7383 0.8695 0.7059 0.8549 0.8549 0.8549 0.8280 0.9048 0.9048 0.9048 0.9484 0.7883 0.8549 0.7346 0.9134 0.7416 0.8659 0.8619 0.7416 0.8619 0.7416 0.8619 0.7416 0.8619 0.7412 0.8619 0.7112 0.86350 0.8350 0.9261 </td <td>RMSE 0.2098 0.5618 0.3657 0.7052 0.3007 0.6636 0.3244 0.1235 0.4546 0.2107 0.5653 RMSE 0.4707 0.5653 RMSE 0.1700 0.5658 0.3244 0.2107 0.5653 RMSE 0.1700 0.5658 0.3244 0.2619 0.6598 0.3244 0.3308 0.3308 0.3244</td> <td>Bumps SNR 99.0651 7.5524 13.8661 3.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844 2.9911 5.6148 4.3158 4.3158 266.1092 25.5206</td> <td>SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5857 0.6610 0.8587 0.6100 0.6283 0.9016 0.7850 0.8654 0.6822 0.8654 0.6872 0.7850 0.6372 0.78590 0.6371 0.5351 0.8431 0.5351 0.6338 0.9146 0.6338 0.9146 0.7906 0.9146 0.7906 0.9146 0.7906 0.9146 0.7906</td> <td>RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2876 0.0485 0.1343 0.0736 0.2356 RMSE 0.0485 0.2356 0.2356 0.2356 0.2357 0.3792 0.1114 0.3292 0.2470 0.2370 0.2370 0.2370</td> <td>Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6719 1021.0333 2096.9345 1658.1665 722.0750 483.3397 2958.4999 4180.0672</td> <td>SSIM I 0.9876 0 0.9806 0 0.9800 0 0.9803 0 0.9725 0 0.9836 0 0.9767 0 0.9803 0 0.9716 0 0.9636 0 0.9767 0 0.9876 0 0.9786 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9934 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9444 0</td> <td>Single Single RMSE 3 0.0723 - 0.0773 - 0.0773 - 0.0773 - 0.0979 - 0.0979 - 0.0979 - 0.1145 - 0.0963 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0868 - 0.0869 - 0.0869 - 0.0667 - 0.1406 - 0.14147 - 0.14147 - 0.1406 -</td> <td>043,7160 gnal Doppler SNR 1576,0468 1534,1732 346,0324 228,3804 865,2308 88794 1655,2308 88594 1633,4767 1488,8284 mal Doppler SNR 3348,3633 3001,9109 603,1572 347,0005 1794,9318 1173,6201 22,294,5495 4488,4772</td> <td>SSIM 0.9872 0.9872 0.9872 0.9872 0.9872 0.9872 0.9872 0.9644 0.9717 0.9644 0.9717 0.9664 0.9782 0.9782 0.9782 0.9782 0.93855 0.93825 0.93825 0.93857 0.93856 0.93857 0.88666 0.7944 0.98857 0.86666 0.7944 0.93733 0.9466</td> <td>RMSE 0.0074 0.0074 0.0075 0.0192 0.0100 0.0120 0.0074 0.0075 0.0075 0.0075 0.0075 0.0075 0.0075 0.0076 0.0051 0.0156 0.0156 0.0070 0.0086 0.0052 0.0055 0.0056 0.0052 0.0052 0.0053</td> <td>Epr 1 SNR 657.0315 458.5849 512.8109 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774 192.9850 9.3476 1362.3670 800.5943</td> <td>SSIM 0.9833 0.9828 0.9629 0.9629 0.9745 0.9809 0.9745 0.9809 0.9745 0.9809 0.9821 0.9821 0.9885 0.9878 0.9878 0.9878 0.9878 0.9878 0.9878 0.9878 0.9878 0.9878 0.9882 0.9882 0.9882 0.9882 0.9882 0.9882 0.9882 0.9882</td> <td>RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0001</td> <td>Epr 2 SNR 770.7123 501.2712 532.9110 262.5089 617.0429 448.1095 157.1578 69554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939 163.6533 6.9562 1232.5936 1232.5937 1235.533 6.9562 1232.5935 1235</td> <td>SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9833 0.9874 0.9894 0.9850 0.9874 0.9874 0.9874 0.9876 0.9876 0.9886 0.9899 0.9895 0.9885 0.9885 0.9886 0.9885 0.9885 0.9886 0.9885 0.98</td> <td>RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0003 0.0001 0.0001</td>	RMSE 0.2098 0.5618 0.3657 0.7052 0.3007 0.6636 0.3244 0.1235 0.4546 0.2107 0.5653 RMSE 0.4707 0.5653 RMSE 0.1700 0.5658 0.3244 0.2107 0.5653 RMSE 0.1700 0.5658 0.3244 0.2619 0.6598 0.3244 0.3308 0.3308 0.3244	Bumps SNR 99.0651 7.5524 13.8661 3.0960 33.7368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 37.7844 2.9911 5.6148 4.3158 4.3158 266.1092 25.5206	SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5857 0.6610 0.8587 0.6100 0.6283 0.9016 0.7850 0.8654 0.6822 0.8654 0.6872 0.7850 0.6372 0.78590 0.6371 0.5351 0.8431 0.5351 0.6338 0.9146 0.6338 0.9146 0.7906 0.9146 0.7906 0.9146 0.7906 0.9146 0.7906	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2876 0.0485 0.1343 0.0736 0.2356 RMSE 0.0485 0.2356 0.2356 0.2356 0.2357 0.3792 0.1114 0.3292 0.2470 0.2370 0.2370 0.2370	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6719 1021.0333 2096.9345 1658.1665 722.0750 483.3397 2958.4999 4180.0672	SSIM I 0.9876 0 0.9806 0 0.9800 0 0.9803 0 0.9725 0 0.9836 0 0.9767 0 0.9803 0 0.9716 0 0.9636 0 0.9767 0 0.9876 0 0.9786 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9914 0 0.9934 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9474 0 0.9444 0	Single Single RMSE 3 0.0723 - 0.0773 - 0.0773 - 0.0773 - 0.0979 - 0.0979 - 0.0979 - 0.1145 - 0.0963 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0867 - 0.0868 - 0.0869 - 0.0869 - 0.0667 - 0.1406 - 0.14147 - 0.14147 - 0.1406 -	043,7160 gnal Doppler SNR 1576,0468 1534,1732 346,0324 228,3804 865,2308 88794 1655,2308 88594 1633,4767 1488,8284 mal Doppler SNR 3348,3633 3001,9109 603,1572 347,0005 1794,9318 1173,6201 22,294,5495 4488,4772	SSIM 0.9872 0.9872 0.9872 0.9872 0.9872 0.9872 0.9872 0.9644 0.9717 0.9644 0.9717 0.9664 0.9782 0.9782 0.9782 0.9782 0.93855 0.93825 0.93825 0.93857 0.93856 0.93857 0.88666 0.7944 0.98857 0.86666 0.7944 0.93733 0.9466	RMSE 0.0074 0.0074 0.0075 0.0192 0.0100 0.0120 0.0074 0.0075 0.0075 0.0075 0.0075 0.0075 0.0075 0.0076 0.0051 0.0156 0.0156 0.0070 0.0086 0.0052 0.0055 0.0056 0.0052 0.0052 0.0053	Epr 1 SNR 657.0315 458.5849 512.8109 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774 192.9850 9.3476 1362.3670 800.5943	SSIM 0.9833 0.9828 0.9629 0.9629 0.9745 0.9809 0.9745 0.9809 0.9745 0.9809 0.9821 0.9821 0.9885 0.9878 0.9878 0.9878 0.9878 0.9878 0.9878 0.9878 0.9878 0.9878 0.9882 0.9882 0.9882 0.9882 0.9882 0.9882 0.9882 0.9882	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 262.5089 617.0429 448.1095 157.1578 69554 757.7529 719.1125 511.2195 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939 163.6533 6.9562 1232.5936 1232.5937 1235.533 6.9562 1232.5935 1235	SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9833 0.9874 0.9894 0.9850 0.9874 0.9874 0.9874 0.9876 0.9876 0.9886 0.9899 0.9895 0.9885 0.9885 0.9886 0.9885 0.9885 0.9886 0.9885 0.98	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0003 0.0001 0.0001
SWT	COIFS Method Hard Soft Garotte Hard Firm COIFS Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal Universal Heur. SURE MINIMAX	Level 5 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 138.5960 17.6176 46.3927 10.7929 65.9442 12.2687 55.0778 52.6838 405.9475 27.6555 137.6594 17.2810 Blocks SNR 208.2155 17.8817 55.8844 10.9178 86.2422 12.4543 55.9466 53.3230 692.8110 28.3074 203.5541	SSIM 0.8895 0.7383 0.8395 0.7383 0.8095 0.7383 0.8095 0.8549 0.8549 0.8549 0.8280 0.9048 0.9488 0.9484 0.7483 0.84909 0.7346 0.9134 0.7459 0.8174 0.7459 0.8170 0.7016 0.8859 0.8859 0.84859 0.7422 0.86860 0.9261 0.9261 0.9261 0.79201 0.9155	RMSE 0.2098 0.5618 0.3557 0.7052 0.3007 0.6636 0.3244 0.1235 0.4546 0.1230 0.4546 0.12107 0.5653 RMSE 0.1700 0.5587 0.3244 0.3244 0.3244 0.3934 0.4561	Bumps SNR 99.0651 7.5524 13.8861 3.8861 3.8861 3.37368 3.0027 5.5730 4.2975 219.8949 25.7596 93.9431 6.9172 Bumps SNR 111.9661 7.4515 15.0849 2.0909 3.77844 2.9911 5.6148 4.3158 2.66.1092 25.5226 107.1882	SSIM 0.8632 0.6927 0.7671 0.7671 0.5299 0.8261 0.5299 0.8261 0.5299 0.8261 0.5299 0.8261 0.6120 0.8357 0.6100 0.7850 0.9016 0.7850 0.8654 0.7850 0.8654 0.7850 0.6372 0.7850 0.63511 0.5351 0.6341 0.6318 0.9146 0.6328 0.9146	RMSE 0.0718 0.2294 0.1747 0.3788 0.1184 0.3287 0.2876 0.0485 0.1343 0.0485 0.0485 0.0485 0.0485	Heavisine SNR 1833.9204 1845.3986 994.1497 730.2146 1237.5945 1039.2808 658.1572 493.7265 1325.9118 2179.5845 1832.7230 1842.4255 Heavisine SNR 3365.2407 3210.7574 1476.6719 1021.0333 2096.9345 1658.1665 722.0750 483.3397 2958.4999 4180.0672 3392.7314	SSIM I 0.9876 0 0.9880 0 0.9800 0 0.9725 0 0.9803 0 0.9716 0 0.9803 0 0.9716 0 0.9716 0 0.9716 0 0.9766 0 0.9767 0 0.9768 0 0.9767 0 0.9881 0 0.9884 0 0.99014 0 0.99014 0 0.99014 0 0.99014 0 0.99014 0 0.99014 0 0.99013 0 0.99014 0 0.99013 0 0.99014 0 0.99013 0 0.99014 0 0.99015 0 0.99016 0 0.99017 0 0.99018 0	Single Control State Sta	043,7160 ipnal Doppler SNR 1576.0468 1534.1732 346.0324 228.3804 865.2308 887.3909 22.3787 8.8594 1533.4767 1489.8284 inal Doppler SNR 3348.3633 3001.9109 503.1572 347.0005 7794.9318 1173.6201 22.944.84772 3289.9461	SSIM 0.9872 0.9872 0.9872 0.9874 0.9872 0.9717 0.9674 0.9604 0.9685 0.9855 0.9885 0.9855 0.9885 0.9856 0.9866 0.9925 0.9866 0.9856 0.9865 0.9866 0.9867 0.9866 0.9867 0.9866 0.9943 0.9943 0.9944 0.9943 0.9943 0.9943 0.9944	RMSE 0.0074 0.0075 0.0192 0.0100 0.0192 0.0100 0.0192 0.0076 0.0924 0.0075 0.0075 0.0075 0.0076 0.0075 0.0076 0.0076 0.0076 0.0051 0.0054 0.0054 0.0076 0.0070 0.0054 0.0050 0.0070 0.0086 0.0052 0.0054 0.0055 0.0044 0.00451	Epr 1 SNR 657.0315 458.5849 512.8109 156.5728 589.1419 300.7501 189.7536 9.3197 859.7482 593.1300 532.0710 445.4389 Epr 1 SNR 938.6651 578.5280 628.3121 228.6387 750.3304 420.7774 192.9850 9.3476 1362.3670 300.5943 629.3615	SSIM 0.9833 0.9828 0.9629 0.9629 0.9745 0.9809 0.9745 0.9809 0.9811 0.9881 0.9821 0.9885 0.9885 0.9878 0.9878 0.9878 0.9879 0.9745 0.9829 0.9878 0.9879 0.9758 0.9829 0.9885 0.9880 0.9829 0.9854 0.9102 0.9854 0.9102 0.9854 0.9102 0.9885 0.9885 0.9885 0.9885	RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 770.7123 501.2712 532.9110 242.5089 617.0429 448.1095 157.1578 6.9554 757.7529 719.1125 535.7472 Epr 2 SNR 1235.7235 616.5406 752.0269 377.1889 940.3162 523.8939 163.6533 6.9562 1325.9304 1216.9505 1152.3854	SSIM 0.9841 0.9841 0.9862 0.9833 0.9796 0.9848 0.9809 0.9856 0.9889 0.9889 0.9889 0.9889 0.9886 0.9986 0.	RMSE 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001

Table S3. Performance of the SWT at decomposition levels 5 and 6 with the coif 5 wavelet for 6 thresholding combinations. The tables give the performance of each combination in terms of SNR, SSIM, and RMSE in order of increasing starting SNR (10, 50, 100, 200) of the noisy test signal. Results are presented for the following test signals: blocks, bumps, heavisine, doppler, 1^{st} EPR test signal, and 2^{nd} EPR test signal. Method refers to the thresholding form, while selection refers to the means of calculating the threshold value.

												Sig	inal								
	BIOR22	SNR=10		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
			5	41.4970	0.7579	0.3763	39.6093	0.7775	0.1101	271.0727	0.9558	0.1882	72.8114	0.9074	0.0337	198.0704	0.9220	0.0002	214.7371	0.9202	0.0002
	Hard	Universal	6	24.6391	0.7600	0.4802	19.6650	0.7932	0.1517	291.8265	0.9548	0.1811	47.0702	0.8983	0.0412	166.2818	0.9427	0.0002	195.5132	2 0.9434	0.0002
			5	26.0574	0 7250	0.4669	7.4475	0.6636	0.2289	267.9706	0 9549	0.1893	33.1572	0.8706	0.0493	139.4033	0.9200	0.0002	142.4853	0 9168	0.0003
	Soft	Universal	6	12.8509	0 7143	0.6422	3.5059	0.6032	0.3047	267.9607	0.9531	0.1887	17.0146	0.8432	0.0661	48.9434	0.9332	0.0003	53.5314	0.9309	0.0005
			5	28,3341	0 7316	0.4489	14,1162	0 7184	0.1744	268,2973	0.9549	0.1892	42,4920	0.8841	0.0437	164,9758	0.9206	0.0002	180,4965	5 0 9182	0.0003
	Garotte	Universal	6	15.3871	0.7310	0.5919	6.5146	0.6818	0.2393	270.1197	0.9532	0.1880	24,2176	0.8671	0.0560	96.8012	0.9200	0.0002	109,2636	0.9102	0.0003
SWT			5	73 3307	0.7255	0 2847	9.4641	0.6671	0.2106	276.0162	0.0002	0 1872	21 4 388	0.0071	0.0610	93 1264	0.0002	0.0002	77 3256	0.00/1	0.0004
	Hard	Heur. SURE	6	77 2462	0.7055	0.2770	8 5795	0.0071	0.2161	374 7538	0.0557	0.1615	8 6592	0.0455	0.0014	8 2940	0.011	0.0007	5 8051	0.9140	0.0012
			5	84.0505	0.01/7	0.2677	80 / 162	0.7072	0.0701	250 4107	0.9337	0.1083	120 5231	0.7855	0.0264	107 1103	0.9014	0.0007	201 4585	0.0524	0.0002
	Hard	MINIMAX	6	54 6881	0.7918	0.2011	54 6515	0.0050	0.0045	363 5807	0.9554	0.1651	0/ /302	0.9197	0.0204	220 3703	0.9154	0.0002	260 6850	0.9155	0.0002
			5	41 6570	0.8050	0.3232	24.0497	0.0501	0.0345	276 2110	0.9490	0.1001	70 7001	0.9228	0.0233	100 2042	0.9400	0.0002	200.0000	0.9464	0.0002
	Firm	MINIMAX	0	41.0070	0.7507	0.3742	47 5000	0.7720	0.1105	270.2110	0.9500	0.1005	12.1321	0.9062	0.0337	199.2042	0.9210	0.0002	220.12/0	0.9205	0.0002
			0	25.5099	0.7656	0.4709	17.3090	0.7854	0.1561	305.6133	0.9555	0.1769	45.5967	0.8979	0.0416	159.2902	0.9455	0.0002	100.7215	0.9436	0.0003
												Sig	nal								
	BIOR	22 SNR=50		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Metho	od Selection	Lev	el SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM R	MSE
	Hard	Universal	5	151.0134	4 0.8851	0.1999	9 196.8082	0.9320	0.0509	926.0523	0.9789	0.1020	250.7820	0.9596	0.0184	484.8865	0.9756	0.0001	431.3728	0.9761 0	.0002
			6	79.4510	0.8917	7 0.2741	68.6446	0.9307	0.0849	1039.1477	0.9805	0.0973	117.6024	0.9451	0.0264	352.9374	0.9764	0.0001	411.5234	0.9819 0	.0002
	Soft	Universal	5	50.3246	0.8348	3 0.3396	3 23.7794	0.8764	0.1360	665.6600	0.9726	0.1201	68.3388	0.9258	0.0346	331.9310	0.9747	0.0001	345.7118	0.9755 0	.0002
			6	24.0500	0.8143	3 0.4794	8.1789	0.7739	0.2144	512.6012	0.9677	0.1367	30.3908	0.8957	0.0503	106.7514	0.9700	0.0002	130.6239	0.9736 0	.0003
	Garot	te Universal	5	73.6250	0.8562	0.2829	66.4503	0.9147	0.0853	723.0526	0.9746	0.1154	113.9026	0.9424	0.0270	429.8003	0.9753	0.0001	416.0130	0.9760 0	.0002
SW	т		6	37.2149	0.8464	1 0.3919	20.8983	0.8656	0.1452	632.6386	0.9709	0.1236	53.5881	0.9216	0.0384	220.1926	0.9730	0.0002	278.0957	0.9778 0	.0002
	Hard	Heur, SUR	8E 5	87.1714	0.8659	9 0.2615	5 9.5081	0.7739	0.2096	673.2948	0.9732	0.1197	22.6322	0.8681	0.0594	117.4861	0.9719	0.0002	96.9654	0.9722 0	.0003
			6	86.9797	0.8950	0.2615	5 8.5281	0.7625	0.2163	721.8025	0.9740	0.1163	8.7464	0.7977	0.0911	8.4263	0.9372	0.0007	5.9120	0.9373 0	.0012
	Hard	MINIMAX	5	312.1474	4 0.9012	2 0.1401	399.8178	0.9391	0.0361	1062.1718	0.9747	0.0957	490.0415	0.9703	0.0132	504.4275	0.9748	0.0001	492.5760	0.9749 0	.0002
			6	187.2176	6 0.9207	7 0.1797	182.0533	0.9485	0.0531	1525.5232	0.9819	0.0800	278.1575	0.9636	0.0175	471.3278	0.9805	0.0001	452.9541	0.9832 0	.0002
	Firm	MINIMAX	5	145.0570	0.8834	1 0.2038	8 181.6408	0.9309	0.0530	934.2656	0.9787	0.1016	235.7614	0.9591	0.0189	439.6543	0.9759	0.0001	334.0593	0.9766 0	.0002
			6	76.1504	0.8886	5 0.2792	2 62.7433	0.9280	0.0886	1004.1832	0.9795	0.0986	111.6603	0.9446	0.0271	346.4846	0.9767	0.0001 3	399.5213	0.9815 0	.0002
												Sig	nal								
	BIOR22	SNR=100		Blocks			Bumps			Heavisine		Sig	nal Doppler			Epr 1			Epr 2		
	BIOR22 Method	SNR=100 Selection	Level	Blocks SNR	SSIM	RMSE	Bumps SNR	SSIM	RMSE	Heavisine SNR	SSIM	Sig RMSE	nal Doppler SNR	SSIM	RMSE	Epr 1 SNR	SSIM	RMSE	Epr 2 SNR	SSIM	RMSE
	BIOR22 Method Hard	SNR=100 Selection	Level	Blocks SNR 302.5134	SSIM 0.9324	RMSE 0.1422	Bumps SNR 359.1325	SSIM 0.9663	RMSE 0.0382	Heavisine SNR 1941.8538	SSIM 0.9889	Sig RMSE 0.0706	nal Doppler SNR 506.6253	SSIM 0.9766	RMSE	Epr 1 SNR 581.3284	SSIM 0.9837	RMSE	Epr 2 SNR 530.6969	SSIM 0.9841	RMSE
	BIOR22 Method Hard	SNR=100 Selection Universal	Level 5 6	Blocks SNR 302.5134 128.3804	SSIM 0.9324 0.9256	RMSE 0.1422 0.2169	Bumps SNR 359.1325 103.6527	SSIM 0.9663 0.9623	RMSE 0.0382 0.0696	Heavisine SNR 1941.8538 1870.2313	SSIM 0.9889 0.9890	Sig RMSE 0.0706 0.0721	nal Doppler SNR 506.6253 165.2425	SSIM 0.9766 0.9555	RMSE 0.0130 0.0224	Epr 1 SNR 581.3284 473.8570	SSIM 0.9837 0.9843	RMSE 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594	SSIM 0.9841 0.9864	RMSE 0.0002 0.0002
	BIOR22 Method Hard Soft	SNR=100 Selection Universal	Level 5 6 5	Blocks SNR 302.5134 128.3804 76.7110	SSIM 0.9324 0.9256 0.8850	RMSE 0.1422 0.2169 0.2762	Bumps SNR 359.1325 103.6527 37.1811	SSIM 0.9663 0.9623 0.9315	RMSE 0.0382 0.0696 0.1104	Heavisine SNR 1941.8538 1870.2313 1033.6593	SSIM 0.9889 0.9890 0.9821	Sig RMSE 0.0706 0.0721 0.0961	nal Doppler SNR 506.6253 165.2425 101.1128	SSIM 0.9766 0.9555 0.9456	RMSE 0.0130 0.0224 0.0285	Epr 1 SNR 581.3284 473.8570 440.0385	SSIM 0.9837 0.9843 0.9833	RMSE 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689	SSIM 0.9841 0.9864 0.9837	RMSE 0.0002 0.0002 0.0002
	BIOR22 Method Hard Soft	SNR=100 Selection Universal Universal	Level 5 6 5 6	Blocks SNR 302.5134 128.3804 76.7110 32.1897	SSIM 0.9324 0.9256 0.8850 0.8495	RMSE 0.1422 0.2169 0.2762 0.4168	Bumps SNR 359.1325 103.6527 37.1811 10.9900	SSIM 0.9663 0.9623 0.9315 0.8308	RMSE 0.0382 0.0696 0.1104 0.1881	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404	SSIM 0.9889 0.9890 0.9821 0.9731	Sig 0.0706 0.0721 0.0961 0.1154	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373	SSIM 0.9766 0.9555 0.9456 0.9106	RMSE 0.0130 0.0224 0.0285 0.0454	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568	SSIM 0.9837 0.9843 0.9833 0.9774	RMSE 0.0001 0.0001 0.0001 0.0002	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941	SSIM 0.9841 0.9864 0.9837 0.9805	RMSE 0.0002 0.0002 0.0002 0.0002
	BIOR22 Method Hard Soft Garotte	SNR=100 Selection Universal Universal	Level 5 6 5 6 5 5 5	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093	SSIM 0.9889 0.9890 0.9821 0.9731 0.9850	Sig 0.0706 0.0721 0.0961 0.1154 0.0864	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624	RMSE 0.0130 0.0224 0.0285 0.0454 0.0205	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186	SSIM 0.9837 0.9843 0.9833 0.9774 0.9837	RMSE 0.0001 0.0001 0.0001 0.0002 0.0002	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte	SNR=100 Selection Universal Universal	Level 5 6 5 6 5 6 5 6	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8848	RMSE 0.2169 0.2762 0.4168 0.2122 0.3232	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786	SSIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800	Sig 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359	RMSE 0.0130 0.0224 0.0285 0.0454 0.0205 0.0334	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634	SSIM 0.9837 0.9843 0.9833 0.9774 0.9837 0.9803	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 5 5	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8848 0.8962	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2628	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.8138	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214 0.2098	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546	SSIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800 0.9768	Sig <u>RMSE</u> 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.1121	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715	RMSE 0.0130 0.0224 0.0285 0.0454 0.0205 0.0334 0.0594	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603	SSIM 0.9837 0.9843 0.9833 0.9774 0.9837 0.9803 0.9802	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9840 0.9841 0.9803	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 6 5 6	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8848 0.8962 0.9109	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2628 0.2643	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519	SSIM 0.9663 0.9315 0.8308 0.9574 0.9140 0.8138 0.7833	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214 0.2098 0.2167	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088	SSIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800 0.9768 0.9771	Sig RMSE 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.1121 0.1119	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990 8.7569	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715 0.7998	RMSE 0.0130 0.0224 0.0285 0.0454 0.0205 0.0334 0.0594 0.0910	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374	SSIM 0.9837 0.9843 0.9833 0.9774 0.9837 0.9803 0.9802 0.9433	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9803 0.9424	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 5 6 5 5	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403 958.4361	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8848 0.8962 0.9109 0.9430	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2628 0.2643 0.0811	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.8138 0.7833 0.9704	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214 0.2098 0.2167 0.0255	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756	S SIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800 0.9768 0.9771 0.9872	Sig <u>RMSE</u> 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.1121 0.1119 0.0651	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990 8.7569 8886.7644	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715 0.7998 0.9818	RMSE 0.0130 0.0224 0.0285 0.0454 0.0205 0.0334 0.0594 0.0910 0.0098	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712	SSIM 0.9837 0.9843 0.9833 0.9774 0.9837 0.9803 0.9802 0.9433 0.9840	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9803 0.9424 0.9847	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0003 0.0001
SWT	BIOR22 Method Hard Soft Garotte Hard Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403 958.4361 311.0608	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8848 0.8962 0.9109 0.9430 0.9431	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2628 0.2643 0.0811 0.1397	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.8138 0.7833 0.9704 0.9719	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214 0.2098 0.2167 0.0255 0.0432	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991	S SIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800 0.9768 0.9771 0.9872 0.9923	Sig RMSE 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.1121 0.1119 0.0651 0.0548	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990 8.7569 886.7644 443.8720	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715 0.7998 0.9818 0.9757	RMSE 0.0130 0.0224 0.0255 0.0454 0.0205 0.0334 0.0594 0.0910 0.0098 0.0138	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662	SSIM 0.9837 0.9843 0.9833 0.9774 0.9803 0.9802 0.9802 0.9433 0.9840 0.9861	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9803 0.9424 0.9847 0.9876	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0003 0.0012 0.0001 0.0001
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 5 6 5 5	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403 958.4361 311.0608 307.8672	SSIM 0.9324 0.9256 0.8850 0.9100 0.8848 0.8962 0.9109 0.9430 0.9441 0.9312	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2643 0.0811 0.1397 0.1411	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.4643 9.4540 8.4519 807.2213 274.0819 354.2006	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.8138 0.7833 0.9704 0.9719 0.9664	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214 0.2098 0.2167 0.0255 0.0432 0.0382	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 1022.5786 1022.5786 761.9088 2283.4756 3235.4991 1928.4188	S SIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800 0.9768 0.9771 0.9872 0.9923 0.9889	Sig RMSE 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.1121 0.1119 0.0651 0.0548 0.0707	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990 8.7569 886.7644 443.8720 459.1724	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715 0.7998 0.9818 0.9757 0.9760	RMSE 0.0130 0.0224 0.0285 0.0454 0.0205 0.0334 0.0594 0.0910 0.0098 0.0138 0.0136	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613	SSIM 0.9837 0.9843 0.9833 0.9774 0.9837 0.9803 0.9802 0.9433 0.9840 0.9861 0.9841	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9858	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9803 0.9424 0.9847 0.9876 0.9844	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 5 6 5 5 6 5 5 6	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 84.5403 958.4361 311.0608 307.8672 120.8063	SSIM 0.9324 0.9256 0.8850 0.9100 0.8848 0.8962 0.9109 0.9430 0.9431 0.9312 0.9239	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2628 0.2643 0.0811 0.1397 0.1411 0.2225	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.8138 0.7833 0.9704 0.9719 0.9664 0.9598	RMSE 0.0382 0.0696 0.1104 0.0643 0.1214 0.2098 0.2167 0.0255 0.0432 0.0382 0.0720	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4766 1928.4188 1851.7938	S SIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800 0.9768 0.9771 0.9872 0.9923 0.9889 0.9889	Sig 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.1121 0.1119 0.0651 0.0548 0.0707 0.0723	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990 886.7649 886.7644 443.8720 459.1724 164.5700	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715 0.7998 0.9818 0.9757 0.9760 0.9576	RMSE 0.0130 0.0224 0.0285 0.0454 0.0205 0.0334 0.0594 0.0910 0.0098 0.0138 0.0136 0.0224	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600	SSIM 0.9837 0.9843 0.9833 0.9774 0.9803 0.9803 0.9802 0.9433 0.9840 0.9861 0.9841 0.9839	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 5.0997 786.0141 570.2064 415.9858 476.6276	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9803 0.9424 0.9847 0.9876 0.9844 0.9865	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0001 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 5 6 6 6 5 6	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403 958.4361 958.4361 311.0608 307.8672 120.8063	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8848 0.8962 0.9109 0.9430 0.9431 0.9312 0.9239	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2628 0.2643 0.811 0.1397 0.1411 0.2225	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.8138 0.7833 0.9704 0.9719 0.9664 0.9598	RMSE 0.0382 0.0696 0.1104 0.0643 0.1214 0.2098 0.2167 0.0255 0.0432 0.0382 0.0720	Heavisine SNR 1941.8538 1870.2313 1033.6593 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938	S SIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800 0.9768 0.9771 0.9872 0.9823 0.9889 0.9890	Sig 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.1121 0.1121 0.01121 0.0651 0.0548 0.0707 0.0723 Sig	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990 886.7644 443.8720 459.1724 164.5700 nal	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715 0.7998 0.9818 0.9757 0.9760 0.9576	RMSE 0.0130 0.0224 0.0285 0.0454 0.0205 0.0334 0.0594 0.0910 0.0098 0.0138 0.0136 0.0224	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600	SSIM 0.9837 0.9843 0.9833 0.9774 0.9803 0.9802 0.9433 0.9840 0.9861 0.9841 0.9839	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 786.0141 570.2064 415.9858 476.6276	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9843 0.9843 0.9847 0.9876 0.9844 0.9865	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0012 0.0001 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm BIOR22	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 302.5134 76.7110 32.1897 132.5825 55.5109 88.57986 84.6403 958.4361 311.0608 307.8672 120.8063 Blocks	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8848 0.8962 0.9109 0.9430 0.9431 0.9312 0.9239	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2628 0.2643 0.0811 0.1397 0.1411 0.2225	Bumps SNR 359.13255 37.1811 10.9900 119.6250 30.6463 8.4540 8.4549 807.2213 274.0819 354.2006 95.6455 Bumps	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.8138 0.7833 0.9704 0.9719 0.9664 0.9598	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214 0.2098 0.2167 0.0255 0.0432 0.0382 0.0720	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine	S SIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800 0.9768 0.9771 0.9872 0.9823 0.9889 0.9890	Sig RMSE 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.1121 0.1121 0.0651 0.0548 0.0707 0.0723 Sig	nal Doppler SNR 506.6253 165.2425 101.1128 37.8373 200.1970 71.5805 22.5990 8.7569 886.7644 443.8720 4459.1724 164.5700 nal Doppler	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715 0.7998 0.9818 0.9757 0.9760 0.9576	RMSE 0.0130 0.0224 0.0255 0.0454 0.0205 0.0334 0.0594 0.0910 0.0098 0.0136 0.0224	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1	SSIM 0.9837 0.9843 0.9833 0.9774 0.9803 0.9802 0.9433 0.9840 0.9861 0.9841 0.9839	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9858 476.6276 Epr 2	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9803 0.9424 0.9847 0.9876 0.9844 0.9865	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0001 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm BIOR22 Method	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection	Level	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403 958.4361 311.0608 307.8672 120.8063 Blocks SNR	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8848 0.8962 0.9109 0.9430 0.9441 0.9312 0.9239 SSIM	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2643 0.2643 0.2643 0.1397 0.1411 0.2225	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.914 0.8138 0.7833 0.9704 0.9719 0.9664 0.9598 SSIM	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214 0.2098 0.2167 0.0255 0.0432 0.0382 0.0720	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine SNR	S SIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9768 0.9772 0.9972 0.9923 0.9889 0.9889 0.9890 S SIM	Sig RMSE 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.1121 0.1121 0.0651 0.0548 0.0707 0.0723 Sig RMSE	nal Doppler SNR 506.6243 165.2425 200.1970 71.5805 22.5990 886.7644 443.8720 459.1724 164.5700 nal Doppler SNR	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.8715 0.7998 0.8715 0.9757 0.9760 0.9576 SSIM	RMSE 0.0130 0.0224 0.0255 0.0454 0.0205 0.0334 0.0910 0.0098 0.0138 0.0138 0.0224	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR	SSIM 0.9837 0.9843 0.9774 0.9803 0.9803 0.9802 0.9433 0.9840 0.9861 0.9841 0.9839 SSIM	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9858 476.6276 Epr 2 SNR	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9847 0.9876 0.9844 0.9865 SSIM	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm BIOR22 Method Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal	Level 5 6 5 6 5 6 5 6 5 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 5 5 6 6 5 5 5 6 6 5 5 5 5 5 6 6 5	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403 958.4361 311.0608 307.8672 120.8063 Blocks SNR 694.6432	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8848 0.8962 0.9109 0.9430 0.9441 0.9412 0.9239 SSIM	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2643 0.2643 0.3811 0.1397 0.1411 0.2225 RMSE 0.0946	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR 722.4458	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.8138 0.9704 0.9719 0.9664 0.9598 SSIM 0.9825	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214 0.2098 0.0255 0.0432 0.0382 0.0720 RMSE 0.0267	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 758.6546 758.6546 758.0546 1022.5786 758.0546 1022.5786 1023.5786 1025.7786 1	S SIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9768 0.9771 0.9872 0.9872 0.9889 0.9889 0.9890 S SIM	Sig RMSE 0.0706 0.0721 0.0961 0.1154 0.0974 0.0974 0.01121 0.0651 0.0548 0.0707 0.0723 Sig RMSE 0.0519	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990 886.7644 443.8720 459.1724 164.5700 nal Doppler SNR	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715 0.7998 0.9757 0.9760 0.9760 0.9576	RMSE 0.0130 0.0224 0.0255 0.0454 0.0205 0.0334 0.0910 0.0138 0.0136 0.0124	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095	SSIM 0.9837 0.9843 0.9833 0.9774 0.9803 0.9802 0.9802 0.9433 0.9802 0.9433 0.9841 0.9841 0.9839 SSIM 0.9881	RMSE 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9858 476.6276 Epr 2 SNR 727.2110	SSIM 0.9841 0.9864 0.9837 0.9803 0.9841 0.9803 0.9424 0.9847 0.9846 0.9847 0.9846 0.9847 0.9846 0.9847 0.9846 0.9847 0.9846 0.9846 0.9847 0.9846 0.9846	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm BIOR22 Method Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal	Level 5 6	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403 958.4361 311.6068 958.4361 311.6063 Blocks SNR 694.6432 242.2129	SSIM 0.9324 0.9256 0.8850 0.8495 0.8495 0.8491 0.9100 0.8448 0.9109 0.9430 0.9431 0.9312 0.9239 SSIM 0.9593 0.9505	RMSE 0.1422 0.2169 0.2762 0.3232 0.2628 0.2643 0.8111 0.14411 0.2225 RMSE 0.0946 0.1587	Bumps SNR 359.1325 103.6527 37.1811 10.9000 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 95.6455 Bumps 5NR 722.4458 166.7632	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.8138 0.9704 0.9719 0.9664 0.9598 SSIM 0.9825 0.9771	RMSE 0.0382 0.0696 0.1104 0.3821 0.0643 0.1214 0.2098 0.2167 0.0255 0.0432 0.0382 0.0720 RMSE 0.0267 0.0556	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine SNR 3563.8823 3243.0299	S SIM 0.9889 0.9890 0.9820 0.9731 0.9850 0.9800 0.9768 0.9771 0.9872 0.9923 0.9889 0.9890 S SIM 0.9939 0.9938	Sig RMSE 0.0706 0.0721 0.0961 0.1154 0.0864 0.0974 0.01121 0.0454 0.0548 0.0548 0.0548 0.0548 0.0548 0.0549 0.0545	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5900 8.7569 886.7644 443.8720 459.1724 164.5700 nal Doppler SNR 806.2839 213.4945	SSIM 0.9766 0.9555 0.9456 0.9106 0.9624 0.9359 0.8715 0.7998 0.9757 0.9760 0.9576 SSIM 0.9829 0.9623	RMSE 0.0130 0.0224 0.0255 0.0344 0.0594 0.0910 0.0098 0.0138 0.0136 0.0224 RMSE 0.0103 0.0138 0.0138 0.0139	Epr 1 SNR 581.3284 473.8570 440.0385 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004	SSIM 0.9837 0.9843 0.9833 0.9774 0.9803 0.9802 0.9433 0.9840 0.9861 0.9881 0.9881 0.9881	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9658 476.6276 Epr 2 SNR 727.2110 510.0676	SSIM 0.9841 0.9854 0.9805 0.9805 0.9840 0.9841 0.9803 0.9424 0.9876 0.9846 0.9876 0.9876 0.9844 0.9876 0.9845 SSIM 0.9893 0.9893	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0012 0.0001 0.0002 0.0002 0.0001 0.0002 RMSE 0.0001 0.0001
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm BIOR22 Method Hard Soft	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selecton Universal	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 302,5134 128,3804 76,7110 32,1897 132,5825 55,5109 85,7986 84,6403 958,4361 311,0608 307,8672 120,8063 Blocks SNR 694,6432 242,2129 115,1432	SSIM 0.9324 0.9256 0.8850 0.8405 0.9100 0.8488 0.8910 0.9430 0.9430 0.9432 0.9323 SSIM 0.9593 0.9593	RMSE 0.1422 0.2169 0.2762 0.2122 0.3232 0.2643 0.2643 0.0111 0.1397 0.1411 0.2225 RMSE 0.0946 0.01587 0.2264	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR 722.4458 166.7632 61.5627	SSIM 0.9663 0.923 0.9315 0.8308 0.9574 0.9574 0.9574 0.9574 0.9574 0.9574 0.9574 0.9574 0.9545 0.95464 0.9598 SSIM 0.9825 0.9771 0.9627	RMSE 0.0382 0.0696 0.1104 0.181 0.0643 0.1214 0.2098 0.2167 0.0382 0.0382 0.0720 RMSE 0.0267 0.0556 0.0370	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine SNR 3563.8233 3243.0239 1524.4889	SSIM 0.9889 0.9890 0.9731 0.9731 0.9850 0.9768 0.9771 0.9872 0.9872 0.9889 0.9889 0.9890 SSIM 0.9939 0.9938 0.9938	Sig RMSE 0.0706 0.0721 0.0961 0.1154 0.0864 0.0864 0.0864 0.0864 0.0864 0.0519 0.0519 0.0545 0.0792	nal Doppler SNR 506.6253 105.2425 101.1128 37.6373 200.1970 71.5805 22.5990 8.7569 8.86.7644 443.8720 4459.1724 1459.1724 1459.1724 1459.1724 1459.1724 1459.1724 138.06.2839 213.4945 139.5169	SSIM 0.9766 0.9555 0.9456 0.9106 0.9359 0.8715 0.7998 0.9760 0.9760 0.9576 SSIM 0.9829 0.9623 0.9572	RMSE 0.0130 0.0224 0.0255 0.0454 0.0205 0.0344 0.0594 0.03940 0.0138 0.0136 0.0224 RMSE 0.0103 0.0103 0.0103	Epr 1 SNR 581.3284 473.8570 440.0385 145.5668 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004 515.3936	SSIM 0.9837 0.9843 0.9843 0.9837 0.9802 0.9803 0.9802 0.9803 0.9804 0.9802 0.9803 0.9804 0.9802 0.9841 0.9841 0.9842 0.9841 0.9881 0.9881 0.9881	RMSE 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9658 476.6276 Epr 2 SNR 727.2110 510.0676 517.6145	SSIM 0.9841 0.9841 0.9805 0.9840 0.9840 0.9840 0.9876 0.9876 0.9876 0.9844 0.9865 SSIM 0.9893 0.9893 0.9893	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm BIOR22 Method Hard Soft	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal	Level 5 6 5 6 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 302.5134 76.7110 32.1897 132.5825 55.5109 88.4361 311.0608 307.8672 120.8063 Blocks SNR 694.6432 242.2129 115.1432 48.8145	SSIM 0.9324 0.9256 0.8850 0.8495 0.9100 0.8488 0.8962 0.9401 0.9430 0.9431 0.9312 0.9323 SSIM 0.9533 0.9593 0.95935 0.9172 0.8791	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2643 0.0811 0.3275 RMSE 0.0587 0.2524 0.325	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR 722.4458 166.7632 61.5627 15.1070	 SSIM 0.9663 0.9315 0.9315 0.9315 0.93140 0.9574 0.9574 0.9704 0.9704 0.9664 0.9598 SSIM 0.9825 0.9257 0.9617 0.8702 	RMSE 0.0382 0.0696 0.1104 0.0433 0.1214 0.2055 0.0432 0.0382 0.0382 0.0382 0.0382 0.0362 0.0265 0.0266 0.0267 0.0266 0.0267 0.0267 0.0267 0.0267 0.0267 0.0267	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine SNR 3563.8823 3243.0239 1524.4889 940.8218	SSIM 0.9889 0.9902 0.9731 0.9850 0.9748 0.9778 0.9770 0.9772 0.9930 0.9890 0.9892 0.9893 0.9938 0.9938 0.9938	Sig RMSE 0.0706 0.0721 0.0961 0.1154 0.0864 0.0874 0.0974 0.0519 0.0545 0.0792 RMSE 0.0519 0.0545 0.0792 0.0545	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 825.5900 8.7569 8.86.7644 443.8720 459.1724 164.5700 nal Doppler SNR 806.2839 213.4945 139.5169 44.0760	SSIM 0.9766 0.9555 0.9456 0.9456 0.9456 0.9456 0.9456 0.9576 0.9576 0.9576 0.9576 0.9576 0.9576 0.9523 0.9623 0.9623 0.9572 0.9572 0.9197	RMSE 0.0130 0.0224 0.0285 0.0344 0.0554 0.0384 0.0138 0.0138 0.0138 0.0138 0.0138 0.0138 0.0138 0.0138 0.0138 0.0138 0.0138 0.0198 0.0194 0.01421	Epr 1 SNR 581.3284 473.8570 145.5568 547.6186 300.7634 123.1603 145.57662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004 515.3936 211.1037	SSIM 0.9837 0.9843 0.9837 0.9803 0.9802 0.9841 0.9841 0.9841 0.9841 0.9841 0.9845 0.9841 0.9835 0.9846 0.9881 0.9886 0.9881 0.9876 0.9885	RMSE 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9858 476.6276 Epr 2 SNR 727.2110 510.0676 510.6676 517.6145 254.5368	SSIM 0.9841 0.9805 0.9840 0.9841 0.9843 0.9844 0.9846 0.9847 0.9846 0.9846 0.9847 0.9876 0.9886 0.9883 0.9883 0.9883 0.9886 0.9886 0.9886	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Firm BIOR22 Method Hard Soft Garotte	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal Universal	Level 5 6	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 86.57886 84.6403 958.4361 311.0608 307.8672 120.8063 Blocks SNR 694.6432 242.2129 115.1432 48.8145 234.4160	SSIM 0.9324 0.9256 0.8850 0.8495 0.9109 0.9440 0.9324 0.9325 0.9109 0.9430 0.9430 0.9430 0.9430 0.9430 0.9430 0.9505 0.9505 0.9507 0.8507 0.9508 0.9505 0.9505 0.9505 0.9505 0.9505 0.9505 0.9505	RMSE 0.1422 0.2169 0.2762 0.3232 0.3232 0.2628 0.2628 0.2643 0.0811 0.1397 0.1411 0.2225 RMSE 0.0946 0.1587 0.3244 0.3177 0.1602	Bumps SNR 359.13255 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR 722.4458 166.7632 16.15627 15.1070 235.2659	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9100 0.8138 0.7833 0.9704 0.9664 0.9858 SSIM 0.9858 0.9771 0.98702 0.9771	RMSE 0.0382 0.0696 0.1104 0.0696 0.131 0.0643 0.2167 0.0452 0.0432 0.0420 0.0382 0.0720 RMSE 0.0566 0.0570 0.0560 0.0570	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine SNR 3563.8823 3243.0239 1524.4889 940.8218 2165.1882	SSIM 0.9889 0.9871 0.9871 0.9872 0.9768 0.9778 0.9872 0.9889 0.9890 SSIM 0.9938 0.9938 0.9938 0.9938 0.9781 0.9938 0.9781	Sig RMSE 0.0706 0.0721 0.0961 0.0961 0.0154 0.0154 0.0548 0.0707 0.0723 Sig RMSE 0.0519 0.0545 0.0792 0.00545 0.0792 0.00545	nal Doppler SNR 506.6253 105.2425 101.1128 37.6373 200.1970 71.5805 22.5990 886.7644 443.8720 459.1724 164.5700 nal Doppler SNR 806.2839 213.4945 139.5169 44.0760 309.027	SSIM 0.9766 0.9456 0.9456 0.9456 0.9456 0.9456 0.9457 0.9457 0.9760 0.9576 0.9576 0.9818 0.9818 0.9818 0.9576 0.9823 0.9622 0.9627 0.9197 0.9726	RMSE 0.0130 0.0224 0.0334 0.0584 0.0454 0.0594 0.0304 0.0100 0.0334 0.0138 0.0138 0.0138 0.0124 RMSE 0.0108 0.0124 0.0124 0.0124	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004 515.3936 211.1037 629.2516	SSIM 0.9837 0.9843 0.9803 0.9802 0.9802 0.9802 0.9840 0.9840 0.9841 0.9861 0.9849 0.9881 0.9881 0.9881 0.9881 0.9881	RMSE 0.0001 0.0002 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9858 476.6276 Epr 2 SNR 727.2110 510.0676 517.6145 254.5368 598.7811	SSIM 0.9841 0.985 0.9805 0.9840 0.9841 0.9842 0.9844 0.9846 0.9847 0.9846 0.9847 0.9846 0.9847 0.9846 0.9847 0.9886 0.9886 0.9893 0.9886 0.9882 0.9888	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm BIOR22 Method Hard Soft Garotte	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403 958.4361 311.0608 307.8672 120.8063 Blocks SNR 694.6432 242.2129 115.1432 242.2129 115.1432 234.4160 96.0851 10.0011	SSIM 0.9324 0.9256 0.8850 0.8495 0.8495 0.8484 0.8926 0.8940 0.9109 0.9430 0.9312 0.9329 SSIM 0.9593 0.95912 0.98791 0.98791 0.98792 0.98791 0.9426 0.9126	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.3232 0.2643 0.2643 0.2141 0.2225 RMSE 0.0946 0.1587 0.2624 0.3177 0.1602 0.2441	Bumps SNR 359.13255 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR 722.4458 166.7632 61.5627 15.1070 235.2659 46.5696	SSM 0.9663 0.9523 0.9315 0.8308 0.9574 0.910 0.8138 0.9704 0.9709 0.9664 0.9709 0.9664 0.9709 0.9625 0.9711 0.9672 0.9778 0.9708	RMSE 0.0382 0.0696 0.1104 0.1881 0.0432 0.2167 0.0255 0.0432 0.0720 RMSE 0.0567 0.0567 0.0567 0.0567 0.0567 0.0567 0.0567 0.0570	Heavisine SNR 1941.8538 1870.2313 1870.2313 1022.5786 758.6540 764.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine SNR 3563.8823 3243.0239 1524.4889 940.8218 2165.1882 1497.4779	SSIM 0.9889 0.9820 0.9821 0.9820 0.9820 0.9820 0.9820 0.9771 0.9870 0.9771 0.9870 0.9978 0.9889 0.9889 0.9890 0.9938 0.9881 0.9781 0.9781	Sig RMSE 0.0706 0.0721 0.0961 0.0154 0.01154 0.0548 0.01154 0.0548 0.0548 0.0549 0.0549 0.0579 0	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990 886.7649 443.8720 459.1724 164.5700 nal Doppler SNR 806.2839 213.4945 139.5169 43.0720 309.9027 87.5617	SSIM 0.9766 0.9555 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9372 0.9576 0.9829 0.9829 0.9624 0.9576 0.9829 0.9627 0.9107 0.9176 0.9172 0.9173	RMSE 0.0130 0.0224 0.0255 0.0454 0.0205 0.0304 0.0594 0.0594 0.0138 0.0138 0.0124 PMSE 0.0103 0.0103 0.0104 0.0124 0.0124 0.0124 0.0124 0.0124	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004 515.3936 211.1037 629.2516 419.9459	SSIM 0.9837 0.9843 0.9833 0.9802 0.9802 0.9802 0.9840 0.9881 0.9881 0.9881 0.9881 0.9881 0.9881 0.9882 0.9885 0.9875 0.9858	RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9658 476.6276 Epr 2 SNR 727.2110 510.0676 517.6145 254.5368 598.7811 441.6324	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9863 0.9844 0.9865 SSIM 0.9883 0.9883 0.9883 0.9883 0.9888 0.9880	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.00012 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Firm BIOR22 Method Hard Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 302,5134 128,3804 76,7110 32,1897 132,5825 55,5109 85,7986 84,6403 958,4361 311,0608 907,8672 120,8063 Blocks SNR 694,6432 242,2129 115,1432 44,8610 96,0851 85,5984 85,5984 85,5984 15,5109 10,000 11,00	SSIM 0.9324 0.9256 0.8495 0.8495 0.8496 0.9400 0.9400 0.9401 0.9420 0.9239 SSIM 0.9593 0.9593 0.9595 0.9172 0.8791 0.8792 0.9295	RMSE 0.1422 0.2169 0.2762 0.3232 0.2628 0.2643 0.2814 0.1397 0.1411 0.2225 RMSE 0.0344 0.3946 0.3447 0.3447 0.3460 0.3461 0.3462 0.3464 0.3467 0.3464 0.3467 0.2624 0.2624 0.2624 0.2625	Bumps SNR 359.1325 103.6527 37.1811 10.9000 119.6250 30.463 9.4540 8.4519 807.2213 274.0819 807.2213 274.0819 805.6455 Bumps 50.4555 Bumps 50.4555 166.7632 61.5627 15.1070 235.2659 46.5696 9.4880 1.51.57	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.9140 0.9140 0.9140 0.9749 0.9664 0.96598 SSIM 0.9825 0.9771 0.9617 0.8702 0.8702 0.9778 0.9778	RMSE 0.0382 0.0696 0.1104 0.1881 0.0643 0.1214 0.2055 0.0432 0.0382 0.0255 0.0432 0.0255 0.0432 0.0566 0.0870 0.1639 0.0462 0.0462 0.0462 0.0462	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine SNR 3563.8823 3243.0239 1524.4889 940.8218 2165.1882 1497.4779 783.1875	SSIM 0.9889 0.9890 0.9821 0.9731 0.9800 0.9821 0.9781 0.9781 0.9782 0.9782 0.9890 0.9890 0.9890 0.9890 0.9890 0.9890 0.9938 0.9938 0.9938 0.9938 0.9938 0.9938 0.9938 0.9938 0.9938 0.9938 0.9938 0.9938 0.9939 0.9938 0.9938 0.9938 0.9939 0.9938 0.9938 0.9938 0.9939 0.9938	Sig RMSE 0.0706 0.0721 0.0961 0.0961 0.0961 0.0961 0.0961 0.0651 0.0651 0.0723 Sig RMSE 0.0519 0.0545 0.0792 0.0106 0.00655 0.0792 0.00655 0.0792 0.00655 0.0792 0.010655 0.0792 0.010655 0.0792 0.010655 0.01092 0.010555 0.0792 0.010655 0.01092 0.00655 0.0792 0.010655 0.005555 0.005555 0.00555 0.0	nal Doppler SNR 506.6253 105.2425 101.1128 37.8373 200.1970 71.5805 22.5990 8.7569 8.867.644 443.8720 4459.1724 164.5700 nal Doppler SNR 806.2839 213.4945 139.5169 44.0760 309.9027 87.5617 22.7113	SSIM 0.9766 0.9555 0.9456 0.9456 0.9456 0.9456 0.9456 0.930 0.8715 0.93829 0.9576 0.9829 0.9623 0.9572 0.9100 0.9252 0.9170 0.9726 0.9172 0.9723 0.9435 0.8723	RMSE 0.0130 0.0224 0.0255 0.0454 0.0205 0.0334 0.0594 0.0138 0.0138 0.0103 0.0103 0.0103 0.0104 0.0105 0.0104 0.0105 0.0104 0.0105 0.0104 0.0105 0.0105 0.0105	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004 515.3936 211.1037 629.2516 419.9459 123.4859 123.4859	SSIM 0.9837 0.9843 0.9843 0.9803 0.9803 0.9803 0.9844 0.9841 0.9841 0.9841 0.9881 0.9881 0.9881 0.9882 0.9882 0.9858 0.9876	RMSE 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9658 476.6276 Epr 2 SNR 727.2110 510.0676 517.6145 254.5368 598.7841 441.6324 10.5968	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9840 0.9844 0.9865 SSIM 0.9893 0.9893 0.9886 0.9888 0.98880 0.9852 0.98880 0.9852	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0003 0.0001 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002
SWT	BIOR22 Method Hard Soft Hard Hard Firm BIOR22 Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 SNR=200 Universal Universal Universal Heur. SURE	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 302,5134 128,3804 76,7110 32,1897 132,5825 55,5109 85,7986 84,6403 958,4361 311,0608 307,8672 120,8063 Blocks SNR Blocks SNR 694,6432 242,2129 115,1432 44,8145 234,4160 80,0851 85,5984 83,9953	SSIM 0.9324 0.9256 0.8485 0.9100 0.9401 0.9401 0.9401 0.9312 0.9239 0.9503 0.9503 0.9503 0.9503 0.9503 0.9504 0.9504 0.9504 0.9504 0.9505 0.9172 0.9426 0.9165 0.9172 0.9455 0.9172 0.9456 0.9165 0.9165 0.9165 0.916 0.916 0.916 0.9165 0.916 0	RMSE 0.1422 0.2169 0.2762 0.2122 0.2688 0.2643 0.3372 0.2628 0.3411 0.1397 0.1411 0.2225 RMSE 0.0946 0.3417 0.2264 0.3417 0.2644 0.3417 0.2644 0.3417 0.2644 0.2642 0.2480 0.2480 0.2632	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.4643 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR 722.4458 166.7632 61.5627 15.1070 235.2659 46.6596 9.4880 8.4738	SSIM 0.9663 0.9623 0.9315 0.8308 0.9574 0.9140 0.9400 0.9400 0.9598 SSIM 0.9598 SSIM 0.9598 0.9571 0.9617 0.8702 0.9778 0.89450 0.9450 0.9450	RMSE 0.0382 0.0596 0.1104 0.1881 0.0210 0.0255 0.0382 0.0320 0.0320 0.0320 0.0322 0.0320 0.0320 0.0320 0.0320 0.0320 0.0320 0.0320 0.0320 0.0320 0.0320 0.0320 0.0320 0.0320 0.0420 0.1044 0.2093 0.2104	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine SNR 3563.8223 3243.0239 1524.4889 940.8218 2165.1882 1497.4779 738.31875 738.31875	SSIM 0.9889 0.9890 0.9821 0.9731 0.9850 0.9800 0.9701 0.9768 0.9771 0.9782 0.9890 0.9889 0.9890 0.9889 0.9938 0.9938 0.9938 0.9938 0.9938 0.9938 0.9937 0.9774 0.9938 0.9938 0.9938 0.9938 0.9939 0.9774	Sig RMSE 0.0706 0.07021 0.0721 0.0721 0.0707 0.0747 0.01121 0.0545 0.0707 0.0773 Sig RMSE 0.0659 0.0659 0.0659 0.06799 0.00799 0.00792 0.00595 0.005555 0.005555 0.005555 0.005555 0.005555555 0.0055555	nal Doppler SNR 506.6253 105.2425 101.1128 37.6373 200.1970 71.5805 22.5990 8.7569 8.86,7644 443.8720 4459.1724 4459.1724 4459.1724 1345.1769 213.4945 139.5169 213.4945 139.5169 213.4945 139.5169 244.0760 309.9027 87.5617 22.7113 8.7760	 SSIM 0.9765 0.9456 0.9106 0.9655 0.9456 0.9106 0.9623 0.9576 0.9576 0.9576 0.9576 0.9623 0.9623 0.9623 0.9572 0.91726 0.9435 0.8723 0.9435 0.8723 0.9435 	RMSE 0.0130 0.0224 0.0285 0.0454 0.0304 0.0594 0.0594 0.0334 0.0594 0.0334 0.0138 0.0138 0.0124 0.0198 0.0198 0.0194 0.0194 0.0193 0.0194 0.0194 0.0194 0.0194 0.0194 0.0194 0.0194 0.0194 0.0194 0.0194 0.0194 0.0194 0.0194	Epr 1 SNR 581.3284 473.8570 440.0385 145.5668 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004 515.3936 211.1037 629.2516 419.9459 123.4859 8.4741	SSIM 0.9833 0.9843 0.9803 0.9803 0.9802 0.9833 0.9840 0.9833 0.9841 0.9835 0.9841 0.9835 0.9881 0.9881 0.9882 0.9876 0.9882 0.9876 0.9882 0.98844 0.98844 0.98844	RMSE 0.0001 0.0002 0.0001 0.0002 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9658 CPF 2 SNR 727.2110 510.0676 517.6145 254.5368 598.7811 441.6324 101.5968 5.9139	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9803 0.9424 0.9865 0.9865 0.9865 0.9865 0.9883 0.9893 0.9886 0.9852 0.9888 0.9880 0.9852 0.9888 0.9880	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002
SWT	BIOR22 Method Hard Soft Hard Hard Firm BIOR22 Method Hard Soft Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX SNR=200 Selection Universal Universal Universal Heur. SURE	Level 5 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 84.54361 311.0608 307.8672 120.8063 Blocks SNR 694.6432 242.2129 115.1432 48.8145 234.4160 96.0851 85.5984 83.9963 2129.9909	SSIM 0.9324 0.9256 0.8850 0.8495 0.8495 0.8495 0.9100 0.9430 0.9430 0.9430 0.9430 0.9430 0.9430 0.9432 0.9505 0.9172 0.8505 0.9172 0.9466 0.9135 0.9138 0.9138	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.2323 0.2624 0.2623 0.1411 0.2252 0.1411 0.2252 0.1411 0.2252 0.1587 0.1687 0.2624 0.2164 0.2402 0.2632 0.2632 0.2634 0.2635	Bumps SNR 359.1325 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR 722.4458 166.7632 61.5627 15.1070 235.2659 46.5696 9.4880 8.4738 149.9861	SSIM 0.9663 0.9623 0.9523 0.9315 0.8308 0.9574 0.9140 0.9410 0.9640 0.9598 SSIM 0.9598 SSIM 0.9425 0.9771 0.9617 0.9717 0.9778 0.9425 0.94710 0.94710 0.94710 0.94710 0.9471000000000000000000000000000000000000	RMSE 0.0382 0.0596 0.1104 0.1821 0.0265 0.0382 0.0320 0.0322 0.0382 0.0267 0.0267 0.0566 0.0567 0.0566 0.0567 0.0467 0.0467 0.0467 0.0467 0.04639 0.0464 0.04639 0.24163 0.24163 0.2163 0.2163 0.2163	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4766 3235.4991 1928.4188 1851.7938 Heavisine SNR 3563.8823 3243.0239 1524.4889 940.8218 2165.1882 1497.4779 738.1875 736.3482	SSIM 0.9889 0.9821 0.9731 0.9820 0.9731 0.9820 0.9781 0.9800 0.9782 0.9823 0.9889 0.9890 SSIM 0.9938 0.9938 0.9938 0.9761 0.9776 0.9786 0.9787 0.9786 0.9787 0.9786 0.9786 0.9787 0.9788 0.9786 0.9787 0.9786 0.9776 0.9776 0.9776	Sig RMSE 0.0706 0.0721 0.0721 0.0721 0.0721 0.0721 0.0744 0.0707 0.0545 0.0703 Sig RMSE 0.0545 0.01133 0.01133 0.01133 0.01133 0.01133 0.01133 0.01133 0.01135 0.011555 0.011555 0.01155 0.011555 0.011555 0.011555 0.01	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 825.5900 8.7569 8.86.7644 443.8720 459.1724 164.5700 nal Doppler SNR 806.2839 213.4945 139.5169 44.0760 309.9027 87.5617 22.7113 8.7706	SSIM 0.9766 0.9456 0.9456 0.9456 0.9456 0.9456 0.9457 0.9757 0.9760 0.9576 0.9858 0.9857 0.9623 0.9623 0.9623 0.9623 0.9623 0.9623 0.9623 0.9623 0.9624 0.9457 0.9726 0.9457 0.9726 0.9457 0.9457 0.9457 0.9457 0.9457 0.9457 0.9555 0.9456 0.9557 0.9757 0.9756 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9456 0.9457 0.9456 0.9457 0.94770 0.94770 0.94770 0.94770 0.94770 0.94770000000000000000000000000000000000	RMSE 0.0130 0.0224 0.0454 0.0594 0.0594 0.0594 0.0130 0.0594 0.0138 0.0138 0.0138 0.0138 0.0124 RMSE 0.0108 0.0124 0.0128 0.0124 0.0128 0.0128 0.0124 0.0128 0.0124 0.0128 0.0124 0.0128 0.0128 0.0124 0.0128 0.0124 0.0124 0.0124 0.0124 0.0124 0.0124 0.0124 0.0124 0.0124 0.0124 0.0125 0.0126 0.0127	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004 515.3936 211.1037 629.2516 419.9459 123.4859 8.4741 1090.4738	SSIM 0.9837 0.9843 0.9843 0.9803 0.9803 0.9803 0.9803 0.9803 0.9802 0.9833 0.9841 0.9835 0.9842 0.9836 0.9841 0.9837 0.9862 0.9876 0.9825 0.9876 0.9824 0.9844 0.9466 0.9844 0.9466 0.9844 0.9466	RMSE 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0002 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9858 476.6276 Epr 2 SNR 727.2110 510.0676 517.6145 254.5368 598.7811 441.6324 101.5968 5.9139 1277.021	SSIM 0.9841 0.9805 0.9805 0.9806 0.9807 0.9803 0.9803 0.9841 0.9803 0.9844 0.9876 0.9876 0.9876 0.9883 0.9883 0.9883 0.9888 0.9888 0.9888 0.9882 0.9882 0.9822 0.9462 0.9962	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0003 0.0002 0.0003 0.0003 0.0001
SWT	BIOR22 Method Hard Soft Garotte Hard Firm BIOR22 Method Hard Garotte Hard Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX SNR=200 Selection Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 84.54361 311.0608 307.8672 120.8063 Blocks SNR 694.6432 242.2129 115.1432 242.2129 115.1432 48.8145 234.4160 96.0851 85.5984 85.5984 239.5935 2129.9909 827.7577	SSIM 0.9324 0.9256 0.8850 0.8495 0.8495 0.9109 0.9440 0.9322 0.9329 SSIM 0.9505 0.9505 0.9505 0.9426 0.9135 0.9145 0.9145 0.9146	RMSE 0.1422 0.2169 0.2762 0.4168 0.2122 0.2028 0.2628 0.2643 0.2643 0.03411 0.2225 RMSE 0.0946 0.1587 0.1687 0.2628 0.2629 0.2644 0.0946 0.1587 0.2640 0.2632 0.2632 0.2643 0.2643 0.2644 0.2645 0.2645 0.2646 0.2647	Bumps SNR 359.13255 103.6527 37.1811 10.9900 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR 722.4458 166.7632 15.1070 235.2659 46.5696 9.4880 8.4738 1469.9861 468.991	SSIM 0.9663 0.9623 0.9523 0.9315 0.8308 0.95740 0.9404 0.9410 0.9664 0.9825 0.9771 0.9664 0.9825 0.9771 0.9778 0.9364 0	RMSE 0.0382 0.0696 0.1104 0.1881 0.0426 0.2167 0.0255 0.0382 0.03720 RMSE 0.0566 0.0556 0.0556 0.0556 0.0556 0.0556 0.0567 0.1639 0.0462 0.1004 0.2093 0.2093 0.2163 0.02163 0.0318 0.0328	Heavisine SNR 1941.8538 1870.2313 1033.6593 720.0404 1284.4093 1022.5786 758.6546 761.9088 2283.4756 3235.4991 1928.4188 1851.7938 Heavisine SNR 3563.8823 3243.0239 1524.4888 2145.1882 1497.4779 783.1875 736.3482 4434.7390 5293.475	SSIM 0.9889 0.9871 0.9821 0.9731 0.9821 0.9800 0.9800 0.9800 0.9800 0.9800 0.9800 0.9800 0.9800 0.9800 0.9800 0.9800 0.9938 0.9938 0.9938 0.9781 0.9782 0.9783 0.9784 0.9780 0.9781 0.9781 0.97931 0.97931 0.9755	Sig RMSE 0.0706 0.0721 0.0721 0.0721 0.0721 0.0721 0.0723 Sig RMSE 0.0703 Sig RMSE 0.0545 0.0703 0.0545 0.0113 0.0113 0.0455 0.0455 0.0455 0.0113 0.0455 0.0455 0.0455 0.0455 0.0113 0.0455 0.045	nal Doppler SNR 506.6253 101.1128 37.6373 200.1970 71.5805 22.5990 886.7644 443.8720 459.1724 164.5700 nal Doppler SNR 806.2839 213.4945 139.5169 44.0760 309.9027 87.5617 22.7113 87.706 1450.9790 585.1196	SSIM 0.9766 0.9456 0.9456 0.9456 0.9456 0.9456 0.9457 0.9760 0.9818 0.9818 0.9757 0.9760 0.9576 0.9623 0.9623 0.9623 0.9623 0.9623 0.9455 0.9726 0.9455 0.9726 0.9455 0.9726 0.9455 0.9726 0.9455 0.9726 0.9455 0.9726 0.9455 0.9726 0.9455 0.9272 0.9455 0.9275 0.9276 0.9275 0.9276 0.9275 0.9276 0.9275 0.9255 0.9275 0.9255 0.9275 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.9255 0.92555 0.92555 0.92555 0.92555 0.92555 0.92555 0.92555 0.92555 0.92555 0.92555 0.92555 0.925555 0.9255555 0.9255555555555555555	RMSE 0.0130 0.0224 0.0255 0.0454 0.0205 0.0334 0.0594 0.0100 0.0138 0.0138 0.0124 RMSE 0.0103 0.0194 0.0124 RMSE 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0145 0.0390 0.0077 0.0121	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 433.747 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004 515.3936 211.1037 629.2516 419.9459 123.4859 8.4741 1090.4733 729.1466	SSIM 0.9833 0.9774 0.9833 0.9774 0.9803 0.9802 0.9802 0.9803 0.9802 0.9802 0.9803 0.9802 0.9802 0.9814 0.9825 0.9875 0.9864 0.9875 0.9875 0.9875 0.9864 0.9865 0.9865 0.9865 0.9865 0.9865 0.9865 0.9865 0.9865 0.9865 0.9865 0.9865 0.9865 0.9865 0.9865	RMSE 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 5.9097 786.0141 570.2064 415.9858 476.6276 Epr 2 SNR 727.2110 510.0676 517.6145 254.5368 598.7811 441.6324 101.5968 5.9139 1277.021	SSIM 0.9841 0.9842 0.9837 0.9805 0.9840 0.9841 0.9842 0.9844 0.9876 0.9844 0.9876 0.9846 0.9847 0.9876 0.9886 0.9883 0.9886 0.9882 0.9882 0.9462 0.9462	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0012 0.0002
SWT	BIOR22 Method Hard Soft Garotte Hard Hard Firm BIOR22 Method Hard Garotte Hard Garotte Hard	SNR=100 Selection Universal Universal Heur. SURE MINIMAX MINIMAX Universal Universal Universal Heur. SURE MINIMAX	Level 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5	Blocks SNR 302.5134 128.3804 76.7110 32.1897 132.5825 55.5109 85.7986 84.6403 958.4361 311.0608 307.8672 120.8063 Blocks SNR 694.6432 242.2129 115.1432 48.8145 96.0851 85.5984 83.9953 2129.9909 827.7577 730.5664 120.9051 120.9055 120.9051 120.90555 120.9055 120.9055 120.9055 120.9055 120.9055 120.905	SSIM 0.9324 0.9256 0.8495 0.8495 0.9100 0.9400 0.9401 0.9401 0.9420 0.9312 0.9505 0.9172 0.8791 0.9505 0.9172 0.8791 0.9426 0.9426 0.9426 0.9468 0.9661	RMSE 0.1422 0.2169 0.2762 0.3232 0.2628 0.2643 0.0307 0.1411 0.2255 RMSE 0.0344 0.1397 0.1411 0.2255 RMSE 0.03417 0.2644 0.2642 0.2643 0.2644 0.2645 0.2654 0.0566 0.0581 0.0916	Bumps SNR 359.1325 103.6527 37.1811 10.9000 119.6250 30.6463 9.4540 8.4519 807.2213 274.0819 354.2006 95.6455 Bumps SNR 722.4458 166.7632 61.5627 15.1070 15.1070 46.5696 9.4880 8.4738 4.459.9861 4459.9861	SSIM 0.9663 0.9523 0.9315 0.8308 0.9574 0.9574 0.9400 0.9400 0.9644 0.9598 SSIM 0.9625 0.9771 0.9677 0.9677 0.9677 0.9450 0.9376 0.9384 0.9836 0.9837	RMSE 0.0382 0.0696 0.1104 0.1881 0.0425 0.0382 0.0382 0.0325 0.0326 0.0326 0.0556 0.0556 0.0525 0.0422 0.0567 0.05670 0.1639 0.1642 0.1004 0.2033 0.2163 0.0188 0.0339 0.0265	Heavisine SNR 1941.8538 1870.2313 1870.2313 1870.2313 1870.2313 1870.2313 1870.2313 1870.2313 1872.3786 1872.3786 1928.4188 1851.7938 Heavisine SNR 3263.8823 3243.0239 1524.4889 2165.1882 1497.4779 783.1875 736.3482 4434.7390 5239.3475 3449.0884	SSIM 0.9889 0.9871 0.9871 0.9820 0.9821 0.9820 0.9820 0.9820 0.9820 0.9820 0.9820 0.9820 0.9820 0.9820 0.9830 0.9931 0.9771 0.9781 0.9770 0.9931 0.9935 0.9937	Sig RMSE 0.0706 0.0721 0.0961 0.0961 0.0961 0.0964 0.0974 0.0651 0.0723 Sig RMSE 0.0519 0.0548 0.0519 0.0545 0.0545 0.0706 0.0545 0.0545 0.0707 0.0548 0.0551 0.0551 0.0555 0.0706 0.0551 0.0555 0.0706 0.0555 0.0707 0.0555 0.0707 0.0555 0.0707 0.0555 0.0707 0.0725 0.0707	nal Doppler SNR 506.6253 165.2425 101.1128 37.6373 200.1970 71.5805 22.5990 886.7644 443.8720 459.1724 164.5700 nal Doppler SNR 806.2839 213.495 139.5169 309.9027 87.5617 22.7113 8.7706 1450.9790 585.1196 737.0599	SSIM 0.9766 0.9455 0.9455 0.9456 0.9456 0.9456 0.9457 0.9757 0.9760 0.9576 0.9829 0.9623 0.9572 0.9197 0.9197 0.9197 0.9193 0.8013 0.8013 0.8013 0.8013 0.9873	RMSE 0.0130 0.0224 0.0255 0.0454 0.0205 0.0304 0.0594 0.0594 0.0138 0.0138 0.0124 0.0103 0.0124 0.0121 0.0146 0.0304 0.0594 0.0421 0.0165 0.0304 0.0593 0.0077 0.0121 0.0121	Epr 1 SNR 581.3284 473.8570 440.0385 145.5568 547.6186 300.7634 123.1603 8.4374 731.4712 569.7662 467.0613 454.1600 Epr 1 SNR 708.7095 581.7004 515.3936 211.1037 629.2516 419.9459 123.4859 8.4741 1090.4732 729.1466 578.4883	SSIM 0.9837 0.9803 0.9803 0.9803 0.9802 0.9802 0.9840 0.9840 0.9861 0.9861 0.9885 0.9875 0.9875 0.9875 0.9875 0.9875 0.9875 0.9875 0.9875 0.9875 0.9885 0.9985 0.9985 0.9985 0.9985 0.9985 0.9985 0.9985 0.9985 0.9985 0.99	RMSE 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0002 0.0001 0.0002 0.0001 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001 0.0001	Epr 2 SNR 530.6969 464.1594 419.3689 187.4941 493.9512 370.0135 97.8830 786.0141 570.2064 415.9858 476.6276 Epr 2 SNR 727.2110 510.0676 517.6145 254.5368 598.7811 441.6324 101.5968 5.9139 1277.021 805.3058 813.9672	SSIM 0.9841 0.9864 0.9837 0.9805 0.9840 0.9841 0.9876 0.9844 0.9876 0.9844 0.9865 SSIM 0.9893 0.9883 0.9883 0.9883 0.9882 0.9882 0.9882 0.9882 0.9822 0.9622 0.9622 0.9622 0.9622 0.9625 0.96555 0.96555 0.96555 0.96555 0.96555 0.96555 0.96555 0.96555 0.965555 0.96555555555555555555555555555555555555	RMSE 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.0001 0.0001

Table S4. Performance of the SWT at decomposition levels 5 and 6 with the bior2,2 wavelet for 6 thresholding combinations. The tables give the performance of each combination in terms of SNR, SSIM, and RMSE in order of increasing starting SNR (10, 50, 100, 200) of the noisy test signal. Results are presented for the following test signals: blocks, bumps, heavisine, doppler, 1st EPR test signal, and 2nd EPR test signal. Method refers to the thresholding form, while selection refers to the means of calculating the threshold value.

												Sig	gnal								
	BIOR24	SNR=10		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	46.5057	0.7609	0.3573	48.5285	0.7775	0.1005	263.5782	0.9549	0.1910	91.3612	0.9132	0.0303	210.8588	0.9204	0.0002	219.1190	0.9178	0.0002
			6	27.5225	0.7627	0.4575	19.4970	0.7778	0.1531	309.9567	0.9560	0.1760	73.0578	0.9121	0.0336	196.5427	0.9431	0.0002	243.6321	0.9455	0.0002
	Soft	Universal	5	27.4816	0.7238	0.4570	8.4339	0.6659	0.2174	259.5529	0.9539	0.1924	39.2097	0.8778	0.0457	170.2713	0.9192	0.0002	171.8807	0.9155	0.0003
			6	13.6970	0.7119	0.6256	3.3848	0.5859	0.3103	268.3856	0.9521	0.1887	22.2265	0.8582	0.0587	67.0162	0.9348	0.0003	76.4914	0.9333	0.0004
	Garotte	Universal	5	30.5305	0.7320	0.4350	16.9048	0.7255	0.1614	259.9769	0.9540	0.1922	53.4624	0.8928	0.0394	192.8349	0.9195	0.0002	203.4115	0.9165	0.0002
SWT	ourouo	onnoroar	6	16.8405	0.7285	0.5695	6.2503	0.6656	0.2445	274.0844	0.9525	0.1867	34.7351	0.8826	0.0476	131.1982	0.9399	0.0002	157.3984	0.9399	0.0003
	Hard	Heur SURE	5	74.0756	0.7845	0.2836	9.8289	0.6630	0.2079	273.1135	0.9504	0.1881	21.6943	0.8452	0.0609	111.4474	0.9186	0.0002	94.4266	0.9135	0.0004
	mara	noun cont	6	78.3572	0.8167	0.2753	8.9718	0.7063	0.2128	377.5119	0.9578	0.1605	8.8492	0.7835	0.0913	9.1445	0.9004	0.0007	6.4515	0.8861	0.0012
	Hard	MINIMAX	5	91.3278	0.7918	0.2584	92.7938	0.8001	0.0741	222.9178	0.9194	0.2116	138.8789	0.9198	0.0248	182.9861	0.9091	0.0002	193.7320	0.9088	0.0002
	mara		6	58.4856	0.8032	0.3193	56.5581	0.8265	0.0935	314.9986	0.9315	0.1804	130.6104	0.9296	0.0254	230.4127	0.9437	0.0002	270.7126	0.9462	0.0002
	Firm	ΜΙΝΙΜΔΧ	5	45.9741	0.7590	0.3583	42.6750	0.7748	0.1065	269.0971	0.9546	0.1890	89.5800	0.9120	0.0306	206.1864	0.9200	0.0002	216.8272	0.9178	0.0002
			6	28.4869	0.7662	0.4489	17.2957	0.7715	0.1602	317.4938	0.9552	0.1738	68.2772	0.9099	0.0346	177.7018	0.9450	0.0002	237.3486	0.9452	0.0002
				:								Sig	gnal								
	BIOR24	SNR=50		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	162.3575	0.8830	0.1935	237.1333	0.9281	0.0467	998.4312	0.9792	0.0981	380.3219	0.9661	0.0150	498.8530	0.9751	0.0001	439.8185	0.9755	0.0002
	mara	onnoroar	6	73.9978	0.8819	0.2860	61.3896	0.9141	0.0894	1127.1018	0.9809	0.0931	179.6432	0.9523	0.0217	437.5078	0.9782	0.0001	445.8799	0.9826	0.0002
	Soft	Universal	5	53.3718	0.8318	0.3310	27.8743	0.8780	0.1267	689.4479	0.9733	0.1180	91.2508	0.9348	0.0302	413.0300	0.9748	0.0001	408.3364	0.9753	0.0002
	0011	onversar	6	23.6750	0.8035	0.4854	6.9648	0.7367	0.2295	549.7399	0.9681	0.1322	43.3192	0.9114	0.0428	145.2064	0.9717	0.0002	191.3154	0.9762	0.0002
	Garotte	Universal	5	79.1023	0.8547	0.2739	82.7753	0.9152	0.0772	764.1955	0.9756	0.1123	167.0381	0.9504	0.0225	484.1802	0.9751	0.0001	441.7916	0.9755	0.0002
S/M/T	Garotte	Universal	6	36.0533	0.8360	0.4004	17.2990	0.8337	0.1578	697.7693	0.9724	0.1180	84.0135	0.9352	0.0312	291.2591	0.9747	0.0001	367.3591	0.9801	0.0002
0001	Hord	Hour SUDE	5	92.0969	0.8639	0.2547	10.0116	0.7706	0.2056	671.1148	0.9730	0.1199	22.9789	0.8671	0.0592	148.4501	0.9726	0.0002	124.8375	0.9727	0.0003
	паги	Heur. SUKE	6	91.6669	0.8914	0.2550	9.0417	0.7584	0.2116	746.6795	0.9745	0.1141	8.9436	0.7964	0.0910	9.2966	0.9345	0.0007	6.5690	0.9310	0.0012
	Linud		5	314.8996	0.8966	0.1396	447.4117	0.9343	0.0341	981.9046	0.9690	0.0998	605.3142	0.9732	0.0119	509.3342	0.9738	0.0001	500.6672	0.9742	0.0002
	паги		6	173.8049	0.9118	0.1875	164.6313	0.9352	0.0559	1493.6221	0.9800	0.0808	454.5650	0.9713	0.0137	508.8838	0.9807	0.0001	466.8390	0.9834	0.0002
	Firm		5	155.2147	0.8817	0.1976	223.2248	0.9278	0.0481	977.4594	0.9790	0.0993	348.6904	0.9650	0.0157	404.3591	0.9752	0.0001	316.5486	0.9756	0.0002
	FIIM	WIINIWAA	6	71.7986	0.8794	0.2895	53.3518	0.9089	0.0956	1096.7996	0.9802	0.0943	184.6406	0.9544	0.0214	423.2466	0.9782	0.0001	446.5288	0.9825	0.0002
				•								Sig	nal								
	BIOR24	SNR=100		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	316.3572	0.9302	0.1398	431.2842	0.9621	0.0350	2041.8418	0.9892	0.0690	749.1271	0.9803	0.0107	601.2888	0.9835	0.0001	560.9492	0.9840	0.0001
			6	117.8724	0.9157	0.2273	78.3269	0.9411	0.0794	1994.8557	0.9895	0.0696	293.2134	0.9663	0.0171	557.2437	0.9856	0.0001	501.8069	0.9870	0.0002
	Soft	Universal	5	81.4734	0.8844	0.2688	45.6103	0.9331	0.1008	1098.5701	0.9826	0.0933	145.2900	0.9551	0.0240	529.6500	0.9834	0.0001	493.5934	0.9838	0.0002
			6	31.1940	0.8377	0.4250	8.6091	0.7844	0.2091	765.4946	0.9738	0.1120	54.2388	0.9250	0.0384	196.9947	0.9793	0.0002	268.8277	0.9827	0.0002
	Garotte	Universal	5	142.2422	0.9096	0.2055	157.4018	0.9566	0.0568	1388.2620	0.9857	0.0832	323.8502	0.9703	0.0162	592.1742	0.9836	0.0001	531.8295	0.9840	0.0002
SWT			6	52.4701	0.8736	0.3338	22.9949	0.8774	0.1384	1104.6980	0.9815	0.0937	114.7821	0.9475	0.0268	392.1839	0.9821	0.0001	455.8287	0.9856	0.0002
0	Hard	Heur SURE	5	92.3863	0.8963	0.2534	9.9014	0.8119	0.2063	800.7370	0.9770	0.1092	22.9548	0.8709	0.0592	157.1476	0.9809	0.0002	127.1961	0.9810	0.0003
	. Iai a	noun cont	6	91.0072	0.9073	0.2550	8.9159	0.7800	0.2127	820.3453	0.9782	0.1081	8.9564	0.7986	0.0909	9.3152	0.9409	0.0007	6.5677	0.9360	0.0012
	Hard	MINIMAX	5	917.9456	0.9385	0.0827	888.9350	0.9674	0.0243	2179.6339	0.9852	0.0664	1174.1633	0.9846	0.0086	770.9487	0.9837	0.0001	804.4988	0.9840	0.0001
			6	279.6157	0.9374	0.1480	239.5332	0.9582	0.0463	3227.1873	0.9917	0.0548	704.3728	0.9804	0.0111	599.0050	0.9863	0.0001	617.2707	0.9879	0.0001
	Firm	MINIMAX	5	322.2700	0.9291	0.1383	451.3934	0.9633	0.0341	2042.4828	0.9893	0.0688	709.8079	0.9801	0.0110	438.2359	0.9836	0.0001	580.0236	0.9843	0.0001
			6	111.1729	0.9142	0.2331	73.1108	0.9389	0.0822	1963.2975	0.9896	0.0701	282.7801	0.9670	0.0173	531.0351	0.9850	0.0001	524.7500	0.9872	0.0002
			-									Sig	nal								
	BIOR24	SNR=200		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE

| Method | . | | | | | | |
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| Methou | Selection | Level | SNR | SSIM | RMSE | SNR | SSIM | RMSE
 | SNR
 | SSIM
 | RMSE | SNR | SSIM | RMSE
 | SNR | SSIM
 | RMSE | SNR | SSIM | RMSE |
| Hard | Universal | 5 | 697.7270 | 0.9560 | 0.0954 | 855.2380 | 0.9794 | 0.0247
 | 3717.0172
 | 0.9938
 | 0.0509 | 1115.5558 | 0.9846 | 0.0088
 | 738.3267 | 0.9881
 | 0.0001 | 824.2442 | 0.9894 | 0.0001 |
| i lai a | onnorodi | 6 | 202.7430 | 0.9387 | 0.1738 | 90.2786 | 0.9550 | 0.0743
 | 3532.3055
 | 0.9938
 | 0.0523 | 392.3793 | 0.9735 | 0.0148
 | 626.0736 | 0.9886
 | 0.0001 | 559.3632 | 0.9901 | 0.0001 |
| Soft | l Inivers al | 5 | 120.6366 | 0.9162 | 0.2219 | 73.0066 | 0.9604 | 0.0807
 | 1688.5348
 | 0.9890
 | 0.0754 | 205.8278 | 0.9651 | 0.0202
 | 603.9420 | 0.9878
 | 0.0001 | 598.7140 | 0.9888 | 0.0001 |
| 0011 | Universal | 6 | 44.5778 | 0.8653 | 0.3575 | 9.3598 | 0.8027 | 0.2016
 | 1030.6722
 | 0.9792
 | 0.0961 | 63.4949 | 0.9326 | 0.0356
 | 286.4301 | 0.9846
 | 0.0001 | 350.4759 | 0.9873 | 0.0002 |
| Garotte | Universal | 5 | 244.8698 | 0.9413 | 0.1573 | 295.7592 | 0.9751 | 0.0417
 | 2429.3543
 | 0.9918
 | 0.0629 | 510.7738 | 0.9781 | 0.0129
 | 675.2571 | 0.9880
 | 0.0001 | 657.4185 | 0.9890 | 0.0001 |
| Garotte | Universal | 6 | 83.8600 | 0.9032 | 0.2653 | 25.7977 | 0.8954 | 0.1312
 | 1683.1395
 | 0.9882
 | 0.0753 | 140.6621 | 0.9539 | 0.0243
 | 524.9386 | 0.9870
 | 0.0001 | 510.9414 | 0.9893 | 0.0002 |
| Hard | Heur SLIRE | 5 | 92.8947 | 0.9138 | 0.2530 | 10.0963 | 0.8341 | 0.2045
 | 842.9094
 | 0.9797
 | 0.1067 | 23.0640 | 0.8715 | 0.0591
 | 157.9007 | 0.9852
 | 0.0002 | 132.8477 | 0.9859 | 0.0003 |
| nara | HOUL OUTLE | 6 | 90.8215 | 0.9141 | 0.2556 | 9.0910 | 0.7880 | 0.2109
 | 805.9618
 | 0.9789
 | 0.1093 | 8.9713 | 0.7992 | 8060.0
 | 9.3527 | 0.9440
 | 0.0007 | 6.5721 | 0.9399 | 0.0012 |
| Hard | ΜΙΝΙΜΔΧ | 5 | 1958.3518 | 0.9633 | 0.0559 | 1637.5570 | 0.9821 | 0.0179
 | 4087.3566
 | 0.9907
 | 0.0488 | 1910.6945 | 0.9893 | 0.0067
 | 1140.6878 | 0.9890
 | 0.0001 | 1326.1252 | 0.9900 | 0.0001 |
| nara | | 6 | 579.8509 | 0.9584 | 0.1064 | 267.6269 | 0.9690 | 0.0437
 | 5259.8157
 | 0.9952
 | 0.0431 | 898.8342 | 0.9844 | 0.0098
 | 812.4889 | 0.9895
 | 0.0001 | 926.6422 | 0.9911 | 0.0001 |
| Firm | ΜΙΝΙΜΔΧ | 5 | 742.1036 | 0.9565 | 0.0913 | 873.3774 | 0.9793 | 0.0245
 | 3698.0715
 | 0.9937
 | 0.0510 | 1117.2395 | 0.9852 | 8800.0
 | 684.8821 | 0.9883
 | 0.0001 | 905.9233 | 0.9896 | 0.0001 |
| | | 6 | 189.8985 | 0.9388 | 0.1787 | 84.0091 | 0.9523 | 0.0767
 | 3268.4399
 | 0.9937
 | 0.0542 | 356.5246 | 0.9725 | 0.0154
 | 645.8709 | 0.9887
 | 0.0001 | 613.7425 | 0.9903 | 0.0001 |
| | Hard
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Garotte Universal 6
Hard Heur. SURE 6
Hard MINIMAX 5
6
Firm MINIMAX 5
6 | Hard Universal 6 697.7270 Alard Universal 6 202.7430 Soft Universal 5 120.6366 Garotte Universal 6 44.5778 Garotte Universal 6 33.8600 Hard Heur. SURE 90.8215 90.8215 Hard MINIMAX 5 1958.3518 6 579.8509 574.21036 6 Firm MINIMAX 6 189.9985 | Hard Universal 6 697.727 0.9560 Soft Universal 5 120.6366 0.9162 Garotte Universal 5 120.6366 0.9162 Garotte Universal 5 244.8698 0.9413 Garotte Universal 6 90.8215 0.9134 Hard Heur. SURE 5 92.8947 0.9138 Hard MINIMAX 5 1958.3518 0.9633 Firm MINIMAX 5 1958.3518 0.9565 6 149.8965 0.9388 579.8509 0.9585 | Hard Universal 5 697.727 0.9560 0.0954 Soft Universal 5 120.6366 0.9162 0.2219 Garotte Universal 5 120.6366 0.9162 0.2219 Garotte Universal 6 44.5778 0.8653 0.3575 Garotte Universal 6 83.8600 0.9032 0.2633 Hard Heur.SURE 5 92.8947 0.9138 0.2530 Hard MINIMAX 5 1958.3518 0.9633 0.559 Firm MINIMAX 5 1958.3518 0.9638 0.1737 | Hard Universal 5 697.7270 0.9560 0.0954 855.2380 Soft Universal 5 120.6366 0.9162 0.2219 73.0066 Garotte Universal 5 120.6366 0.9162 0.2219 73.0066 Garotte Universal 5 120.6366 0.9162 0.2219 73.0066 Garotte Universal 5 244.8698 0.9413 0.1573 925.7592 Garotte Universal 6 83.6600 0.9032 22653 25.7977 Hard Heur. SURE 5 92.8947 0.9138 0.2550 10.0963 Hard MINIMAX 5 1958.3518 0.9633 0.0559 1637.5570 Firm MINIMAX 5 742.1036 0.9555 0.0913 873.3774 6 189.8985 0.9388 0.1787 84.0911 10.7874 84.0911 | Hard Universal 5 697.7270 0.9560 0.0954 855.2380 0.9794 Soft Universal 6 697.7270 0.9560 0.0954 855.2380 0.9794 Soft Universal 5 120.6366 0.9162 0.2219 73.0066 0.9604 Garotte Universal 5 120.6366 0.9162 0.2219 73.0066 0.9604 Garotte Universal 5 244.8698 0.9413 0.1573 295.7592 0.9751 Hard Heur.SURE 5 92.8947 0.9138 0.2530 10.0963 0.8821 Hard MINIMAX 5 1958.3518 0.9633 0.0559 1637.5570 0.9821 6 579.8509 0.9544 0.1064 267.6269 0.9949 Firm MINIMAX 5 742.1036 0.9555 0.0913 873.3774 0.9523 Firm MINIMAX 6 189.8985 0.9388 0.1787 84.0091 0.9523 </td <td>Hard Universal 6 697.7270 0.9560 0.0954 855.2360 0.9794 0.0247 Soft Universal 5 120.6366 0.9162 0.2219 73.0066 0.9604 0.0807 0.0807 Garotte Universal 5 120.6366 0.9162 0.2219 73.0066 0.9604 0.0807 Garotte Universal 5 120.6366 0.9112 0.2219 73.0066 0.9604 0.0807 Garotte Universal 5 244.8698 0.9413 0.1573 295.7592 0.9717 0.4917 Hard Heur.SURE 5 92.8947 0.9138 0.2530 10.0963 0.8341 0.2045 Hard Heur.SURE 5 1958.3518 0.9633 0.0559 1637.5570 0.9821 0.0179 Hard MINIMAX 5 1958.3518 0.9633 0.0559 1637.5570 0.9821 0.0179 Firm MINIMAX 5 1742.1036 0.9565</td> <td>Hard Universal 5 697.7270 0.9560 0.0964 855.2380 0.9794 0.0247 3117.0172 Soft Universal 5 697.7270 0.9387 0.1738 90.2786 0.9550 0.0743 3532.3055 Soft Universal 5 120.6366 0.9162 0.219 73.0066 0.9604 0.0807 1688.5348 Garotte Universal 5 120.6366 0.9162 0.219 73.0066 0.9604 0.0807 1688.5348 Garotte Universal 5 244.8698 0.9413 0.1573 295.7592 0.9751 0.0417 2429.3543 6 83.8600 0.9020 0.2653 25.7977 0.8954 0.1312 1683.3548 Hard Heur.SURE 5 92.8947 0.9138 0.2530 10.0963 0.8341 0.2047 842.9044 90.8215 0.9141 0.2565 9.0910 0.7880 0.2109 805.9618 Hard MINIMAX 5<td>Hard Universal 5 697.7270 0.9560 0.0974 0.09794 0.09734 0.0914 0.9978 0.0917 0.0917 0.0917 0.0917 0.09174 0.09134 0.9134</td><td>Hard Universal 5 92.994 0.935 0.2053 0.974 0.0247 3717.0172 0.9938 0.0523 Soft Universal 5 120.6366 0.9162 0.2219 73.0066 0.9743 0.3523.055 0.9938 0.0523 Soft Universal 5 120.6366 0.9162 0.2219 73.0066 0.9604 0.807 1688.5348 0.9890 0.0754 Garotte Universal 5 120.6366 0.9162 0.2219 73.0066 0.9604 0.807 1688.5348 0.9890 0.0754 Garotte Universal 5 244.8698 0.9132 295.7592 0.9751 0.0417 2429.343 0.9918 0.0629 Sa A600 0.9032 0.2633 25.7977 0.8954 0.1312 1683.1395 0.9882 0.0753 Hard Heur.SURE 5 92.8947 0.9138 0.2503 10.0963 0.8341 0.2045 842.9044 0.9799 0.1067 90.</td><td>Hard Universal 6 697.7270 0.9560 0.9954 0.5502 0.9741 0.024 717.0172 0.9938 0.0520 0.1115.5558 Soft Universal 5 120.6366 0.9162 0.2217 73.0066 0.9604 0.8027 0.216 130.6722 0.9793 0.0523 392.3793 Soft Universal 5 120.6366 0.9162 0.2217 73.0066 0.9604 0.8007 1688.5348 0.9890 0.0754 252.8278 Garotte Universal 5
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Table S5. Performance of the SWT at decomposition levels 5 and 6 with the bior2,4 wavelet for 6 thresholding combinations. The tables give the performance of each combination in terms of SNR, SSIM, and RMSE in order of increasing starting SNR (10, 50, 100, 200) of the noisy test signal. Results are presented for the following test signals: blocks, bumps, heavisine, doppler, 1st EPR test signal, and 2nd EPR test signal. Method refers to the thresholding form, while selection refers to the means of calculating the threshold value.

												Sig	gnal								
	BIOR26	SNR=10		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	46.6752	0.7593	0.3572	48.6925	0.7729	0.1007	258.7202	0.9544	0.1928	99.3534	0.9151	0.0292	211.0833	0.9193	0.0002	217.4147	0.9162	0.0002
	mara	onnoroar	6	26.2913	0.7577	0.4672	16.8658	0.7540	0.1640	307.1511	0.9559	0.1769	83.7679	0.9149	0.0315	209.9651	0.9432	0.0002	259.5044	0.9460	0.0002
	Soft	Universal	5	27.5220	0.7216	0.4576	8.3901	0.6580	0.2184	254.9443	0.9533	0.1941	42.3314	0.8808	0.0441	180.0375	0.9185	0.0002	181.1171	0.9145	0.0003
	oon	onnoroar	6	13.4892	0.7070	0.6310	3.0698	0.5648	0.3237	265.4175	0.9513	0.1898	24.6078	0.8629	0.0562	74.3442	0.9349	0.0003	88.4703	0.9343	0.0004
	Garotte	Universal	5	30.5539	0.7297	0.4357	16.8613	0.7198	0.1620	255.3111	0.9534	0.1940	59.1884	0.8962	0.0376	199.6378	0.9187	0.0002	208.1547	0.9153	0.0002
SWT	ourous	onnoroar	6	16.5163	0.7233	0.5752	5.4199	0.6403	0.2597	271.4189	0.9517	0.1877	39.6821	0.8870	0.0449	144.7322	0.9399	0.0002	180.3623	0.9410	0.0003
0	Hard	Heur SURE	5	73.8510	0.7836	0.2840	9.9973	0.6591	0.2069	265.6862	0.9489	0.1906	21.6536	0.8442	0.0611	118.9662	0.9184	0.0002	101.6289	0.9129	0.0003
	mara	noun cont	6	77.8029	0.8150	0.2762	9.1126	0.6968	0.2122	364.7661	0.9559	0.1629	8.8749	0.7820	0.0916	9.4013	0.8948	0.0007	6.6813	0.8799	0.0012
	Hard	ΜΙΝΙΜΔΧ	5	89.0713	0.7881	0.2614	92.0422	0.7949	0.0745	217.2932	0.9164	0.2144	143.7177	0.9173	0.0244	178.7654	0.9077	0.0002	190.4567	0.9070	0.0003
	mara		6	54.9703	0.7985	0.3288	50.6026	0.8115	0.0988	307.8142	0.9300	0.1819	142.0037	0.9306	0.0244	233.9031	0.9427	0.0002	269.7234	0.9447	0.0002
	Firm	ΜΙΝΙΜΔΧ	5	45.8852	0.7570	0.3591	42.8962	0.7701	0.1066	264.6277	0.9538	0.1906	97.4025	0.9140	0.0295	204.4299	0.9189	0.0002	211.8493	0.9161	0.0002
			6	27.4100	0.7613	0.4570	14.8464	0.7498	0.1717	315.2443	0.9551	0.1745	77.6126	0.9127	0.0326	204.1519	0.9437	0.0002	253.4129	0.9456	0.0002
				•								Sig	gnal								
	BIOR26	SNR=50		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	155.8103	0.8788	0.1976	231.1077	0.9214	0.0473	991.3281	0.9789	0.0985	434.5537	0.9677	0.0141	497.9014	0.9748	0.0001	436.8189	0.9751	0.0002
	mara	onversar	6	62.1347	0.8699	0.3129	42.1042	0.8787	0.1073	1124.6757	0.9806	0.0932	222.3264	0.9560	0.0197	466.8725	0.9788	0.0001	449.3501	0.9826	0.0002
	Soft	Universal	5	51.9546	0.8271	0.3359	27.8006	0.8708	0.1269	687.0793	0.9730	0.1182	102.9697	0.9379	0.0285	439.7567	0.9746	0.0001	424.6085	0.9750	0.0002
	oon	onversar	6	21.6797	0.7899	0.5076	5.1562	0.6866	0.2606	554.6952	0.9679	0.1316	51.0346	0.9171	0.0397	166.0232	0.9725	0.0002	218.3386	0.9771	0.0002
	Garotte	Universal	5	76.0754	0.8503	0.2797	83.1164	0.9091	0.0770	764.2064	0.9754	0.1123	194.9379	0.9531	0.0209	495.4483	0.9749	0.0001	443.2941	0.9752	0.0002
SW/T	Garotac	onversar	6	31.9353	0.8220	0.4259	11.4858	0.7802	0.1889	707.1879	0.9725	0.1173	102.3821	0.9394	0.0285	329.2534	0.9755	0.0001	395.1867	0.9808	0.0002
0111	Hard	Heur SURE	5	95.0584	0.8628	0.2509	10.1181	0.7669	0.2052	676.6237	0.9728	0.1195	22.9581	0.8659	0.0594	162.4887	0.9727	0.0002	137.5213	0.9727	0.0003
	mara	neur. oone	6	94.2569	0.8872	0.2517	9.1273	0.7430	0.2116	764.6798	0.9746	0.1131	8.9733	0.7951	0.0912	9.5589	0.9287	0.0007	6.8000	0.9248	0.0012
	Hard	MINIMAY	5	293.2406	0.8919	0.1447	432.0617	0.9293	0.0348	958.8900	0.9677	0.1010	627.8837	0.9734	0.0117	503.1900	0.9732	0.0001	496.5145	0.9735	0.0002
	mara		6	149.0472	0.9027	0.2035	113.2635	0.9140	0.0671	1460.3418	0.9791	0.0818	539.7529	0.9733	0.0126	516.5735	0.9807	0.0001	467.1842	0.9833	0.0002
	Firm	ΜΙΝΙΜΔΧ	5	148.3976	0.8780	0.2023	220.7731	0.9213	0.0484	972.1746	0.9788	0.0995	401.6730	0.9667	0.0146	389.8671	0.9748	0.0001	306.8108	0.9751	0.0002
			6	61.6784	0.8668	0.3134	35.4075	0.8710	0.1159	1101.7092	0.9798	0.0941	228.4886	0.9577	0.0194	453.8732	0.9787	0.0001	452.8321	0.9827	0.0002
												Sig	nal								
	BIOR26	SNR=100		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE	SNR	SSIM	RMSE
	Hard	Universal	5	302.9551	0.9260	0.1427	418.6107	0.9558	0.0358	2029.8474	0.9891	0.0691	830.4000	0.9807	0.0102	601.7693	0.9834	0.0001	566.9782	0.9839	0.0001
			6	97.7455	0.9033	0.2492	48.5016	0.9023	0.0997	2015.2432	0.9896	0.0692	383.4721	0.9705	0.0150	574.8497	0.9858	0.0001	507.5687	0.9871	0.0002
	Soft	Universal	5	79.4055	0.8816	0.2725	45.3480	0.9262	0.1015	1101.8452	0.9824	0.0931	169.9817	0.9584	0.0222	555.1471	0.9833	0.0001	511.6007	0.9837	0.0002
			6	28.0015	0.8235	0.4476	5.6184	0.7181	0.2505	767.3933	0.9736	0.1120	64.7796	0.9306	0.0353	223.3263	0.9801	0.0002	304.5431	0.9834	0.0002
	Garotte	Universal	5	137.2276	0.9068	0.2092	156.4542	0.9501	0.0572	1394.5120	0.9856	0.0830	393.7634	0.9725	0.0147	599.1075	0.9834	0.0001	536.5783	0.9838	0.0001
SWT			6	45.1499	0.8592	0.3587	12.9659	0.8129	0.1780	1107.1479	0.9815	0.0937	143.7524	0.9519	0.0241	433.9684	0.9829	0.0001	479.1500	0.9860	0.0002
	Hard	Heur. SURE	5	94.8206	0.8963	0.2502	10.0288	0.8063	0.2058	816.5070	0.9769	0.1083	22.9428	0.8699	0.0594	172.7061	0.9811	0.0002	140.9057	0.9812	0.0003
			6	93.0020	0.9029	0.2524	9.0363	0.7646	0.2124	845.7042	0.9786	0.1066	8.9874	0.7974	0.0911	9.5793	0.9350	0.0007	6.8000	0.9298	0.0012
	Hard	MINIMAX	5	814.9282	0.9348	0.0877	842.5343	0.9643	0.0250	2124.9382	0.9843	0.0673	1228.5398	0.9851	0.0084	765.8856	0.9835	0.0001	804.7227	0.9836	0.0001
			6	240.8853	0.9291	0.1593	130.4695	0.9335	0.0626	3167.5023	0.9914	0.0553	798.2082	0.9811	0.0104	607.1773	0.9864	0.0001	628.0676	0.9878	0.0001

												Sig	jnal								
	BIOR26	SNR=200		Blocks			Bumps			Heavisine			Doppler			Epr 1			Epr 2		
	Method	Selection	Level	SNR	SSIM	RMSE															
	Hard	Universal	5	570.4563	0.9515	0.1045	784.3059	0.9756	0.0259	3693.5765	0.9934	0.0510	1205.9519	0.9847	0.0085	740.2639	0.9881	0.0001	829.9270	0.9893	0.0001
	- lara	onnoroan	6	131.2387	0.9210	0.2149	49.3317	0.9107	0.0988	3586.7497	0.9937	0.0519	528.4988	0.9772	0.0128	635.0006	0.9886	0.0001	565.5057	0.9901	0.0001
	Soft	l Inivers al	5	114.8077	0.9129	0.2274	72.1631	0.9545	0.0813	1691.2403	0.9887	0.0753	246.8249	0.9679	0.0185	629.6063	0.9878	0.0001	616.1310	0.9888	0.0001
	001	Universal	6	33.9541	0.8412	0.4081	5.5683	0.7244	0.2513	1044.6376	0.9791	0.0954	77.8314	0.9385	0.0323	322.4789	0.9852	0.0001	387.3388	0.9879	0.0002
	Garotte	l Inivers al	5	226.1353	0.9377	0.1634	289.1478	0.9696	0.0422	2431.6438	0.9916	0.0629	629.4125	0.9796	0.0117	682.1657	0.9879	0.0001	666.5885	0.9890	0.0001
SW/T	Garotte	Universal	6	58.1641	0.8786	0.3172	12.8103	0.8196	0.1788	1713.2062	0.9882	0.0746	183.2220	0.9589	0.0214	563.3187	0.9875	0.0001	526.5293	0.9896	0.0002
0111	Hard	Heur SLIRE	5	95.7539	0.9137	0.2493	10.1883	0.8263	0.2042	862.9306	0.9798	0.1058	23.0485	0.8706	0.0592	174.0262	0.9855	0.0002	147.3062	0.9861	0.0003
	nara	Hear. OUNE	6	93.0933	0.9101	0.2525	9.1477	0.7719	0.2111	831.1565	0.9794	0.1080	9.0027	0.7980	0.0910	9.6154	0.9381	0.0007	6.8042	0.9336	0.0012
	Hard	ΜΙΝΙΜΔΥ	5	1750.1691	0.9608	0.0592	1580.6431	0.9803	0.0182	4014.1880	0.9904	0.0492	2094.5528	0.9900	0.0064	1133.6803	0.9889	0.0001	1326.3942	0.9897	0.0001
	nara		6	326.7668	0.9478	0.1369	134.5106	0.9413	0.0614	5125.7262	0.9946	0.0436	1048.5716	0.9853	0.0091	831.0163	0.9896	0.0001	942.4059	0.9911	0.0001
	Firm	ΜΙΝΙΜΔΥ	5	660.3647	0.9535	0.0966	826.3895	0.9757	0.0252	3656.4594	0.9935	0.0513	1283.8979	0.9859	0.0082	718.8349	0.9882	0.0001	916.1859	0.9895	0.0001
			6	125.5106	0.9207	0.2194	40.6155	0.9053	0.1078	3289.4069	0.9935	0.0540	470.5048	0.9758	0.0135	664.1622	0.9888	0.0001	621.5024	0.9904	0.0001

303.8457 0.9258 0.1423 434.6282 0.9574 0.0348 2030.6721 0.9891 0.0690 817.3358 0.9811 0.0103 428.8261 0.9833 0.0001 547.7358 0.9840 0.0002

92.5220 0.9017 0.2548 40.6069 0.8966 0.1079 1949.3939 0.9894 0.0704 360.6326 0.9704 0.0154 556.0264 0.9854 0.0001 533.4063 0.9873 0.0002

5

6

MINIMAX

Firm

Table S6. Performance of the SWT at decomposition levels 5 and 6 with the bior2,6 wavelet for 6 thresholding combinations. The tables give the performance of each combination in terms of SNR, SSIM, and RMSE in order of increasing starting SNR (10, 50, 100, 200) of the noisy test signal. Results are presented for the following test signals: blocks, bumps, heavisine, doppler, 1st EPR test signal, and 2nd EPR test signal. Method refers to the thresholding form, while selection refers to the means of calculating the threshold value.

Chapter 4: Accessing BtuB hatch-barrel information in the native system through modulation of the *E. coli* Dsb system and DEER spectroscopy.

4.1 Introduction

As with other TonB dependent transporters, the *E. coli* cobalamin transporter BtuB must coordinate with the trans-periplasmic protein TonB to move cobalamin across the outer membrane. The size of the cobalamin substrate means that substantial rearrangement is likely to be required in the hatch domain of BtuB before a sufficiently large translocation channel is formed. Additionally, the loops of BtuB have been observed to be in dynamic conformational equilibria, which can be shifted in the presence and absence of calcium, substrate, or TonB (1). To function productively, these motions must also be coordinated allosterically to TonB binding events on the periplasmic face. Thus, it is critical to identify methods with which conformational changes can be determined both in the extracellular loops and the hatch domain.

Distance measurements using pulsed-EPR are an attractive means of obtaining this information. DEER requires much smaller labels than comparable fluorescence techniques while providing sufficient resolution to identify even small conformational shifts. Additionally, recent work in our lab had involved the translation of EPR techniques into the native environments of outer membrane isolates and intact cells. For this project, the aim was to develop a strategy to observe changes between a relatively static site in the barrel, and a potentially mobile one in the hatch.

To do this, site 188 in the extracellular loops was selected as the initial barrel residue. This site had previously been characterized in isolated outer membranes and appeared to label in intact cells (1, 2). DEER data was also available in both systems from site 188 to site 399 in an opposing loop. In Outer membranes, this pair underwent a disorder-to-order transition with the addition of calcium and displayed a change in width but not position with the subsequent addition of substrate (1). *In vivo*, calcium will always be present, and so this pair appeared to present an attractive target as semi-static reference sites in the barrel.

In the hatch domain, site 90 was selected as the initial site as it had also been shown to label in the same intact cell experiments (2). Further, it occupies the most extracellular position in the hatch domain, is near the substrate, and points upward into the extracellular environment, hopefully increasing its accessibility towards the label. Having selected the sites, the 90-188 pair, which is shown in Figure 1, was developed both in the OM and whole cell systems. More details of how the current protocols presented in this work were obtained are available in the recent thesis of Thushani Nilaweera. Here, a brief summary of the method's development is presented in non-chronological order with a subsequent focus on its application to conformational changes observed in BtuB.



Figure 1. A side view of BtuB showing the sites 188 and 90 (orange sticks) in the extracellular loops and upper hatch, respectively. The cobalamin substrate is shown in dark red. This pair was used to check for movement of the upper hatch region in response to substrate binding.

4.2 Additional Methods Information by Figure

Fig. 2 Growth and isolation of OMs from RK5016 cells overexpressing BtuB 90C-188C proceeded as written in Chapter 2.

Fig. 4 Growth of RK5016 cells overexpressing BtuB 90C or BtuB 188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 1 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively.

Fig. 5 (A, B) Growth of RK5016 cells overexpressing BtuB 90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0 with or without 100 mM DTT. Incubation with DTT proceeded for 10 minutes at 37° C after which Labeling occurred for 1 hr with 3 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively. **(C, D)** Growth of RK5016 cells overexpressing BtuB 90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 or 0.2 mg of MTSL and was followed by 2x 30-minute by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM HEPES, pH 7.0 and 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 or 0.2 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM HEPES, pH 5.5, respectively.

Fig. 6 Growth of RK5016 cells overexpressing BtuB 90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 3 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively.

Fig. 7 Growth of DsbA⁻ cells overexpressing BtuB 90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.05, 0.1, 0.25, or 0.5 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively.

Fig. 8 Growth of DsbA⁻ cells overexpressing BtuB 90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 mg of MTSL and

was followed by 2x 30-minute wash steps at RT with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively. The +cobalamin condition used 100 μ M B₁₂.

Fig. 9 Growth and isolation of OMs from RK5016 cells overexpressing BtuB 90C-188C proceeded as written in Chapter 2. 100 μ M cobalamin was added for the + cobalamin condition.

Fig. 10 (A-D) Growth of DsbA⁻ cells overexpressing WT BtuB to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.2 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively.

(E-H) Growth of DsbA⁻ cells overexpressing BtuB 90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 mg of MTSL and was followed by 2x 30-minute wash steps at RT with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively.

Fig. 11 Growth of DsbA⁻ cells overexpressing BtuB 90C-188C was the same as in Fig. 8. Growth of DsbB⁻ cells overexpressing BtuB 90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively. **Fig. 12** Growth of DsbC⁻ cells overexpressing BtuB 90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 mg of MTSL and was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 mg of MTSL and was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively.

Fig. 13 Growth of DsbA⁻ cells overexpressing BtuB 90C-188C was the same as in Fig. 8. 0, 5, 10, 20, 30, 60, or 100 μ M B₁₂ was added to + substrate samples.

Fig. 14 Growth of DsbA⁻ cells overexpressing BtuB 90C-188C was the same as in Fig. 8. Growth of DsbA⁻ cells overexpressing BtuB L8P-90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 mg of MTSL and was followed by

2x 30-minute wash steps at RT with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively. The +cobalamin condition used 100 μ M B₁₂.

Fig. 16 Growth of DsbA⁻ cells overexpressing BtuB 188C-399C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 0.1 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively.

Fig. 17 Growth of DsbA⁻ cells overexpressing BtuB 188C-399C was the same as in Fig. 16. The +cobalamin condition used 100 μ M B₁₂.

Fig. 19 Growth of DsbA⁻ cells overexpressing BtuB 74C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 30 minutes with 0.1 mg of MTSL and was followed by 2x 15-minute wash steps at RT with 100 mM HEPES, pH 7.0. All buffers now contained 2.5% glucose.

Fig. 20 Growth of DsbA⁻ cells overexpressing BtuB 74C-188C was the same in Fig. 19. The +cobalamin condition used 100 μ M B₁₂.

Fig. 21 Growth of DsbA⁻ cells overexpressing BtuB 90C-188C or L8P-90C-188C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 30 minutes with 0.1 mg of MTSL and was followed by 2x 15-minute wash steps on ice with 100 mM HEPES, pH

7.0. All buffers now contained 2.5% glucose. The +cobalamin condition used 100 μ M B₁₂.

Fig. 23 Growth and isolation of OMs from RK5016 cells overexpressing BtuB 6C-510C proceeded as written in Chapter 2.

Fig. 24 Growth and isolation of OMs from RK5016 cells overexpressing BtuB 6C-510C proceeded as written in Chapter 2. The +cobalamin condition used 32 μ M B₁₂.

Fig. 25 Growth of DsbA⁻ cells overexpressing BtuB 6C-510C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 30 minutes with 0.1 mg of MTSL and was followed by 1x minimum time wash step at RT with 100 mM HEPES, pH 7.0. All buffers now contained 2.5% glucose. The +cobalamin condition used 100 μM B₁₂.

Results:

Development of a method for labeling hatch-barrel double mutants in whole cells:

As indicated above, sites 90 and 188 had been previously shown to label in OM isolates and apparently intact cells. Still, they had not been combined and used in pulsed-EPR experiments. So, initial work involved acquiring DEER data for the pair in OMs and characterization of the single-site mutants in RK5016 cells. The 90-188 pair was successfully isolated in OMs, and the resulting DEER spectra are shown in Figure 2.



Figure 2. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 90-188 pair in RK5016 Outer Membranes. For the time domain and dipolar evolution data, the apo condition is shown in blue, and a +100 μ M cobalamin condition is shown in red. For the distance data, the results of 2-Gaussian fitting with a quadratic background function in the program LongDistances are shown. Two peaks are observed in the distribution, with a longer component at 3.2 nm and a shorter component at 2.4 nm. The histograms give the predicted distances from the apo (PDB ID: 1NQG) and substrate-bound (PDB ID:1NQH) crystal structures using the program MMM. The longer distance aligns with the apo prediction, while the shorter distance aligns with +substrate.

The DEER traces were cut back from their original length to a set time of 2 µs and subtracted using a quadratic background function in the proGram LongDistances. The distances were then extracted using 2-Gaussian fitting to the dipolar evolution functions. Unless otherwise noted, the other traces presented in this chapter were analyzed in the same way. The details of why this method of analysis was selected are explained in the following chapter on crowding effects in the bacterial OM. Looking at the dipolar traces shown in Fig. 2A, it is apparent that both the apo (blue) and +cobalamin (red) traces display oscillations at identical time-positions, differing only in their oscillatory amplitudes. This is borne out in the distance distributions recovered in Fig. 2B, where the positions of the two components are identical, and the increase in amplitude results in

slightly narrower features in the apo distribution.

The positional difference of the two components was 8 Å, larger than the expectation length of the MTSL spin-label used in this experiment, and thus unlikely to arise solely through rotameric rearrangement of the label. To help explain this shift, the predicted DEER distributions are shown for in-silico labels attached at sites 90 and 188 in the apo and substrate bound crystal structures of BtuB (PDB ID: 1NQG and PDB ID 1NQH). These predictions were generated using the software package MMM (3). The apo prediction (blue) shows a split distribution, whose average aligns well with the longer distance component in the DEER distribution. The +substrate prediction (red), meanwhile, displays a shorter peak centered at 2.7 nm, which was still longer than the shorter data peak. Still, the shift direction aligned with the idea that the long-distance component corresponded to the apo structure, and the short-distance component to the +substrate structure. An overlay of these structures from the front and side is shown in Figure 3.



Figure 3. Front (A) and Side (B) views of the apo (PDB ID: 1NQG) and +cobalamin (PDB ID: 1NQH) crystal structures of BtuB. The apo and +substrate structures are shown in blue and raspberry, respectively. The labels used in this section at sites 90 and 188 are shown in stick representation, with 90 in the hatch domain and 188 in the extracellular loops. It is apparent from the structures that the hatch loop containing site 90 is partially helical in the apo structure, drawing it down and increasing the interlabel distance. In the +cobalamin structure, the helix becomes disordered, raising site 90 and decreasing the inter-label distance.

In both the apo (blue) and +cobalamin (raspberry) structures, the position of site 188 in the extracellular loops is invariant. In contrast, the hatch loop containing site 90 displays helical structure at its base in the apo structure. This pulls site 90 towards the hatch, increasing the observed distance for the 90-188 pair. In the +cobalamin structure, the helical element is disordered, and the loop is free to extend upward, reducing the expected interspin distance. Thus, the two components may correspond to a conformational change in a hatch element at the substrate binding site. Observing shifts in these components would then be an excellent start to mapping out the conformational environment of the BtuB hatch domain.

Unfortunately, no such shift was observed here in the OM preparations, and so the project moved into whole cells. There, the initial work involved spin-labeling single mutants of 90 and 188 for BtuB overexpressed in RK5016 cell cultures. Representative spectra obtained for these sites are shown in Figure 4. The dominant component in site 90 is highly immobile, and reflects



Figure 4. Representative spectra of site 90 (A) and 188 (B) in BtuB overexpressed in RK5016 cells. The cultures were grown to early log (OD 0.3) and spin labeled with 1 mg of MTSL. Spectra are not normalized.

its position in the interior hatch domain. Site 188, by contrast, shows a much more mobile lineshape that reflects its elevated position on an extracellular loop. The contrast in splitting between these elements means that both should be discriminable in composite CW spectra of the 90-188 pair. After confirming the viability of single mutants of 90 and 188 in RK 5016 cells, the double mutant was attempted several times without success. No significant labeling was observed in the RK5016 cells for the 90-188 pair despite BtuB appearing on protein gels. Additionally, the ability to produce DEER spectra of 90-188 in isolated OMs indicated that the

protein was produced and stably folded in the cells.

Something appeared to be altering the ability to label the protein in live cells. The simplest explanation was that the redox environment was different between the cells and their isolated membranes. As discussed in the introductory chapter, cysteine chemistry in the periplasm is tightly controlled by members of the Dsb system. Additionally, the periplasm had consistently been observed to reduce MTSL label after entry, indicating a significant reductive potential. These observations provided two explanations for the failure to label 90-188. First, the protein may have gained a disulfide bond between site 90 and site 188, with the formation of this bond occurring at one of three points. During translocation, disulfide bonds are nucleated by the DsbA protein, which would produce a linkage prior to protein folding. Absent disulfide bond formation at this stage, it was possible that the disulfide bond was acquired during insertion by the Bam complex, as consecutive β -hairpins are added around the central hatch domain. Finally, a sufficiently close approach distance would have permitted formation of the disulfide after insertion on the cell surface. This last possibility was unlikely, as both distance components observed in the OM DEER were too far for efficient disulfide bond formation post-insertion.

Still, all three points of formation were expected to lead to the formation of stable disulfidebonded BtuB on the cell surface. To perturb these potential bonds, excess MTSL label was used in combination with the reducing agent DTT. The results are shown in Figure 5 A and B. Excess label produced two distinct spectral components. The major component was highly mobile, and indicative of free MTSL reagent. The second, minor component was highly immobile and may correspond to adsorption of label to the cell surface or interactions with the LPS glycans. Addition of DTT increased the percentage of the immobile component, with the shift likely indicating an increased affinity of off-target DTT-MTSL species for the surface. Neither case produced the expected lineshape for 90-188.



Figure 5. Results of labeling Btub 90-188 in RK5016 cells at OD 0.3 with (A) excess MTSL, (B) excess MTSL and DTT, (C) 0.1 mg MTSL, and (D) 0.2 mg MTSL. The excess condition produces a small population of immobile label that may correspond to adsorption onto the cell surface and a large population of highly mobile free MTSL. Addition of DTT causes a sharp increase in the immobile population, which may now be comprised of adsorbed DTT-MTSL species. Both fail to produce the expected lineshape for 90-188. Low MTSL concentrations produce similarly poor results, failing to produce significant labeling above baseline at both 0.1 and 0.2 mg of MTSL. Spectra are not normalized.

An alternative explanation to the labeling problem stemmed from the rapid reduction observed for MTSL labels entering the periplasm. Perhaps this reductive environment extended to the cell surface, and the BtuB cysteines existed as highly reduced sulfhydryls. In this scheme, addition of excess MTSL, itself a weak reducing agent, would serve to further prevent formation of protein-label disulfide bonds. To test this, much lower concentrations of MTSL were employed, at 0.1 or 0.2 mg of MTSL instead of the typical 1 mg quantity that was sufficient for single-site experiments. The results of these trials are shown in Figure 5. C and D. Again, they failed to display the expected lineshape for the 90-188 pair. In both cases, there was no indication of labeling above the resonator baseline.

Despite the unappealing CW results, DEER experiments were still attempted in the hopes that the desired spectra were hidden beneath the free-spin and adsorption components. Representative apo and B12 traces for 90-188 in RK5016 cells are shown in Figure 6. Both in

the absence and presence of DTT and with and without substrate, these early DEER traces could be cleanly subtracted with a 3-dimensional background function, leaving a trace with 0 depth and no apparent oscillation. The lack of oscillation was consistent with no intramolecular dipolar coupling, and thus with a lack of doublylabeled transporters. The 3D background, meanwhile, indicated that the spins were homogeneously distributed in the cell buffer, and proteins on the 2d cell surface. So, the DEER res



Figure 6. Dipolar Evolutions obtained for BtuB 90-188 in RK5016 cells at OD 0.3 with excess MTSL with (red) and without (blue) cobalamin. The data cleanly subtracts with a 3-dimensional background to leave no apparent oscillations. This indicates a total lack of intramolecular coupling in the sample.

homogeneously distributed in the cell buffer, and thus also did not correspond to singly-labeled proteins on the 2d cell surface. So, the DEER results at this stage confirmed that the protein was not being sufficiently labeled.

It was clear that a different approach was required. The second line of reasoning, with reduced BtuB sulfhydryls, could have been explored further by treating the cells with weak oxidizing agents, but western blots became available that showed that the protein appeared to be quantitatively cross-linked (currently unpublished data). This was also consistent with another observation from the OM isolates. In those preparations, a large excess of MTSL was used in combination with very long labeling times of 2 hours. Unlike other systems in the lab, where labeling could be cut back to as short as 10-15 minutes and small quantities of MTSL could be employed, in the OM preparations any deviation led to poor labeling. In light of the western result, this was now consistent with the MTSL acting as both label and reducing agent, slowly breaking apart protein disulfide bonds before forming its own protein-label linkages.

All attention was now focused on ways to disrupt disulfide formation in the protein. The Dsb system could be modulated through mutants of *dsbA*, *dsbB*, and *dsbC*. If bonds were formed during insertion by the Bam complex, however, little could be done to block their formation and so it was hoped that the disulfide bond was formed during periplasmic translocation. To test this

hypothesis, the *E. coli* K-12 strain RI89 strain was obtained along with corresponding *dsbA*⁻, *B*⁻, and *C*⁻ mutations. These knockouts are referred to by the affected protein for the remainder of the work, as DsbA⁻, DsbB⁻, and DsbC⁻, while the WT control RI89 strain is referred to simply as Dsb. The DsbA⁻ strain was selected for initial experiments, as it interacts directly with the protein during disulfide-bond formation and was considered the most likely to disrupt the process. High levels of MTSL again displayed no evidence of labeling for BtuB 90-188. However, the situation at low concentrations was entirely different, with spectra obtained for DsbA⁻ cells with 0.05 to 0.25 mg of MTSL shown in Figure 7. At low levels of spin-label, there is now a distinct lineshape that



Figure 7. CW spectra obtained for BtuB 90-188 in DsbA cells at OD 0.3 with (A) 0.05, (B) 0.1, (C) 0.25, and (D) 0.5 mg of MTSL. A lineshape consistent with an additive combination of sites 90 and 188 is observed in the 0.05 mg MTSL condition and is enhanced in the 0.1 mg MTSL condition. For the higher quantities of label, the spectra become overwhelmed by background adsorption, and in the 0.5 mg MTSL case is completely hidden.

corresponds to an additive combination of the 90 and 188 lineshapes observed in the singlylabeled RK5016 cultures. This lineshape is present with only 0.05 mg of MTSL but is clearly enhanced with an increase to 0.1 mg of MTSL. Further increases instead contribute to the background, with 0.25 mg of MTSL displaying a dominant background adsorption and significant free MTSL. By 0.5 mg of MTSL, any trace of BtuB 90-188 is hidden. Thus, 0.1 mg of MTSL was settled upon as the optimal spin label quantity.

Now, with the observation of an apparently double-labeled protein in the DsbA⁻ cells, DEER experiments were possible. The DEER results for apo and +cobalamin BtuB 90-188 in DsbA⁻ cells are presented in Figure 8. The peak positions are unchanged from the OM data



Figure 8. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 90-188 pair in DsbA⁻ cells at OD 0.3. For the time domain and dipolar evolution data, the apo condition is shown in blue, and a +100 µM cobalamin condition is shown in red. For the distance data, the results of 2-Gaussian fitting with a quadratic background function in the program LongDistances are shown. Two peaks are observed in the distribution, with a longer component at 3.2 nm and a shorter component at 2.4 nm. Histograms again give the predicted distances from the crystal structures. Compared to the RK5016 OM data, there is now a marked shift from the longer distance component in the apo state to the shorter distance component in the +cobalamin state.

presented in Fig. 2 for the RK5016 cell line, but the peak areas now shift dramatically from the longer component in the apo state to the shorter component in the +cobalamin state. This appeared to be evidence of the desired conformational shift, but it was necessary to determine if it was inherent to the membrane environment of the DsbA⁻ cell line, or unique to the whole cells.

To test this, the OM isolate control was repeated using the BtuB 90-188 pair and the DsbAcell line. The resulting DEER data is shown in Figure 9. As with the RK5016 OM data, the two dipolar traces are nearly identical, with the apo trace again displaying enhanced oscillation amplitude consistent with narrower distance components. In the distance distributions, the data now fit best to 3 Gaussians, with the shorter distance component observed in previous results being split into a peak at 2.3 nm and one at 2.7 nm. There is still minimal shifting between the two conditions in the OM, with only a slight increase in the shortest component in the +cobalamin condition. Thus, most of the observed conformational change for BtuB 90-188 appears to be unique to the whole cells.



Figure 9. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 90-188 pair in RK5016 Outer Membranes. For the time domain and dipolar evolution data, the apo condition is shown in blue, and a +100 μ M cobalamin condition is shown in red. For the distance data, the fit is now improved with a 3rd Gaussian component that splits the shorter distance observed in previous results. Despite this, it is apparent that there is still minimal difference between the apo and +cobalamin conditions.

To further verify this result, and to confirm that the DsbA mutant functioned by disruption of disulfide bond formation in BtuB, the experiments were repeated in Dsb, DsbB⁻, and DsbC⁻ strains. The results of labeling all four Dsb strains at OD 0.3 and with low levels of MTSL are shown in Figure 10. The left side of Fig. 10 shows the results of attempted labeling of WT BtuB with 0.2 mg of MTSL, while the right side shows the results of labeling BtuB 90-188 with 0.1 mg of MTSL. For WT BtuB, no evidence of significant labeling is observed in any Dsb strain (Fig. 10 A-D), even at twice the MTSL quantity employed for labeling of BtuB 90-188 in DsbA⁻ cells. Meanwhile, for BtuB 90-188, there is again no evidence of labeling in the Dsb strain (Fig. 10 E). This matches the result for RK5016. Conversely, both DsbA⁻ and DsbB⁻ display significant labeling with nearly identical lineshape (Fig. 10 F, G), containing an immobile component contributed by site 90 and a more mobile component from site 188. That these two mutations are mutually replaceable is consistent with their functional role in the cell. DsbA is responsible for formation of intra-protein disulfide bonds, but it is dependent on DsbB to recharge it for further rounds of disulfide formation. Without either protein the system is arrested after at most one round of bond formation. In contrast, the DsbC⁻ strain again displays no significant labeling.



Figure 10. CW Spectra obtained for WT BtuB (Left) or BtuB 90-188 (Right) in the presence of *dsb* mutant strains at OD 0.3. For WT BtuB, 0.2 mg of MTSL was used for labeling. The spectra correspond to (A) Dsb, (B) DsbA⁻, (C) DsbB⁻, and (D) DsbC⁻. In all four cases there is no evidence of significant labeling above baseline, implying that there is no significant background labeling in dilute MTSL for this protocol. The only differences are the presence of small free spin components in the DsbA⁻ and particularly DsbB⁻ traces. For BtuB 90-188, 0.1 mg of MTSL was used for labeling. The Spectra correspond to (E) Dsb, (F) DsbA⁻, (G) DsbB⁻, and (D) DsbC⁻. Both Dsb and DsbC⁻ display no significant labeling, while the spectra obtained in DsbA⁻ and DsbB⁻ are nearly identical. This was the expected result, as DsbA and DsbB are directly involved in disulfide bond formation. DsbC is a disulfide isomerase, but as the protein has only a single possible disulfide, knocking out DsbC should play little role in the formation of this bond.

The DsbC protein functions as an isomerase for proteins with multiple disulfides. The BtuB 90-188 used here contains only a single possible disulfide, and so the presence of an isomerase was not expected to have a major effect on formation of the unwanted 90-188 disulfide bond.

Building on the CW results, DEER data were also collected for BtuB 90-188 in the four Dsb strains. A comparison of the results for DsbA⁻ and DsbB⁻ are shown in Figure 11.



Figure 11. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 90-188 pair in DsbA⁻ and DsbB⁻ cells at OD 0.3. For the time domain and dipolar evolution data, the DsbA⁻ data is shown in blue (apo) and red (+cobalamin), while the DsbB- data is shown in light blue (apo) and light orange (+cobalamin). Aside from differences in modulation depth of the dipolar evolution functions, the DsbA⁻ and DsbB⁻ DEER are nearly identical. Both fit well to 2 Gaussians, with similar shifts from the longer distance component in the apo state to the shorter distance component in the +cobalamin state.

The DsbA⁻ traces for BtuB 90-188 shown in Figure 8 are replotted here in blue and red for the apo and +cobalamin conditions, respectively, while the DsbB⁻ traces are shown in light blue and orange. As expected from the CW spectra, the DEER data for the two strains are very similar. Both fit well with 2 Gaussian components, have nearly identical peak locations, and display a shift from the longer component to the shorter component with addition of cobalamin. To finish confirming the trend observed in the CW, DEER results for DsbC⁻ are shown in Figure 12. While the CW results did not appear markedly different from the background labeling, there is a small DEER signal. Still, the modulation depth and thus quantity of interacting spin-pairs is reduced with respect to DsbA⁻ and DsbB⁻ and the distances are poorly resolved, fitting to a single Gaussian component. Thus, DsbC⁻ appears to allow some leak of unbonded BtuB 90-188 into the OM but is not nearly as efficient as DsbA⁻ or DsbB⁻.



Figure 12. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 90-188 pair in DsbC⁻ cells at OD 0.3. For the time domain and dipolar evolution data, the apo condition is shown in blue, and a +100 μ M cobalamin condition is shown in red. The modulation depth for the DsbC⁻ traces is significantly smaller, and the distributions are poorly resolved, fitting only to single Gaussian distributions. There may still be a slight shift between apo and +cobalamin conditions, but the DsbC⁻ strain is clearly inferior to data produced in DsbA⁻ or DsbB⁻.

Taken together, the preceding results clearly demonstrate that while single mutants of 90 and 188 were accessible to MTSL, the double mutant was inaccessible. Labeling was only possible in *dsbA* and *dsbB* null strains, which are directly involved in the formation of protein disulfide bonds during translocation into the periplasm. This was also found in the DEER results, where dipolar correlation was significant when DsbA or DsbB were eliminated, but greatly reduced when only the isomerase DsbC was removed. Further, no DEER could be detected for RK5016 cells having a WT Dsb system. Having thus determined a way to produce efficient double-mutants between hatch and barrel in whole cells, focus shifted to exploiting this method.

4.4 Dose-Dependent Response of the BtuB 90-188 Pair in DsbA⁻ Cells:

The DEER data for the BtuB 90-188 pair, first shown in Figure 8, displayed a strong shift from a distance component at 3.2 nm to a shorter component at 2.4 nm upon addition of the cobalamin substrate. As mentioned in the beginning of this chapter, this site may serve as a reporter for secondary structure changes and potential domain movement in the upper hatch domain. Still, this preliminary result raised a number of questions. Was this shift a local response to substrate binding, or did it reflect larger changes in the hatch domain? Did the shift result from motion of 188, 90, or both? Could the change be tied to TonB binding? Many more were posed, and so several experiments were designed to begin to unravel the nature of this result. First, the shift was reexamined at a range of cobalamin concentrations. Figure 13 A presents the distance distributions obtained for BtuB 90-188 overexpressed in DsbA⁻ cells at cobalamin concentrations of 0, 5, 10, 20, 30, 60, and 100 μ M. The apo condition is shown in blue, and the color transitions to red with increasing concentration of the cobalamin substrate. The data were fit to 2 Gaussians. To determine the positions of the peaks, the data were fit individually, and the average of each component was used as the peak position in subsequent fitting. The widths were allowed to vary although they displayed minimal variance, further indicating that this was a 2-state process. Since the peak widths were not fixed, height is not a direct reporter on the percentage of each component, but it can still be seen from the plot that there is a clear dose-dependent response to cobalamin at the ensemble level. The area occupied by the shorter component was then plotted against the cobalamin concentration in Figure 13 B and C. The first shows a hill fit to the full dataset, with a hill coefficient of 3.29 and R² of 0.992. The second shows a linear fit to the 0-30 uM concentration range, with an R² of 0.983.

Titration-like or globally analyzed plots using DEER data have only recently been introduced, with two literature examples involving the BmrCD ABC transporter and the multidrug transporter LmrP (4, 5). Both are large proteins that exhibit several nm conformational changes, and the studies used lipid nanodiscs or detergent solubilization. The data shown here should represent the first example in a native system. Still, there are a several caveats to producing this type of data with DEER. First, EPR spectroscopy works well in concentration ranges between tens and hundreds of μ M. This is well above the substrate affinity of BtuB and many other proteins, and so a dilute condition is impossible. This limits the interpretation of any binding or dissociation constants obtained through such analysis.



Figure 13. Analysis of DEER data for BtuB 90-188 over a range of cobalamin concentrations. The distance distributions obtained through fitting the data for cobalamin concentrations of 0, 5, 10, 20, 30, 60 and 100 μ M to 2 Gaussian components are shown in (A). The color shifts from blue in the apo state to red with increasing cobalamin concentration. The areas of the shorter component were extracted and plotted against the cobalamin concentration to construct the plots shown in (B) and (C). The hill fit shown in (B) has a hill coefficient of 3.29 ± 1.19 and a coefficient of correlation of 0.992. The linear fit shown in (C) has a coefficient of correlation of 0.983. The meaning of other fit parameters is suspect, as both the protein and substrate are in excess in these experiments.

Additionally, these previously published studies on BmrCD and LmrP relied on a single software package, GLADD, by Eric Hustedt at Vanderbilt (6). In order to produce estimates of error from the set of related fits, the data were globally analyzed with linked peak positions and

widths, allowing for the determination of 95% confidence intervals at each point. Here, the GLADD software could not be employed due to the presence of an anomalous background form likely resulting from protein crowding in the OM, the details of which are described in the next chapter. This background contribution can currently only be removed using a different proGram, LongDistances by Christian Altenbach, but this prevents the determination of error in the individual values. By extension, it cannot be statistically determined if the data is best represented by the sigmoidal fits. At the time of writing, the author was in contact with the creators of both packages, and it may soon be possible to produce error analysis of this dataset.

In the absence of definitive error analysis, the simplest explanation is that the data are described by the piecewise linear fit and represents a sequential loading of BtuB by increasing amounts of cobalamin. This may provide a future method of determining the labeled, accessible concentration of BtuB on the cell surface. Alternatively, if the data are found to be best fit via the hill equation with a high coefficient value, the simplest explanation is that this value reflects the protein organization on the surface. While most TBDTs are thought to act monomerically, many surface proteins are trimeric in Gram-negative bacteria. The FepA TBDT has also been shown to have sigmoidal binding kinetics with a Hill-coefficient of 3, and this was posited to come from a trimeric organization of the FepA protein (7, 8). In support of this, that protein was originally present in a trimeric form in native gels (9). Still, the most likely explanation is that a conformational change occurs in response to substrate, and this experiment follows the percentage of proteins that have undergone said shift.

4.5 Attempted Modulation of the 90-188 Conformational Change

Next, the dependence of this structural transition on the trans-periplasmic energy transduction protein TonB was examined using a transport-defective mutation in the ton-box region, L8P. The C-terminal domain of TonB and the N-terminal ton-box in BtuB form a 4-stranded mixed B-sheet, which is critical to the transport of cobalamin across the OM. This interaction is dependent on hydrogen bonding though the even-numbered residues in the ton-

box, and proline mutations at these sites disrupt sheet formation and interactions between the two proteins (10). A comparison of the results obtained for BtuB 90-188 in DsbA⁻ cells with and without the L8P mutation is shown in Figure 14.



Figure 14. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 90-188 pair in DsbA⁻ cells with and without the L8P mutation. For the time domain and dipolar evolution data, the 90-188 data is shown in blue (apo) and red (+cobalamin), while the L8P-90-188 data is shown in light blue (apo) and light orange (+cobalamin). The traces are nearly identical, and the presence of the substrate defective mutation L8P does not appear to alter the peak positions or the extent of the conformational shift.

The darker blue and red colors show the original 90-188 data while the lighter colors give the results for L8P-90-188. It is immediately clear from the +cobalamin dipolar traces that the 90-188 and L8P-90-188 traces overlay almost exactly. This is also seen in the distance distributions, where L8P alters neither the position of the components nor the magnitude of the shift between them. This result could indicate that the conformational change is dependent only on the substrate binding event. Alternatively, it could reflect a decoupling of TonB binding from the response. TonB interactions are known to provide the energy for transport, but if energization by TonB precedes substrate binding, then a change might not be detected. Finally, recent work with AFM to probe interactions between the TonB C-terminus and the ton-box determined that the primary effect of L8P was to decrease the number of productive association events (11). Still, a substantial percentage of events were productive, and at the ensemble level seen in the DEER experiment they may still be sufficient to create the observed shift (11).

Next, the identity of which element of the 90-188 pair was moving during the shift was examined using two additional pairs, 188-399 and 74-188. The first pair had been previously

characterized in OM and an earlier attempt at EPR in intact cells, and was repeated here using the new protocol (2). This pair is shown in Figure 15. Site 399 is positioned at the base of the



Figure 15. A side view of BtuB showing the sites 188 and 399 (orange sticks) in the extracellular loops. The cobalamin substrate is shown in dark red. This pair was used to check for motion of the 188 site in response to substrate binding

extracellular loop above site 90 and was previously found to change width but not shift in position in response to substrate binding (1). The CW spectrum of 188-399 in DsbA- cells is shown in Figure 16. Again, it displays an immobile component coming from the interior facing 399 site and a more mobile component from site 188. The DEER data obtained for this site in the apo and +cobalamin conditions, meanwhile, is presented in Figure 17. This time, the data were better fit using a quadratic background function and model-free distance determination in LongDistances, resulting in more apparent distance components.

In both the apo and +cobalamin conditions, the major distance is at 3 nm with a shoulder at 2.5 nm. This element does not shift in response to substrate addition. Both cases do show a


unique secondary peak, however, with a poorly resolved short peak in the apo case and a small peak at 4 nm in the +cobalamin condition. Thus, while the majority of the population does not shift in response to substrate binding, a subpopulation does move, either from <2 nm to 4 nm, or in and out of the major population at 3 nm. The goal of this data was to determine if 188 was static in

Figure 16. CW spectrum of the 188-399 pair in DsbA $^{\circ}$ cells at OD 0.3 $^{\circ}$

response to substrate binding, and so an additional pair was needed.



Figure 17. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 188-399 pair in DsbA⁻ cells at OD 0.3. For the time domain and dipolar evolution data, the apo condition is shown in blue, and a +100 μ M cobalamin condition is shown in red. The major distant component at 3nm with a 2.5 nm shoulder does not shift significantly, but the apo condition displays a unique very short distance, which is poorly resolved by the experiment. Likewise, the +cobalamin condition displays a small population of a longer distance at 4 nm. Thus, this trace indicates that a subpopulation of 188-399 moves, and cannot confirm that 188 is static in response to substrate binding. Here, the data were fit using the model-free approach in LongDistances, with a smoothing factor of 10.

The other hatch site that had been previously identified for OM and intact cells was 74, and this was combined with 188 to make a 74-188 pair. The location of this pair is shown in Figure 18. Compared to site 90, 74 is located lower in the hatch domain and has proven more difficult to label due to its reduced accessibility. The CW spectrum of BtuB 74-188 in DsbA⁻ cells is in turn shown in Figure 19, displaying the same general pattern of immobile hatch site and more mobile 188 site. Here, evidence of the struggle to label this site is apparent in the reduced



Figure 18. A side view of BtuB showing the sites 188 and 74 (orange sticks) in the extracellular loops and hatch domain, respectively. The cobalamin substrate is shown in dark red. This pair was used to check for motion of the 188 site or for additional conformational changes in the hatch, depending on the outcome of the DEER experiment.

contribution of the immobile component. After several attempts, DEER data were obtained for BtuB 74-188 in DsbA⁻ cells and are shown below in Figure 20. The apo and +cobalamin traces



Figure 19. CW spectrum of the 74-188 pair in DsbA cells at OD 0.3 $\,$

show the same, sharp oscillation. Both produce a similar distribution to that observed with 90-188, with a main distance at 3.2 nm and a minor distance around 2.5 nm. Unlike 90-188, these distances do not interconvert in response to substrate. Thus, this pair does not display any additional conformational changes of the hatch domain. However, it does indicate that site 188 is

likely to remain _{stationary} in response to substrate addition, and that the conformational shift in 90-188 occurs in the hatch and not in the extracellular loops.



Figure 20. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 74-188 pair in DsbA⁻ cells at OD 0.3. For the time domain and dipolar evolution data, the apo condition is shown in blue, and a +100 μ M cobalamin condition is shown in red. The data are once again fit to 2 Gaussian components in LongDistances. There is no shift in response to cobalamin addition, indicating that sites 74 and 188 are immobile. The amplitudes are also very sharp, with correspondingly narrow peaks. This may reflect rotameric restriction as a result of a more confined environment for site 74, which is deeper in the hatch domain than site 90.

Most of the data described here had been obtained using cell pellets that were collected through centrifugation, and the cell pellet was subsequently loaded directly into capillaries for EPR analysis. There was concern regarding the state of the PMF in these cells, as there was not sufficient buffer for aerobic processes, and the previous wash buffers did not contain glucose for metabolism and subsequent generation of an anaerobic PMF. Thus, the protocol was modified to include 2.5% glucose in all buffers and to keep buffer present with the cells at all steps. This made sample preparation more difficult, as the more dilute cell suspensions had reduced signal in the instruments. Still, data were recollected for both BtuB 90-188 and L8P-90-188 to see if a present or more robust PMF impacted the conformational shift in the 90-188 pair. The DEER data for this protocol variant are shown in Figure 21.

There is no apparent change in the results with the addition of glucose to all buffers. There is still a shift from the longer component to the shorter one with cobalamin, and the L8P mutant fails to change this behavior. This lack of difference implies that the transition is either not associated with energization via TonB interaction, or that the energization precedes conformational shifts that accompany substrate binding.



Figure 21. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 90-188 pair in DsbA⁻ cells at OD 0.3 and with 2.5% glucose. For the time domain and dipolar evolution data, the apo condition is shown in blue, and a +100 µM cobalamin condition is shown in red. The L8P-90-188 pair is shown for the +cobalamin condition in orange. The data are once again fit to 2 Gaussian components in LongDistances. The results are the same as before, with no apparent differences from the addition of glucose.

The easiest way to further characterize the extracellular face of the barrel would be through additional sites, and some progress is reported in the final chapter of this work. Several sites have been identified in both the hatch and barrel domain that label efficiently in DsbA⁻ cells. Combinations of these new residues with sites 188 and 90 that were presented here will hopefully allow for more information to be determined regarding the nature of this conformational change, and if it is indicative of wider shifts in the overall hatch domain.

4.6 Extension of New Method into the Periplasmic Face of BtuB

During the transition towards using glucose in all cell culture buffers, it became apparent that extra metabolite led to a decreased reduction rate of the BtuB spin-labels. This may correlate with a reduced rate of cell death, as several cytoplasmic species are capable of spin-label reduction. Though regardless of the cause it made labeling of the periplasmic side of BtuB in whole cells seem plausible. Work from previous members of the lab had found that no signals could be detected for BtuB sites on the periplasmic surface, and early work leading up to the present method supported this. Still, the periplasm is an extremely attractive target for in-cell studies of BtuB. The periplasmic barrel surface contains only short, static turns instead of the elongated loops present on the extracellular side, which provide excellent reference sites.

Further, the Cafiso group had previously identified extension of a number of residues around the ton-box region of BtuB in response to substrate (12).

To both test if periplasmic labeling was possible and search for ton-box extension within the cellular environment, the 6-510 pair was selected. These sites are shown in orange in Figure 22. Residue 510 is located in one of the periplasmic turns that connect B-strands in the BtuB barrel, while residue 6 is part of the ton-box region of the hatch domain. Unlike proline mutations, cysteine mutations in the ton-box do not abrogate TonB binding.



Figure 22. A side view of BtuB showing the sites 510 and 6 (orange sticks) in the barrel and ton-box region, respectively. This pair can be used to probe for extension of the ton-box into the periplasm.

This pair was previously characterized using both CW and DEER for BtuB reconstituted into POPC vesicles (12). *In vitro*, the apo distance for the 6-510 pair was about 2.5 nm (12). Addition of cobalamin created a second peak at 3.5 nm, consistent with extension of the ton-box away from the barrel (12). To test for this in native systems, the 6-510 pair was first isolated in

RK5016 OM. The CW spectra for this pair in the OM is shown in Figure 23. Ordinarily, there is significant background labeling in the OM isolates, which makes determination of unique spectral



Figure 23. CW spectra for the 6-510 pair in RK5016 Outer Membranes. The contribution from site 6 is best seen in the highfield line, where it contributes a distinct central bump.

features difficult. Fortunately, site 6 has a characteristic bump in the high field line, which makes it easy to identify. The DEER data for this pair in RK5016 OMs is shown in Figure 24. The Dipolar traces show a significant bowl-shape partial oscillation that is particularly evident in the apo trace. This partial oscillation is likely indicative of crowding and correlates with the small peaks at 5-6 nm in the distance distributions. Otherwise,

the apo distribution shows a main peak centered around 2.5 nm, which aligns with the substrate bound predicted distance, but not with the apo structure. Still, the apo predicted distance is less than 2 nm, and firmly in a region that is poorly resolved in DEER experiments. It thus cannot be ruled out that some population samples this distance.



Figure 24. The (A) time domain, (B) dipolar evolution, and (C) Distance distribution for the BtuB 6-510 pair in RK5016 outer membranes analyzed using DeerAnalysis with a variable dimension background. Apo is shown in blue, and +cobalamin is shown in red. The shortest distance aligns in each condition and is similar to the predicted distances for the substrate bound structure (red histogram, PDB ID: 1NQH) but not for the apo structure (blue histogram, PDB ID: 1NQG). Substrate addition creates an intermediate population consistent with ton-box extension. The longest distances around 5-6 nm likely result from crowding.

The +cobalamin distribution has the same main peak at 2.5 nm, but now displays a shoulder around 3.2 nm consistent with ton-box extension. This aligns reasonably well with the *in vitro*

results, where the peaks were centered at 2.5 and 3.5 nm, although more of the population shifted into the longer component *in vitro*.

For the whole cell experiments, the 6-510 pair was grown in DsbA⁻ cells to OD 0.3 in the presence of glucose. Surprisingly, it labeled, although the label disappeared very quickly, and all washing steps had to be cut out of the protocol in order to retain enough signal to obtain DEER data. Still, the resulting traces and distributions are shown in Figure 24 for the 6-510 pair in whole cells. Most of the partial crowding oscillation from the OM samples has disappeared, owing to the sparse distribution of labels that have escaped reduction in the periplasmic space. The distributions also still show the same main peak, which aligns with a folded ton-box observed in the +cobalamin structure and also includes an additional short component that may represent the apo structure. Now, however, there is evidence for several conformations that represent ton-box extension at distances of about 3.2, 3.6, and 4.6 nm. These extended peaks are present in both the apo and +cobalamin conditions, with no real change between the two. It is unclear why substrate dependent extension is not observed in the whole cells. One simple explanation is that only a small fraction of proteins are labeled, and are spared from reduction by their inactivity. Alternatively, it may be that the natural state of the ton-box *in vivo* is extended, to better search for the TonB C-terminus. Clearly, more experiments are needed to understand this phenomenon.



Figure 25. The (A) time domain, (B) dipolar evolution, and (C) Distance distribution for the BtuB 6-510 pair in dsbA⁻ whole cells. Apo is shown in blue, and +cobalamin is shown in red. The major short distance still aligns in each condition and remains similar to the predicted distances for the substrate bound structure, but not for the apo structure. There is now also an extremely short component (<20 A) which is poorly captured but may correspond to the apo structure. The intermediate components that are consistent with ton-box extension are greatly enhanced in whole cells and are present in both apo and +cobalamin conditions.

4.7 Discussion

The results shown here indicate the dependence of disulfide linkages between hatch and barrel cysteine mutant pairs in BtuB upon the bacterial Dsb system. Initial results in a strain having WT Dsb activity (RK5016) showed that it was possible to label single cysteine mutants in the hatch and barrel domains. Subsequent attempts at DEER using the BtuB 90-188 pair in the hatch and barrel, respectively, resulted in the successful acquisition of DEER data in the isolated OM, while the whole cells showed a total absence of DEER (Fig. 2 and 6). The ability to successfully double-label the protein in isolated OMs indicated that the protein was present on the surface and hypothetically possessed a crosslink between sites 90 and 188. This crosslink may have formed at several points during formation and insertion of BtuB (Figure 26).



Figure 26. A model of the disulfide bond formation and OM insertion steps for BtuB. The putative crosslink between sites 90 and 188 in BtuB could have been formed by the proteins of the Dsb system (DsbA, DsbB, DsbC, DsbD in figure), during membrane insertion via the BAM complex, or after insertion on the cell surface. Within the Dsb system, DsbA is involved in the direct formation of template crosslinks and is reoxidized by the IM protein DsbB. DsbC is an isomerase which is recharged by the IM protein DsbD. Figure created by Dr. Thushani Nilaweera using BioRender.

The surface crosslink was probed by addition of excess label and pre-treatment with

DTT, neither of which resulted in the formation of double-labeled protein. This may indicate that

the crosslinked conformation involved a folding over of the 188 loop into a form that was not readily accessible to DTT. Any perturbation of the BAM complex was likely to lead to folding and insertion defects, and thus attention was focused on the Dsb system. Disulfide formation is tightly regulated in Gram-negative bacteria, with initial crosslinks being formed by the protein DsbA during or after translocation of the protein template into the periplasm (13). This occurs through the initial formation of a mixed-protein disulfide between the catalytic Cys-X-X-Cys motif in DsbA and the first template cysteine, with subsequent formation of an additional mixed-disulfide with the second template cysteine and isomerization to give the template disulfide bond (13). The resulting reduced cysteines in DsbA are reoxidized by the IM protein DsbB (13). While this reoxidation of the DsbA catalytic motif is performed by two similar Cys-X-X-Cys motifs in DsbB, the latter protein does not participate directly in template disulfide formation, even when DsbB is decoupled from the IM and the Dsb system is moved to the bacterial cytoplasm (14). That the formation of template disulfides is dependent on both proteins was also observed here, as null mutations in both *dsbA* and *dsbB* resulted in the successful double-labeling of BtuB 90-188 (Fig. 10A and B) and the acquisition of significant DEER data (Fig. 11).

The removal of DsbC through a null mutant of *dsbC*, in contrast, produced no significant increase in labeling relative to a WT BtuB control (Fig. 10C). Further, it produced a much smaller DEER trace having only about 2% modulation depth in the apo condition (Fig. 12). This was consistent with the primary role of DsbC being a disulfide isomerase, as this function is unnecessary for a protein template having only a single putative crosslink. Still, the removal of DsbC did produce evidence of some double-labeled protein existing on the cell surface, and this implied that its removal was altering the extent of periplasmic crosslinking when compared to the WT Dsb and RK5016 strains. Recently, a secondary function has been demonstrated for DsbC and another periplasmic component of the Dsb system, DsbG. *In vivo*, these proteins serve not only as isomerases but also in the protection of free sulfenic acids in proteins

possessing only a single, cysteine residue, such as AraF (15). In the case of AraF, this occurs through the reduction of an inter-protein disulfide, which forms a nonfunctional AraF dimer (15). If DsbC was acting in a protecting role for the BtuB 90-188 template, then its removal would not be expected to contribute to successful double-labeling of the BtuB 90-188 target. Both DsbC and DsbG are reduced by the same IM protein, DsbD, however, and the two proteins have differing substrate specificity (16). Thus, the removal of DsbC may contribute to upregulating the reductive or protective actions of DsbG, although this would require significant future work to fully identify.

The direct role of DsbA in the formation of template disulfides made its removal a logical choice for future work requiring modulation of the Dsb system, and so the remaining experiments were conducted with the dsbA null mutant strain. For the 90-188 pair on the extracellular surface, the short-distance component was generally consistent with that seen in the OM data and also with the crystal structure predicted distances, although in the whole cells it readily split into two components with a substrate dependent inversion (Fig. 11). This inversion may represent an order-to-disorder transition in the hatch loop containing site 90, which can be seen in the apo and substrate bound crystal structures (PDB IDs: 1NQG and 1NQH). The change was also dose-dependent (Fig. 13) with a clear proportional response in addition to increasing quantities of substrate. That the substrate-dependent inversion in the short distances was not affected by the addition of the L8P mutation, which blocks TonB interactions, indicated that the change may not be energy-dependent (Fig. 14). Although, this observation would also be consistent with energization by TonB preceding substrate binding events. DEER spectra in cells lacking DsbA were also obtained for the 74-188 and 188-399 pairs, which showed minimal substrate-dependent shifts and indicated that the 188 loop was a suitable control for looking at movement in the hatch domain (Fig. 17 and 20).

Alteration of the Dsb system also made it possible to double-label sites on the periplasmic face of BtuB, including the 6-510 pair. In Isolated OMs, the DEER spectra for this pair showed the presence of a major short-distance element between 2 and 3 nm which was consistent with a folded ton-box region (Fig. 24). The addition of substrate, however, resulted in the formation of a second, shoulder peak past 3 nm which would be indicative of substrate-dependent extension of the ton-box. This substrate-dependence on the state of the ton-box was also observed in previous *in vitro* work from the Cafiso Lab (12). Through a combination of reducing the time spent in the labeling and processing of the cells, and the probable alterations to the periplasmic redox state due to the removal of DsbA, it was also possible to collect the same DEER data in whole cells (Fig. 25). Curiously, the whole cell data displayed peaks consistent with both a folded and unfolded ton-box in the apo state, with no change upon substrate addition. Thus, it appears that some percentage of BtuB possess constitutively unfolded ton-box elements in the cellular environment, which aligns to *in vitro* data collected for the ferrichrome transporter FhuA, and may have strong future implications on the nature of the interaction between BtuB and TonB (17).

4.8 References

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Chapter 5: Crowding and Organization of overexpressed BtuB on the *E. coli* cell surface 5.1 Introduction

The surface of Gram-negative bacteria is comprised of an OM whose makeup differs drastically from the phospholipid bilayer below. It is filled with transporters and trimeric porins, which form the majority of its surface. In between them sit LPS molecules, whose strong adjacent interactions reduce both diffusion across the membrane and lateral movement along it. Together, they form a constrained envelope around the cell, where diffusion is typically local and movement is driven stochastically by synthesis and insertion of new elements.

It is into these crowded environments that BtuB mutants are inserted in the whole cell experiments presented in this work. In WT cells, BtuB has a copy number of only several hundred, with haploid cells producing about 200 per cell (1). Yet, when overexpressed with the pAG1 plasmid, the level of BtuB may reach 40% of the native porins (1). There can be many tens of thousands of OmpF and OmpC porins on the cell surface, and the addition of a great number of BtuB transporters can be expected to further constrain this tightly packed surface. Additionally, recent work has highlighted the sparse nature of insertion events, with fluorescently tagged TBDTs being observed to appear together in organized patches, or islands, on the OM (2). These patches reached half a micron in size, containing hundreds of proteins (2). Additionally, the proteins comigrated across the cell surface, in agreement with previous measurements of confined diffusion in most OM proteins (3).

Coarse-grained simulation studies designed to mimic BtuB in these islands found that the proteins interacted through two weak interfaces formed from hydrophobic and aromatic residues on the barrel surface (2). An extension of these studies to the mesoscale found the formation of extensive, string-like aggregates of protein driven by these weak interfaces (4). Branching aggregates have also been observed in coarse-grained studies of visual rhodopsin, and even in simplified B-barrel mimetics containing only three amino acids: leucine, serine, and tryptophan (5, 6). For these systems, the aggregation was driven by lipid mismatch effects, which have also

been demonstrated in BtuB. Yet, these protein strings have not been detected experimentally on the cell surface. Fluorescence techniques lack the resolution, and while AFM has been used to probe the supramolecular organization and interactions of the major porins due to their trimeric oligomers, it would be difficult to characterize a mixed-population of smaller, monomeric TBDTs interacting only through weak protein-protein interactions. This presents another niche for EPR spectroscopy, where the DEER experiment can fill in distance information at the molecular level, covering the 20-80 Angstrom range, and does so only for the mutant protein of interest, without interference from other surface species.

Viewed from the top, a single BtuB molecule is an ellipsoid with major and minor axes of 4.2 and 3.7 nm, respectively (7). A pair-wise interaction between BtuB molecules would then produce a distance between about 4 and 8 nm depending on the orientation and radial-offset of the labeled site. For non-random cases, such interactions should appear as discrete peaks in the distribution, while for random interactions created only by the crowded environment, they may only affect the intermolecular background term. Background functions in DEER are typically modeled as simple, decaying exponential functions but this holds only for homogeneously distributed systems. Deviations due to excluded volume, radial offset, and crowded environments all significantly alter the decay of the time-domain data (8). Thus, it should be theoretically possible to discern the mode of interaction for BtuB overexpressed into a highly crowded native environment.

The *in vitro* experiments used by the Cafiso lab to study BtuB for many years have not produced evidence of crowding or protein-protein interactions. Yet, these experiments used BtuB reconstituted into excess POPC vesicles, producing low density incorporation without the LPS or other proteins that define the native surface. During the transition from reconstituted systems towards OM isolates, however, long-distance features began to consistently appear across seemingly unrelated traces. An example is shown in Figure 1, taken from a distance measurement between two extracellular loop sites, 449 and 553, in OM isolate (9). The short

distance components align well with the predicted crystal structure distance (histoGram), but in both the apo and +B12 conditions there are unlinked peaks between 5 and 6 nm. This is particularly apparent in the +B12 trace, where the longer distance component dominates the data, manifesting as a bowl-shaped partial oscillation between 0.5 and 3.5 µs. These peaks were observed in many, if not most, of the data collected in OM isolates, with a distance between 5 and 6 nm. The peak's position changed more with runtime than identity of the sample, suggesting that it might be inherent to BtuB rather than a product of any given label-pair. Yet 5-6 nm is only slightly greater than both the width and height of the protein, and so for most distributions it could be reasonably argued that this long-distance component was an intramolecular feature. Still, when these distance components began to appear again and again in the data used for this thesis, it became apparent that the identity of this peak needed to be investigated.



Figure 1. The long-distance component observed in prior OM isolate data. The figure is taken from (9) for DEER data obtained between sites 449 and 530 in BtuB overexpressed in OM isolates. The peak between 5 and 6 nm is disjoint from the rest of the distribution and is the dominant distance element in the +b12 trace.

5.2 Additional Methods Information by Figure

The modifications to the protocols in Chapter 2 are given below as a function of the experiments reported in each figure.

Fig. 3 Growth and isolation of OMs from RK5016 cells overexpressing BtuB 90C-188C proceeded as written in Chapter 2. 100 µM cobalamin was added for the + cobalamin condition.

Fig. 4 9/20/17 Growth of RK5016 cells overexpressing BtuB 188C to OD 0.6 was followed by resuspension in 50 mM HEPES, pH 8.0. Labeling proceeded for 1 hr with 1 mg of MTSL and was followed by 1x surface wash ice with 50 mM HEPES, pH 8.0. 32 μ M spin-labeled substrate was added for the +substrate condition.

Fig. 6 6/30/17 and 4/21/18 Growth of RK5016 cells overexpressing BtuB 188C to 6.5 hrs post inoculation was followed by resuspension in 50 mM HEPES, pH 8.0. Labeling proceeded for 1 hr with 1 mg of MTSL and was followed by 1x surface wash with 50 mM HEPES, pH 8.0. Growth of RK5016 cells overexpressing BtuB 90C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 1 hr with 1 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively.

Fig. 7 5/24/18 and 5/25/18 Growth and isolation of OMs from RK5016 cells overexpressing BtuB188C proceeded as written in Chapter 2. 1 mg of MTSL was used for the full labeling condition, and 0.5 mg MTSL was combined with 0.5 mg of 1-acetyl-2,2,5,5-tetramethyl- Δ 3-(pyrroline-15N)-3-methyl methanethiosulfonate for the dilution condition.

Fig. 8 6/30/18 and 7/1-4/18 and 7/25/18 and 7/29/18 Growth of RK5016 cells overexpressing BtuB 188C to 6.5, 8, 9.5, 11, 12.5, 14, or 28 hrs post inoculation was followed by resuspension in 50 mM HEPES, pH 8.0. Labeling proceeded for 1 hr with 1 mg of MTSL and was followed by 1x surface wash with 50 mM HEPES, pH 8.0.

Fig. 9 Summarizes results obtained for RK5016 cells at various OD values overexpressing BtuB 188C in the presence and absence of the spin-labeled substrate. The samples were resuspended in 50 or 100 mM HEPES buffer at pH 7.0 or 8.0 with 0-2 30-minute wash steps. All samples were

incubated on ice and 20-60 uM of spin-labeled substrate was added for samples having 2 peaks in the distribution.

Fig. 10, 12, 13, 14 Growth of RK5016 cells overexpressing BtuB 188C OD 0.5 in deuterated media with 0.2% deuterated glycerol as carbon source was followed by resuspension in 100 mM HEPES, pH 8.0. Labeling proceeded for 1 hr with 1 mg of MTSL and was followed by 2x 30-minute wash steps on ice with 100 mM HEPES, pH 7.0 and 100 mM MES, pH 5.5, respectively. All buffers were made in D2O.

Fig. 15 Growth and isolation of OMs from RK5016 cells overexpressing BtuB 90C-188C proceeded as written in Chapter 2.

Fig. 16 (A) Growth and isolation of OMs from RK5016 cells overexpressing BtuB 6C-510C proceeded as written in Chapter 2. 32 μ M spin-labeled substrate was added for the +substrate condition. **(B and C)** Growth of DsbA⁻ cells overexpressing BtuB 6C-510C to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 30 minutes with 0.1 mg of MTSL and was followed by 1x minimum time wash step at RT with 100 mM HEPES, pH 7.0. All buffers now contained 2.5% glucose. 100 μ M cobalamin was added for the + cobalamin condition.

Results and Discussion

5.3 Characterizing Recurrent Long-Distance Components in Native Systems

Before experimental data showing similar long-distance components to that in Figure 1 are presented, Figure 2 gives simulated examples of DEER data showing a single distance at 3 nm or at the 5.5 nm position indicated in Figure 1. These simulated examples have no background from intermolecular interactions, to show what the target trace would look like after an ideal background model is removed from the experimental signal. In the short distance case, a complete oscillation is obtained before 1 µs, and the trace has decayed almost completely by 2 µs. Most of the DEER measurements taken in native systems have runtimes between 3 and 3.5 µs, and so if only short distances are present it would be relatively simple to account for this component. The simulated 5.5 nm trace, meanwhile, completes a full oscillation at more than 4 µs. For traces between 3 and 3.5 µs only a partial oscillation will be present, and this will make background subtraction difficult, since the asymptotic behavior of the signal will not be visible.



Figure 2. Simulated time domain data for DEER traces with distances at 3 nm (A) and 5.5 nm (B) and widths of 4 and 8 Å, respectively. The data were generated using LongDistances with modulation depth of 0.5 and no intermolecular background. In the absence of intermolecular interactions, the DEER traces decay asymptotically towards 0. For the short distance example, which emulates the 90-188 pair discussed in the previous chapter, most of the oscillation is present before 1 μ s. For the longer distance, which mimics the long-distance component in the OM isolate data, a full oscillation is not observed until 4 μ s. Much of the data in native systems could only be run to 3 or 3.5 μ s, and so the longer distance component will appear as a bowl-like shape, making background subtraction difficult.

As a data example, the DEER data for the 90-188 pair in RK5016 OM isolates from Chapter 4 is shown again in Figure 3. Here, the analysis was performed using Tikhonov regularization in DeerAnalysis. The trace was subtracted with a stretched exponential function of dimension 2.4. The initial portion of the dipolar oscillation shown in Fig. 3A is raised above the latter part of the trace, which stems from convoluting the higher frequency short-distance oscillation with the broader decay from the long-distance component. The fit to the data is shown in red, and while sufficient for the early portion of the trace, becomes increasingly poor through the partial oscillation at the end. This is evident in the residuals plot shown in the inset, where an oscillation is still present in the residuals.



Figure 3. The (A) dipolar evolution, and (B) Distance distribution for the BtuB 90-188 pair in RK5016 OM isolates analyzed using Tikhonov regularization in DeerAnalysis2015. The background dimension was 2.4 and the value of the regularization parameter was 100. The dipolar trace is dominated not by the expected 90-188 distance, but by a partial long-distance oscillation from 0.5 $- 3.0 \mu$ s that appears as the peak at 5.2 nm in the distance distribution.

The distance distribution in Figure 3. B contains two peaks. The first is the expected distance at 3 nm, which is not split into two components at 2.4 and 3.2 nm due to the relatively high value (100) of the regularization parameter. The second is at 5.2 nm, and its low width is largely responsible for the poor fit at the end of the trace. Tikhonov regularization is a global optimization procedure, with one regularization parameter that controls the smoothness and by extension peak widths of all components in the distribution. The width of the longer distance peak

is thus constrained by the relatively narrow short distance peak, creating the spike in the residual plot at the end of the trace. Still, the background model is also nonideal, which is manifested in the smooth oscillation present throughout the fit residuals.

The expected distances for the 90-188 pair from the apo and +cobalamin crystal structures were shown in Chapter 4. In both cases, there is no evidence for a peak at 5-6 nm, and if this peak came from an intramolecular interaction, it would indicate substantial rearrangement of the hatch domain consistent with the hatch being partially removed from the barrel. The alternative explanation is that the peak comes from lateral, intermolecular interactions between spins on neighboring BtuB proteins.

To help clarify, data for a second pair is shown in Figure 4. Here, the data were obtained for BtuB 188 in RK5016 cells and a spin-labeled cobalamin analogue, which was provided by Dr. Benesh Joseph (University of Frankfurt) and has been previously characterized (10, 11). The data were again analyzed with DeerAnalysis, this time with a background dimension of 3.0 and a regularization parameter of 10. The Dipolar trace shown in Fig. 4A shows the same features as were seen for 90-188 in Fig. 3. There is a short-time oscillation that correlates to the peaks between 2 and 3 nm in Fig. 4B and a partial oscillation observed through the rest of the trace, which again appears between 5 and 6 nm in the distance distribution. Here, the experiment could be run for slightly longer, allowing more information to be collected on the longer oscillation. Compared to the peak in Fig. 3 with a center at 5.2 nm, the increased runtime has shifted the current peak to 5.6 nm. This suggests that the real distance is longer still, and simply cannot be resolved by the given runtime. Again, the fit is poor at the end of the trace, with a notable spike in the residuals indicating that the peak is overly narrow. Also, there is still a full oscillation across the residuals plot, indicating that the background subtraction and fit still do not fully describe the data.



Figure 4. The (A) dipolar evolution, and (B) Distance distribution for RK5016 BtuB 188 and a spin-labeled cobalamin substrate analyzed using Tikhonov regularization in DeerAnalysis2015. The background dimension was 3.0 and the value of the regularization parameter was 10. The expected background dimension for proteins on a membrane is 2, and so a value of 3 for the background is abnormal. This could reflect the presence of free spin-labeled substrate, but the concentration of cobalamin (32 uM) was too low for free cobalamin to be the dominant background element. Increases in apparent dimensionality have also been seen for crowded systems and in the presence of excluded volume.

For this trace, an intramolecular distance of 5-6 nm would indicate that the substrate had moved to an additional binding site on the periplasmic surface of BtuB. Such a site would almost certainly be accessible to the periplasm, where the rapid reduction would mean that the long-distance peak should disappear after a short incubation. Yet, these traces were taken after much longer incubation times than had to be employed for the 6-510 data shown in Chapter 4, and the long-distance component was relatively stable. If the distance was instead intermolecular, then it would also help explain the other unexpected element of this dataset, the background dimension.

Usually, a dimensional value of 3 would be expected for soluble proteins or detergent solubilized samples. The second spin in this experiment was donated by the spin-labeled

substrate which would be three-dimensionally distributed, but the ligand concentration was only 32 μ M in this experiment. Recalling the dose-dependent response of the BtuB 90-188 pair in Chapter 4, if the data were analyzed in a piece-wise linear form consistent with a measure of substrate loading then the transition point was between 30 and 60 μ M. If that is taken as the typical concentration range for BtuB in these experiments, then the substrate is not present here in excess. BtuB also has a very high substrate affinity, in the nm range. Taken together, there should not be sufficient free, spin-labeled substrate to boost the apparent background dimension.

Alternatively, elevated background dimensions are the hallmark of excluded volume effects. The quasi-exponential decay observed in the DEER experiment, and which is removed through background subtraction, arises mainly from instantaneous diffusion (8). Due to the limited bandwidth of the pulses that can be applied in the experiment, only a fraction of the total spins can be flipped by the observe or pump pulses, and thus contribute to the experiment. If spin flip-flops occur between these experimentally relevant spins and other spins which are not affected by the experiment, then the signal is effectively lost via instantaneous diffusion. For this loss to be modeled as an idealized stretched exponential, the surrounding spins must be homogeneously distributed and all interspin distances must be available. For small proteins this is possible, but as the protein diameter gets larger the minimum interlabel distance also increases and the corresponding high frequency decay at the beginning of the trace is reduced.

Even for moderate protein sizes with diameters of 4 to 6 nm, this reduction in the signal decay can persist for several µs and long enough to affect the entirety of the traces in Figures 3 and 4 (8). Literature examples of excluded volume effects are limited to soluble proteins and onedimensional polymers, but generally find that the background decay occurs with a higher apparent dimension. For human serum albumin (HSA), affected DEER traces had to be fit with a background dimension of 3.74 (12, 13). HSA has a diameter of about 5 nm, slightly larger than a direct BtuB-BtuB contact. Still, AFM studies on the surface of *R. denitrificans* found that the OM porins were separated either by the protruding residues of their aromatic girdles or by single molecules of LPS. The width of the latter, taken from the bilayer simulation shown in the introduction, was about 1.5 nm. Thus, the total inter-protein contact distance would be about 4-6 nm and the increase of 1.0 in dimensionality for the trace shown in Figure 4 is consistent with that seen for HSA.

One approach to dealing with excluded volume effects is to switch the analysis method to a model-based approach with Gaussian distance components. This has the advantage of allowing the background to be cofit with the distance distribution, assisting with its determination. This approach has been applied using the GLADD and DD software packages from Eric Hustedt (14, 15). These packages also contain a specialized background function meant to model excluded volume effects, although this variant was developed in (14) and (8) for three-dimensional systems, and was not found to benefit the traces shown here. A model-free approach has an additional benefit, which is the ability to have unique widths for each peak. Both presented datasets showed poor fit agreement at the end of the trace, which appeared to arise from the constrained, narrow width of the long-distance component. In a Gaussian approach, these peaks are decoupled from the narrow, short-distance components and a better estimate of the peak width may be possible.

The results of refitting the data shown in Figure 4 for BtuB 188 and the spin-labeled cobalamin using a model-based approach in DD are shown in Figure 5. A single-Gaussian fit is shown in blue, and a two-Gaussian fit is shown in black. With one component, the fit had an apparent background dimension of 2.4 and has noticeably poor agreement with the data, with the residuals (Fig. 5A inset top) still containing a strong oscillation. The two-component fit, meanwhile, shows no oscillation in the residuals (Fig. 5A inset top) still containing a strong oscillation, but fit with an apparent dimensionality of 3.3. Both fits show the same short-distance peak, which is consistent with the crystal structure prediction (pink histoGram). For the two-Gaussian fit, the long-distance peak moves relative to the DeerAnalysis fit, with a new position of 6.5 nm. The width also increases, with a σ of 11.5 Å.



Figure 5. The (A) dipolar evolution, and (B) Distance distribution for RK5016 BtuB 188 and a spin-labeled cobalamin substrate analyzed using model-based fitting with Gaussian peaks in DD. The background dimension was 3.3. The elevated background dimension again may indicate a crowded system with excluded volume effects. The fit with a single Gaussian component is shown in blue, and with two Gaussian components in black. The single-Gaussian fit shows a clear oscillation in the residuals (inset top) which is not apparent in the two-Gaussian fit (inset bottom). The two-Gaussian fit also shows a long-distance peak at a similar position to that observed in the DeerAnalysis fit, but it is now much broader.

The substantial increase in width would suggest that this peak is likely an intermolecular effect, with heterogeneous contacts or aggregation of BtuB monomers. If this is the case, then the effect should be observed for single mutants of the protein as well.

To this end, DEER data for singly labeled BtuB 90 and BtuB 188 in RK5016 cells are shown in Figure 6. Cofitting in DD with a variable dimension background and a single Gaussian component produces similar results for both 188 (teal) and 90 (purple). Both fits have apparent background dimensions of 3.3 or 3.4, and the peak positions are at 6.2 nm \pm 10 Å. It can be seen from the residual inset that both fits have good agreement with the data.



Figure 6. The (A) dipolar evolution, and (B) Distance distribution for BtuB 188 (teal) and BtuB 90 (purple) in RK5016 cells using model-based fitting with Gaussian peaks in DD. The background dimensions were 3.3 and 3.4, respectively. The dipolar evolution is shown at the top in (A) and the distance distribution is shown in the lower panel in (B). Both sites show a similar long-distance peak with position around 6.2 nm and a σ of one nm. The residuals shown in the plot inset indicate that both fits have good agreement with the data.

There are, again, several possible explanations for this result. Sites 90 and 188 are on opposite sides of the protein, and so if the peaks are taken to represent a particular interaction, then the proteins must be aligned head-to-tail. Any significant twists out of such an alignment would produce markedly shorter distances for one site over the other. Alternatively, the peaks may represent the contact distance for fully nonspecific crowding of the protein. If the proteins show no preferential alignment during close contact, then no site-specific alterations in peak position would be expected. Finally, the coincidence of the two peaks may reflect insufficient time to resolve the true distance.

One way to separate these effects would be to modulate the degree of crowding and organization on the surface. This could be done experimentally, with dilution of the spin-label with a nonparamagnetic reagent, or physically by changing the point at which the cells are harvested, and by extension the amount of time for protein expression and surface incorporation. For the former case, the results of 50/50 dilution of MTSL label with the diamagnetic analogue are shown in Figure 7. The MTSL condition is shown in purple, and the 50/50 dilution is shown in teal, where the dilution cuts the modulation depth in half. The modulation depth is typically expressed as scaling with the square of the labeling efficiency, and so the modulation depth would be expected to drop to a quarter of the original value. The actual reduction was by half, indicating that the diamagnetic analogue is not as efficiently incorporated as the MTSL, and that the reduction in labeling efficiency was less than 50%.



Figure 7. The (A) dipolar evolution, and (B) Distance distribution for BtuB 188 in RK5016 OMs with MTSL (purple) and with a 50/50 dilution of MTSL and a diamagnetic analogue (teal) using model-based fitting with Gaussian peaks in DD. The background dimensions were 2.4 and 2.3, respectively. The reduction in apparent background dimension likely reflects a reduction in protein density or aggregation, although the reason for this is not apparent. Both peaks are around 6 nm as before, but the σ values in this case have reduced to half a nm. The modulation depth decreases in half with a 50% reduction in paramagnetic label. The modulation depth scales with the square of the labeling efficiency, and so a 50% dilution with diamagnetic analogue may not produce a 50% reduction in labeling efficiency.

Interestingly, while the positions of the long-distance peaks at 5.9 nm in the full MTSL condition and 5.7 nm in the dilute condition are similar to the previous traces, the widths are markedly narrower. The overall modulation depth for the full MTSL condition is also lower in this

OM growth than was observed in the whole cell traces shown in Figure 6, suggesting that perhaps the growth conditions can affect this distance component. A change in width might suggest a change in protein density, and since BtuB is overexpressed via a leaky promoter this could be controlled by harvesting the cells at different time points during the growth cycle.

A comparison of the long-distance components obtained for RK5016 cells overexpressing BtuB at a series of time points is shown in Figure 8, with the corresponding dipolar traces shown in Figure S1. The times were 6.5, 8, 9.5, 11, 12.5, 14, and 28 hours after the start of growth. The distances bunch together, with a range of 6.2 to 6.7 nm. There may be a small trend towards longer distances with increasing expression time (inset), but the effect is very small with changes of 1 or 2 Å per time point. Given the length of these traces, there is significant error in the position of peaks around 6 nm, and it is unlikely that these differences are statistically significant. The widths of each peak are encoded as the inset error bars, and they too are decoupled from time with all traces showing a similar σ of 13-15 Å.

While the long-distance component did not appear to change as a function of the growth cycle or the length of protein expression, other factors could still influence its form. Over the course of optimizing the whole cell methods presented in this work, a great number of spectra were collected for BtuB 188 in RK5016 cells. Between them, there are variations in buffer pH, growth time, temperature, expression levels, and the presence or absence of the spin-labeled cobalamin. Applying this model-based approach with background cofitting across the larger dataset would then allow for testing of the long-distance components' general stability in response to experimental manipulations.



Figure 8. The distance distribution for BtuB 188 in RK5016 harvested at varying times post-induction analyzed using modelbased fitting with Gaussian peaks in DD. The growth times were 6.5, 8, 9.5, 11, 12.5, 14, and 28 hours. The position of the peaks are plotted as a function of time in the inset, with the error bars giving the σ values of each peak. There is an apparent trend towards longer distances with time, but this is within error. Overall, the position and form of the long-distance component appears to be independent of growth duration, at least for cells harvested beginning in mid-log phase.

A total of 23 traces were found to fit easily using the model-based cofitting approach in DD. Of these, 16 are single-site controls with BtuB 188 and 7 have BtuB 188 in the presence of spin-labeled cobalamin. The time domain data and dipolar traces for these datasets are shown in supplementary figures 2 and 3, while the distance data are shown below in Figure 9. From the distributions, it is apparent that the position of the long-distance component is nearly constant across growths. There is more variance in the width, but only 2 of the 23 traces show a significantly narrower peak than was observed in the dilution controls. A summary of the fit statistics is given in supplementary Table 1. The apparent background dimension was 3.1 ± 0.1 across all 23 fits, with all fits showing an increase in dimension consistent with excluded volume effects. The long-distance component had an average position of 6.4 nm, and an average σ of 12 Å.



Figure 9. Distance distributions obtained for a total of n=23 distributions representing samples of BtuB 188 grown in RK5016 cells. All distributions were obtained using model-based fitting in DD. Single peak distributions are control samples with BtuB 188 while distributions with two peaks also contained 20-60 μ M spin-labeled cobalamin. The position of the long-distance component is highly stable across conditions and growths. A few traces show notably narrower peak widths, but the majority show a consistent σ of 1 to 1.5 nm indicative of broad, heterogeneous interactions between proteins.

With limited variance across growth conditions, the remaining explanations for the constant position and width of the long-distance peak were limited. Either the peak represented the protein-protein contact distance, or the real distance was much longer and the short runtimes prevented it from being properly resolved. In DEER, positional accuracy depends on how much of an oscillation is captured in the time-domain data. This is dependent on the experimental runtime which is in turn dependent on the relaxation rates of the sample and the spectrometer hardware. To reasonably measure distances in the 6-7 nm range, the runtimes needed to nearly double from 3-4 µs to around 7 µs. Modest improvements in runtime can be achieved by using D20 in the solvent buffer, which reduces relaxation due to nearby matrix protons. Almost doubling the runtime required more drastic measures, however, and so BtuB 188 was

grown in RK5016 cells using D₂0 and deuterated glycerol as a carbon source.

The resulting data are shown in Figure 10. The target of 7 us was achieved, although only with 48 hours of averaging, and there is still a single, long-distance peak. The apparent background dimension for the fit was 2.7, indicating that the potential excluded volume driven enhancement is still present when the cells are fully deuterated. The position of the peak changed only slightly with this significant increase in runtime, moving to a new value of 6.8 nm, and the σ increased to 18 A. With the increase in width, the peak now covers most of the distance window accessible to the DEER experiment. Such a broad distribution would be consistent with heterogeneous interactions of BtuB across a variety of inter-protein distances and angles.



Figure 10. The (A) dipolar evolution, and (B) Distance distribution for RK5016 BtuB grown in deuterated media and analyzed using model-based fitting with Gaussian peaks in DD. The background dimension was 2.7. The peak position is now 6.8 nm, with a large increase in width that leads to the peak covering most of the observable distance window (2-10 nm). The extremely broad peak would be consistent with heterogeneous interactions covering a variety of contact distances and orientations.

With several datasets to work from, it became possible to examine some of the models

for aggregation in the OM. As mentioned in the introduction, lipidic (hydrophobic) mismatch has

been observed to drive aggregation of model β -barrel proteins in coarse-grained simulation. Further, this aggregation had the form of linear, string-like aggregates even when the model proteins were composed of highly simplified sequences with only three amino acids (6). This pattern of linear aggregation was also observed in coarse-grained simulations of BtuB at densities determined from fluorescence experiments on BtuB in native surfaces (2) In this latter study, the protein was observed to interact through two hydrophobic interfaces, which form vertically aligned strips of hydrophobic contacts at either end of the protein. In a follow-up experiment these interfaces were used to drive larger scale aggregation of the protein at the mesoscale, and successfully recreated most of the experimentally observed qualities of the protein islands (4).

Fluorescence experiments lack the resolution to examine direct BtuB-BtuB interactions, and so these simulation derived interfaces were the best available comparison for the previously shown datasets. For a string-like aggregation of BtuBs with a defined contact interface, the chain can be thought of as a set of repeating dimers, from which expected distances could be generated in MMM and used to compare to the experimental data. The protein models were generated in pymol from the apo structure of BtuB (PDB id: 1NQG) with the separation distance being the minimum distance that resulted in no overlap of the protein van der Waals surfaces. The BtuB monomers were then rotated to achieve alignment of the hydrophobic strips identified in (6), and the resulting BtuB pairs are shown in Figure 11. With two interfaces per protein, this created three possible orientations, which are defined relative to the 188 site. In the head-to-head interaction (Fig. 11A), the two sites that sit directly below 188 (orange) are aligned together, resulting in a short expected distance. The head-to-tail interaction involves the rotation of one of the two proteins by 180 degrees, creating a mixed interaction with the 188 sites aligned to one side of the pair. This interaction should have an intermediate distance that may align with the experimental results. Finally, the tail-to-tail interaction involves a further rotation of 180 degrees for the remaining protein, resulting in the interaction of the two sites opposite residue 188 (red). This interaction creates the maximum possible distances for direct BtuB-BtuB contact and may be difficult to resolve in DEER.



Figure 11. Models of the BtuB-BtuB interaction from the two interaction interfaces derived from coarse-grained simulations in (2). The apo structure (PDB ID: 1NQG) was used to create the interacting BtuB pairs, and the two interfaces are shown in orange and red. The 188 site (purple) sits above the orange interface. The interfaces were aligned in (A) head-to-head, (B) head-to-tail, or (C) tail-to-tail orientations, with the names based on the facing direction of the 188 site. The inter-protein contact distance was set as the minimum separation that did not produce overlap of the protein surfaces.

From these models of the BtuB-BtuB interactions, predicted distance distributions were generated for 188-188 pairs and are shown as histoGrams in Figure 12. A comparison of these predictions with the deuterated 188 trace from Fig. 10 is shown in Fig. 12A. The center of the peak aligns reasonably well with the head-to-tail predicted distances (orange), while the peak

shoulders stretch into the head-to-head (green) and tail-to-tail (purple) distributions. This would indicate that the protein may interact promiscuously with other BtuB monomers, sampling most possible orientations with a weak preference for the head-to-tail interaction. Relative to the expected string-like aggregates predicted in the coarse-grain simulations, this distribution would be consistent with a mixed population of various sized aggregates and distributed monomers.



Figure 12. Comparisons of the predicted distances from the three BtuB-BtuB interaction modes shown in Fig. 11 with experimental data. The head-to-head distribution is green, the head-to-tail conformation is pale orange, and the tail-to-tail orientation is purple. (A) a comparison of the three orientations with the deuterated 188 trace. While the peak is broad enough to have statistically significant probability in all 3 modes, the center is close to the head-to-tail orientation. (B) A comparison of a simulated distance distribution representing the average position and width of the 23 experimental distributions shown in Fig. 9 against the 3 orientations. This average distribution also closely aligns with the head-to-tail case, and the decrease in width would imply a strong favoritism towards this orientation.

Similarly, Fig. 12B compares the expected interaction distances with a simulated DEER distribution taken from the average peak position and width for the 23 traces shown in Figure 9. It thus represents the average form of the peak for the shorter length traces that were not deuterated. Again, there is good agreement with the expected distances for the head-to-tail orientation, although this averaged distribution has a reduced width that implies greatly reduced sampling of other rotational states. Overall, this method of analyzing the single site distributions, where DD is used with a single Gaussian component and a variable dimension background, is consistent with the model of head-to-tail aggregates. This orientation also explains the observation that sites 90 and 188 showed the same peak position in Fig. 6, as the repeating nature of this interaction mode creates an identical peak for all sites on the protein. Given the widths of the distributions, there is still substantial variability in the actual contact angle, and this

may reflect either fraying of the aggregate chains, or perhaps more simply a mixture of aggregated and randomly distributed proteins.

The previous discussion centered on what type of distribution might be observed for BtuB overexpressed on the cell surface. This perspective centers on what remains after a traditional background subtraction. Still, for most of the data shown in the previous chapter, these additional, varied long-distance peaks are a hindrance to the extraction of accurate information about changes in the short-distance peaks. In these cases, the ideal would be to determine a different background model or analysis scheme that permits the subtraction of all of these intermolecular interactions in the crowded cell surface, to facilitate the extraction of the intramolecular distances of interest. Again, no fully realized model exists for DEER traces showing excluded volume effects derived from proteins on 2d surfaces, but the conclusions of the 3d treatment should serve as a useful guide.

Figure 13 gives the results of four different background subtractions of the deuterated 188 trace first shown in Fig. 10. The time-domain data are shown in the main plot, with a fit line from the corresponding background model, while the plot insets give the subtracted dipolar traces. The first subtraction used a stretched exponential with the expected dimension of 2.0 for proteins on a flat membrane surface (Fig. 10A). Here, the data decays sharply until about 2 us, after which it increases constantly until the end of the trace. This initially appears to be a partial oscillation, as seen with the earlier traces, but closer inspection shows that the late time behavior is nearly linear. Excluded volume effects cause a reduction in decay rate that should pervade most or all of the traces shown here. Crowding is noted in (8), however, to repopulate distances equal to or greater than the contact distance. In this way, it should restore intermediate to long-time decay of the background, and at high enough concentrations cause a return to near-homogenous behavior in the later portions of the time-data (8). The effects of crowding were noted to become most apparent after 2 us, and so this was tested in Fig. 13B by shifting the start time of the subtraction

to 2 us (8). It is apparent that while a small upward turn exists in the final us of the data, overall the latter portion of the trace is quite well represented by the 2d background.

In addition to crowding, radial offset of the labeled site is also expected to alter the background decay rate. Site 188 is on the barrel, and as such is on the edge of the protein with a near maximal offset from the protein center. This edge position partially repopulates the short label-label distances that were lost due to excluded volume, causing restoration of the homogeneous background behavior. For radial offset, this effect is most apparent early in the trace although it continues to increase the apparent decay rate until 5 or 6 us. Thus, the overall background behavior should consistent of a competition between excluded volume and radial offset effects in the short-time region leading up to 2 us, and a combination of all three effects in the later portions. The exact contributions of the radial offset and crowding contributions will vary with the site and the protein density, and thus each trace may show differences in their early-time versus late-time behavior.

Still, an attempt to observe this is shown in Fig. 13C. The trace was separated into two sections from 0-2 us and 2-7 us, and two stretched exponential backgrounds with dimension 2 were fit piecewise to the data. It can be seen from the recovered dipolar trace, shown in orange and magenta, that while there is still a small oscillation this piecewise treatment succeeds in removing most of the intermolecular oscillation. The difference between the decay constants for the 2 elements was 17%, which may indicate the relative importance of repopulation due to radial offset versus crowding effects. This approach is limited in that it would require considerable manual effort with each individual trace, but it shows that the same processes governing 3 dimensionally distributed particles with excluded volume effects appear to be operating here.

Piecewise background fitting cannot currently be implemented in analysis software for DEER software, and the only currently available alternative to the stretched exponential model is



Figure 13. The results of applying different background models to the deuterated 188 trace first shown in Fig. 10. (A) Fitting the expected 2-dimensional stretched exponential to the data starting from the maximum position. (B) Shifting the start time of the background fit to 2 us indicates that the long-time behavior can be approximated by a 2-dimensional stretched exponential. (C) Fitting the short (0-2 us) and long (2-7 us) portions of the trace to separate 2-dimensional backgrounds suppresses most of the apparent oscillation. (D) A quadratic background function with 2 background terms having apparent dimensions of 3 and 6 replaces the partial oscillation seen in A with a full oscillation, indicating that the resulting distance should be decreased.

a quadratic model available in LongDistances. This has the form $e^{b_1+b_2*t+b_3*t^2}$ where b₁, b₂, and b₃ are decay constants with generally negative values. DEER backgrounds are typically quoted as the fractal dimension of the time dependence with 2d backgrounds, for example, having $\frac{2}{3}*t$ dependence. The two time-dependent decay terms in the quadratic background then have fractal dimensions 3 and 6 respectively, and so this model loosely emulates the increase in apparent dimension observed for excluded volume effects.

A fit to the deuterated 188 trace with a quadratic background is shown in Fig. 13D. This background model appears to force a complete oscillation in the data, having a similar shape to the original 2d subtraction in Fig. 13A until 4 or 5 us, where the dipolar trace now inverts to
complete the oscillation instead of continuing upward in the 2d subtraction. Fitting this background corrected trace required 2-Gaussian components, and the result is shown in Figure 14 against the predicted distances for the 3 interaction modes from Fig. 12.



Figure 14. Comparison of the deuterated 188 trace subtracted with a quadratic background function to the three interaction modes presented in Fig. 11. (A) The dipolar trace obtained after subtraction with the quadratic background shows a complete oscillation. (B) The resulting distance distribution fits best to two components, with a short main peak at 6 nm that aligns well with the head-to-tail interaction mode. A second peak is now present at 5 nm, which may indicate poor performance of the quadratic background in the intermediate distance range, selective variance in orientation angle between the head-to-tail and head-to-head modes, or an entirely different form of bimodal associations.

The quadratic fit has good numeric agreement with the dipolar data, and the distances are shifted left with respect to the variable dimension data. There is now a relatively narrow peak that coincides with the expected distances for the head-to-tail interaction mode, and a satellite peak at 5 nm. Theoretically, this satellite peak could be interpreted as indicating that other orientations sampled by the proteins tend only towards the head-to-head interaction type. Still, for data of this length simply adding another term to the stretched exponential may not be enough. Truly dealing with these effects may require radial distribution functions derived either from molecular dynamics or Monte Carlo simulations. The former would be useful if the protein is expected to exist primarily in ordered aggregates, while the latter would provide an approximation of a crowded cell surface with non-interacting particles.

Until such simulations or alternative experimental evidence are available, it would still be useful to have an approximation that aids in the analysis of short-distance components. In Figure 13, it was shown that the decay of the deuterated trace can be split into two portions, with one ranging from 0-2 us and another from 2-7 us. Also, adding an additional term to the stretched exponential background to create a quadratic background did not appear to fully suppress this difference. With the very short distances observed both for BtuB 90-188 and BtuB 188 with the spin-labeled cobalamin, however, less than 2 us is required to observe a full oscillation. It should then be possible to truncate the traces to 2 us and deal only with one of the two decay modes.

This is applied in Figure 15, which shows the results of applying variable or quadratic background subtractions with and without data truncation in LongDistances. Cofitting of the background dimension was enabled and the data were fit to the minimal number of possible Gaussian components. The dataset is an OM sample from RK5016 cells overexpressing BtuB 90-188. The variable background model with the full dataset is shown in purple, which fit with an apparent dimension of 2.36. The resulting dipolar trace required a minimum of 2 Gaussian components, with one being the expected long-distance component. Truncating the data to 2 us, shown in pink, raises the background dimension to 2.57, but the data still require 2 Gaussian components to fit. In both cases, the dipolar traces are dominated by the partial oscillation corresponding to the long-distance component, and the background dimension is ambiguous. The guadratic background model with the full dataset is shown in orange and can be fit with a single Gaussian component. With the full-time data, the quadratic background does a good job of flattening the trace to produce the expected asymptotic decay behavior, but does so by inverting the long-time partial oscillation. This results in a slight shift of the short component, and a strong mismatch between the fit and the data through the partial oscillation. Finally, truncating prior to using the quadratic background is shown in green. Truncation removes the inverted oscillation present in the full-length case, and the short-distance is now recovered at the same position as in the variable fits. The shape of the dipolar data now matches very closely to its expected asymptotic decay behavior, with the oscillations decaying about a straight horizontal line drawn through the end of the data, as seen for the simulated no-background traces shown in Fig. 2.



Figure 15. Suppressing the long-distance component through background alteration and data truncation. The dataset was an RK5016 OM sample for BtuB 90-188. The (A) dipolar and (B) distance data are shown for this trace for two background functions and two data lengths. The variable dimension fits with the full-length data (purple) and the data truncated to 2 μ s (pink) both require 2 Gaussian components in the fit and display long-distance peaks. Conversely, the quadratic fits to the full-length (orange) and 2 μ s (green) data both fit with a single Gaussian component. The full-length result is very poor, however, with the background subtraction producing an inverted partial oscillation. This is removed in the truncated dataset. The poor performance in the later time data indicates that the quadratic background can still only treat the first background decay mode, characterized by excluded volume effects and radial-offset contributions.

With the true nature of the long-distance component still unknown, this makes the quadratic background model in combination with a truncation to remove the second decay regime very attractive. This combination effectively removes the long-distance component while producing subtracted data that has the expected shape and behavior for dipolar decays functions. This method was employed throughout the previous chapter, where the expected distances for the extracellular pairs never exceeded 35 angstroms, and the oscillations could be fully observed even at 2 us.

5.4 Case Study: BtuB 6-510 in cells and Outer Membranes

To conclude this chapter and to illustrate the importance of characterizing the protein organization on the membrane surface, the BtuB 6-510 pair on the periplasmic side of the OM is reconsidered here in Figure 16. The DEER data for BtuB 6-510 in isolated OMs is reproduced in Fig. 16A. The apo and +cobalamin traces were analyzed using DeerAnalysis and had background dimensions of 2.3 and 2.2, respectively. The smaller dimensional enhancement when compared to the 90-188 pair may stem from the location of site 6, which is centrally positioned in the protein without radial offset. Both conditions show the long-distance peak at 5-6 nm discussed in this chapter. For the outer membrane samples, where protein densities and

labeling efficiency are high, this peak is easily explained as a result of intermolecular crowding or aggregation. These physical assumptions also translate to the outer surface of the whole cell preparations, where the labels are still relatively stable. Moving to the periplasmic side of the protein, however, these idealistic assumptions break down. On the periplasmic face the labels are quickly reduced, and the modulation depths of the DEER traces shrink. This implies a significant reduction in labeling efficiency, and the spatial distribution of the still labeled proteins will determine whether or not a long-distance crowding peak emerges. If the labeled proteins are sparsely distributed through the islands, then no peak should be visible. If instead the label remains only on some isolated subpopulation of proteins, say at the cell poles, then the peak may still appear. Thus, the interpretation of distances > 4 nm on the periplasmic face becomes even more ambiguous.

To illustrate this further, the DEER data for the BtuB 6-510 pair in DsbA⁻ cells are shown with a quadratic background subtraction in Fig. 16B, and with a variable dimension background subtraction in Fig. 16C. LongDistances was used in both cases with model-free fitting, and the variable background dimensions were 2.35 for the apo condition and 2.45 for +cobalamin. Both background models show the same three major peaks between 2 and 4 nm, with no apparent change after substrate addition. The longest peak shifts by a nm between the quadratic and variable fits, however, with a center at 4.7 nm in the former case and 5.6 nm in the latter. The position in the variable dimension fit aligns to the long-distance peak in the OM sample, although the huge difference in modulation depth, from 12% to just over 2%, would imply that the crowding peak should be minimized in the whole cells. Instead, this peak is even more dominant as a percentage of area in the live cell sample. This final peak would set the limit of ton-box extension from the BtuB hatch domain and has strong implications on the transport mechanism.



Figure 16. The dipolar (left) and distance (right) data for BtuB 6-510 in (A) RK5016 OM isolates, (B) DsbA⁻ cells with a quadratic background, and (C) DsbA⁻ cells with a variable dimension background. The apo condition is shown in blue while the +cobalamin condition is shown in red. The main peak at 2.5 nm is the same across all three, with the +cobalamin condition in the OM showing another peak between 3 and 4 nm that may represent ton-box extension. Both background subtractions for the pair in DsbA⁻ cells show two peaks that are consistent with extension between 3 and 4 nm. The differences between all three conditions appear in the long-distance component. This is between 5 and 6 nm for the OM sample and for the whole cell sample analyzed with the quadratic background, but the rapid reduction of periplasmic labels in the whole cell call the size of this peak into question. In the quadratic subtraction, the long-distance component moves back to between 4 and 5 nm and is decreased in relative area.

In the *E. coli* ferrichrome transporter, FhuA, DEER distances between site 13 in the FhuA ton-box and similar locations to BtuB 510 in the FhuA barrel displayed peaks out to 4.5 nm, with the most probably distances between 3 and 4 nm. Modeling of these distances using simulated

annealing determined that movement of the first 29 residues of FhuA was required to satisfy the most probable distances, with many more being required to satisfy the edges of the distribution (16). The difference in labeled ton-box position, with site 13 in FhuA versus site 6 in BtuB, means that the BtuB distributions should be shifted to the right, but peaks at 4.5 or 5.5 nm should require the movement of dozens of N-terminal residues in the protein. One model for pore formation in BtuB involves the unfolding of the first 50 residues of the hatch domain, and a peak distance of 5.5 nm in particular would be consistent with this theory.

Thus, being able to determine when peaks in the 5-6 nm range arise from intramolecular distances or intermolecular crowding may become critical in the near future. One way around this problem is the use of many sites around the barrel surface, with the hope of only using distances of < 4 or 5 nm. Still, the end goal of a set of periplasmic distance restraints would likely be to model the state of the extended ton-box and its implications on unfolding in the hatch domain, as was done with FhuA (16). This will require several restraints for triangulation of the ton-box segment in space, and it may not be possible to find several pairs with only short distances. Alternatively, dilution of the protein at the growth level through the introduction of WT BtuB plasmids or harvesting the cells even earlier may drop the protein concentrations low enough to minimize the intermolecular peak. Finally, future progress in simulation and modeling may allow for the identification of a radial distribution function for this mode of crowding and potential string-like aggregation, from which background subtraction would be possible. Regardless, future progress will be required both for the understanding of the protein organization on the bacterial cell surface, and for its suppression when attempting to draw quantitative conclusions regarding the transport mode of BtuB and other TBDTs.

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5.6 Supplementary Figures



Figures S1. Summary of the dipolar traces obtained from samples of BtuB labeled at site 188 from different points in the cell growth cycle. All samples were incubated at RT and pH 8.0. Cells were harvested at the following times after inoculation of the main culture: (A) 6.5 hours (B) 8 hours (C) 9.5 hours (D) 11 hours (E) 12.5 hours (F) 14 hours (G) 28 hours. An increase in growth time, or transition from log phase to stationary phase in the growth cycle, does not appear to change the nature of the observed distance distribution.



Figure S2. Time-domain data obtained for a total of n=23 distributions representing samples of BtuB 188 grown in RK5016 cells. The data correlates to the distance distributions in Fig. 19 in the main text.



Figure S3. Dipolar traces obtained for a total of n=23 distributions representing samples of BtuB 188 grown in RK5016 cells. The data correlates to the distance distributions in Fig. 19 in the main text.

	λ	d	r ₀	σ_0	\mathbf{r}_1	σ_1	χ ²
x	4.73 ±	3.13 ±	25.74 ±	1.83 ±	64.30 ±	12.17 ±	0.68 ±
	0.029	0.064	0.26	0.23	0.50	0.71	0.032

Table S1. A summary of the DD fit statistics for 23 PELDOR data sets for BtuB labeled at site 188 in the presence or absence of the spin-labeled cobalamin. Values are reported plus or minus the standard error of the mean. λ and d represent the leading factor and dimensionality of the exponential background used in DD. r_0 and σ_0 are the center and standard deviation of the short-distance component for the 7 samples with labeled cobalamin while r_1 and σ_1 are the center and standard deviation of the long-distance component for all 23 samples having BtuB labeled at site 188. The average chi squared of the fits is less than 1, in accordance with guidelines for fit selection in DD.

Chapter 6: Future Directions

6.1 Introduction

One of the major limitations of the previous two chapters was the number of sites in the hatch and barrel domains of BtuB. For the hatch, the data was presented primarily for the 74 and 90 positions, while the barrel used residues 188 and 399. The long timeframe of development of the whole cell EPR method presented in this work meant that dozens of measurements were collected for sites 90 and 188, both together and separately, but these cannot substitute for the benefits of having additional sites throughout the protein. Once the method had been standardized, the next direction was thus to obtain a mix of sites in the hatch and barrel. The CW spectra could be used to look for regions of change in response to cobalamin binding, and the DEER data could triangulate the motion observed between 90 and 188, or potentially indicate additional sites of substrate-dependent conformational changes. A total of 10 additional hatch sites and 9 additional barrel positions for grew and labeled successfully, and preliminary results are explored in the following sections.

6.2 Additional Methods

Growth of DsbA⁻ cells overexpressing all new mutants to OD 0.3 was followed by resuspension in 100 mM HEPES, pH 7.0. Labeling proceeded for 30 minutes with 0.1 mg of MTSL and was followed by 2x 15-minute wash steps at RT with 100 mM HEPES, pH 7.0. All buffers now contained 2.5% glucose. 140 μ M cobalamin was added for the + cobalamin conditions.

Results and Discussion

6.3 Additional Hatch Sites

In addition to sites 74 and 90, the following sites produced CW spectra in DsbA⁻ cells: 55, 57, 62, 63, 65, 67, 72, 91, 93, and 98. The locations of these new sites are shown in Figure 1. The 90 position shown frequently throughout chapters 4 and 5 is shown in orange, and the 10 new positions are shown in blue. Together, they surround the cobalamin substrate (Fig. 1A) and make up almost the entire upper surface of the hatch domain (Fig. 1B). Based on the position of

the sidechain β -carbon, all but sites 55 and 98 may be in direct substrate contact upon binding. Additionally, all reside in crowded environments and should produce immobilized components in the resulting CW spectra.



Figure 1. Locations of the new mutant sites in the BtuB hatch domain. The original 90 location is shown in orange, and the new positions are shown in blue. The cobalamin substrate is colored dark red. (A) a top view of the hatch domain shows that the new sites fully surround the substrate, allowing future DEER experiments to isolate movement in any direction. (B) a side view showing that the new sites comprise most of the upper hatch domain. These positions were selected based on sidechain directionality, with sidechains pointing up and out of the protein being predicted to be more easily labeled.

Spectra were obtained in the absence (blue) and presence (red) of cobalamin for each site in DsbA⁻ cells and are shown in Figure 2 alongside the previous sites 74 and 90. All spectra are normalized and represent 10 scan averages with the wavelet denoised transforms plotted overtop the noisy data. Based on noise level, the spectra can be broken into two groups with sites 55, 65, 67, and 98 labeling poorly, and the remainder having similar performance to the previously characterized sites 74 and 90. All locations have multicomponent spectra, with one component having a nearly 70 Gauss splitting indicative of rigid limit behavior, and another component being somewhat more mobile. This reflects the crowded environment, with most of the possible MTSL movement blocked by adjacent protein sidechain and backbone atoms. There is some variance in the mobile component, with sites 63, 72, and 91 displaying different motional schemes. Addition of cobalamin causes a shift towards the immobile component in several spectra, notably at sites 63, 72, 74, 91, and 93. The +cobalamin spectra are very similar at all sites, indicating that

the lack of change in site 90, for example, may simply reflect a lack of sufficient mobility in the apo state to resolve further immobilization with the addition of substrate.



Figure 2. CW spectra obtained for sites in the BtuB hatch domain in DsbA⁻ cells. All spectra are multicomponent, indicating that at least 2 motional regimes are available to the spin label, and all contain a highly immobile component indicative of the crowded environment inside the hatch. Changes are observed at several sites upon substrate addition, with the mobile component transitioning towards the immobile one. For sites that already strongly favor the immobile component in the apo condition, such as site 90, no change is observed. This implies that much of the additional ordering comes from rotameric restriction from the bulky substrate. All spectra are normalized averages of 10 scans and the noisy data are overlayed with the wavelet transform.

To look at the structural significance of the substrate induced shifts, the spectra are replotted around the hatch domain in Figure 3. Site 90 is again shown in orange and was noted in Chapter 4 to be located on a loop that undergoes a conformational shift between a partially helical character in the apo crystal structure, and a fully unstructured conformation in the +cobalamin structure. The new sites 91 and 93 are on the opposite side of the loop to the residues that participate in this helix (85-88) but do display substrate dependent shifts in the CW spectra. This may reflect increased motion further along the loop but given the lack of change in site 90 may simply point to the establishment of direct contact between the substrate and label. Moving clockwise, Sites 72 and 67 sit at opposite ends of a 4-residue turn that lies alongside the cobalamin ribose sugar and phosphate group. Both moieties are bulky and would be expected to reduce the rotamers available to the side chain at these locations, although the change in 67 is much less apparent than at the 72 location. The large shift in the spectrum of 72 is interesting on account of the lack of change in the DEER distribution for the 74-188 pair and could be an excellent follow-up to see if more local shifts are occurring in the hatch domain.

Sites 67, 65, and 55 show similarly poor labeling. Together with site 98, these residues are the furthest towards the hatch interior, and indicate that the center of the hatch may be inaccessible in the native environment. Finally, moving towards the opposite side of the hatch from site 90, only site 63 shows a significant shift in response to substrate binding. The sidechain of residue 63 points directly towards the 5,6-dimethylbenzimidazole (DMBI) ligand in the cobalamin substrate, which likely explains its rigidization. Sites 57 and 62, contrastingly, point away from the substrate and sit on a loop at the top of the hatch domain. Site 98 was the most interior location to label, being a nm or more away from the cobalamin binding site and may show a slight shift towards the mobile component with cobalamin addition. This would make an interesting target for DEER experiments, but it may not be possible to get sufficient labeling efficiency for DEER at this location.



Figure 3. The hatch domain CW spectra as a function of their lateral position in the protein. From this perspective, changes are predominantly seen in the right side of the hatch domain. This is the location of the bulky phosphate, ribose, and DMBI groups, and direct contact between the substrate and label may be producing much of the immobilization. Sites 91, and 93 lie on the same loop as site 90, which was observed to shift in the 90-188 DEER data in chapter 4. Sites 72 and 74 (not shown) are on one end of a 4-residue turn next to the substrate phosphate, with site 67 on the other. The large shift in site 72 was not corroborated by the DEER data for 74-188, which showed no changes in either distance component, suggesting that all of the CW change comes from interaction with the nearby ribose sugar. Sites on the left side of this view, which are typically further away from the substrate show little change upon substrate addition. The spectra also fall into two distinct labeling regimes, with more distal sites (63,91,93,72) showing less noise and better labeling efficiency than the remaining residues, which sit lower in the domain. All spectra are normalized averages of 10 scans and the noisy data is overlayed with the wavelet transform.

6.4 Additional Barrel Sites

In addition to new hatch locations, nine barrel locations around the extracellular face of the protein were labeled successfully in DsbA⁻ cells, and the CW spectra are shown in Figure 4. There were two main goals with these new barrel sites. The first was to identify additional positions that like 188, did not appear to shift in response to substrate. This would allow them to be used as controls for triangulation of motion in the hatch domain. The second was to identify sites that showed strong substrate-dependent response, and that could be combined with the control sites for measurements of gating motions in the loops. These measurements have been performed previously in OMs, but not in the whole cells (1). Looking at Fig. 4, sites 237, 330, 404, and 534 show minimal substrate response. This should make them ideal starting points for DEER experiments with hatch domain residues. Of course, there is the possibility that these sites are in constant, unaltered motion, but this should merely increase the widths of the resulting DEER distributions without creating differences in position. Conversely, sites 403, 451, 491, and 493 show strong immobilization upon substrate addition and may provide additional information on loop motions in the native environment.



Figure 4. CW spectra obtained for sites in the BtuB barrel domain in DsbA⁻ cells. All spectra are multicomponent, owing to the ability of the loops to contact each other, other proteins, and the LPS, all of which may lead to distinct motional modes. For DEER spectroscopy to the hatch domain, ideal sites would show no movement with the addition of substrate. This applies to sites 237, 330, 404, and 534 shown here. The loops that show strong changes in response to substrate may instead be ideal for interloop measurements. All spectra are normalized averages of 10 scans overlaid with the wavelet transform.

The barrel spectra are plotted as a function of their position in the protein in Figure 5. Starting from site 188 and working clockwise, residue 237 is on the adjacent loop to 188 and also shows no apparent change in the CW spectra upon substrate binding. This loop is unresolved in the apo structure and fully unstructured in the substrate-bound structure. The spin label sits at the apex of the loop and may form transient interactions with other elements of the protein or the surroundings. Still, the flexibility indicates that its motions are likely uncoupled from substrate binding and capture. This site may work for DEER measurements, but the length and motion may produce extremely broad distributions that could hinder its use as a control site. Next, site 330 sits nearly opposite the 188 site, and is part of series of 3 associated loops containing sites 330, 403, 404, 450, and 451. The 330 spectrum shows only a small change upon substrate addition, although this residue points up and slightly away from the rest of the protein, minimizing any changes that would be observed with loop motion.

The adjacent loop contains residues 403 and 404, with the former showing a strong immobilization upon cobalamin addition and the latter remaining static. This loop is highly structured, with a 2-turn helix element and strong lateral contacts to the 450/451 loop. 404 sits at the loop apex and points upward, while 403 points towards the 403 loop. Thus, the change in 403 may indicate proximity of the 330 loop. A similar relationship is observed for sites 450 and 451, where 450 is static and 451 immobilizes with substrate. This loop contains one of the extracellular calcium binding sites, which likely immobilizes the backbone, and residue 450 points outward toward the calcium ion, likely contributing to its comparative immobility. Residue 451, in contrast, points inwards towards the phenylalanine and tyrosine residues at positions 404 and 405, respectively, and may form differential contacts with them in response to substrate binding.

Residues 491 and 493 lie on the left side of Fig. 5A and are situated on a short loop that projects outward from the barrel. This loop also contains residue 488 which was previously shown to be static with respect to substrate binding in DEER measurements to site 188 in OM isolates (1). Both 491 and 493 show immobilizations with substrate binding, and the simplest explanation



Figure 5. The barrel CW spectra as a function of their lateral position in the protein, viewed from the (A) top and (B) side. Moving clockwise around the protein, site 237 sits on the adjacent loop to site 188. Both sites show no change with addition of substrate, and so site 237 is expected to provide another static control site for hatch-barrel DEER. Measurements to the opposite side of the protein from 188 will be provided by sites 330, 403, 404, 450, and 451, with 404 showing the least substrate dependent change. Finally, sites 491, 493, and 534 are perpendicular to the 188 position and may prove ideal for determining the potential mode of aggregation in the crowded environments. All spectra are normalized averages of 10 scans and the noisy data is overlayed with the wavelet transform.

would be that this loop moves inward towards the rest of the barrel, establishing new label-protein contacts. Finally, site 534 is the apical site on another loop in steric contact with the 188 loop. This position has no nearby bulky sidechains, and so the lack of change with respect to cobalamin addition was expected. Residues 491, 493, and 534 may also be useful in the organization and crowding experiments, as they sit a quarter turn away from the 188 site. These sites would produce the same peak distance as 188 only in the head-to-tail aggregation case, or where there is no preference for contact interface between proteins and all rotations are sampled. Residues 491 and 493 have the additional benefit of being positioned for easy accessibility to the LPS, and it may be possible to use them to further probe the environment around the protein.

6.5 Future Work

The CW experiments shown here establish a set of new hatch and barrel mutants from which a variety of future DEER experiments can be derived. In chapter 4, it was shown that the 90-188 pair responds to substrate in a dose-dependent manner, with quantitative shifts in the population of two distance components that may correspond to an unfolding event in a helical hatch element. To fully explain this potential conformational change, additional triangulation of sites 90 and 188 would be useful. Thus, additional barrel sites will be paired with site 90 and additional hatch sites with residue 188 to fully ascertain whether the motion is confined to the 90 loop and confirm that this effect can be observed at nearby residues, such as sites 91 and 93. Next, further pairs can be constructed to look for additional sites of conformational change in response to substrate binding. The barrel sites can also be combined into loop-loop pairs to observe gating motions in response to substrate binding in the extracellular face, with the expectation of shrinking interlabel distances with substrate.

For the periplasmic face, site 6-510 was shown in Chapter 4 to produce small but significant DEER traces in the DsbA⁻ whole cells. This pair contains site 6 in the ton-box and can be used to follow ton-box extension into the periplasmic environment. In addition to site 510, residue 6 was previously paired with sites 157 and 384 in a reconstituted DEER study by the

Cafiso lab (2). Reobtaining the 6-157 and 6-384 results in the whole cells will allow for triangulation of the ton-box position and provide a comparison with the *in vitro* system that should highlight the differences in the native environment. The resulting DEER distributions can then be used as restraints in XPLOR-NIH for molecular modeling to produce a structure or structures of BtuB with an extended ton-box, and this should provide information on the number of N-terminal residues that must reorient in response to extension. This, work should mirror that performed in FhuA, and will provide information on the validity of hatch formation via N-terminal unfolding (3, 4).

For the crowding work presented in Chapter 5, there are several ways to further resolve the nature of the OM BtuB organization. The first would be through increases in the sample runtime and apparent modulation depth of the traces, as the distances were too long and broad to properly resolve even in the 7 us deuterated trace for BtuB 188. At the time of writing, the Qband instrument used in these experiments was being upgraded with a higher power TWT amplifier, larger volume resonator, and lower temperature cryostat, which should combine to boost both the runtime and modulation depth of subsequently run samples. This experimental setup should also allow the use of refined DEER experiments, such as 5-pulse and echo-train DEER, which leverage additional pulse-trains in the observe frequency and shaped pulses to greatly increase runtime (5, 6). Alternatively, a 7-pulse refocused out of phase (ROOPh) DEER experiment has been devised, which minimizes all non-intermolecular contributions to the background signal and should permit a more accurate determination of the background model at the same runtime as in 4-pulse DEER (7).

From a sample standpoint, the use of other sites around the barrel that were identified in this chapter should also be able to determine whether there is head-to-tail protein aggregation, or the BtuB proteins are simply forced together with no angular dependence. If the aggregation is not head-to-tail, then the sites that are roughly a quarter-turn around the barrel from BtuB, namely 491, 493, and 534, may give substantially shorter distances in single-label DEER experiments. If

the same distance is observed, then the aggregation is either nonspecific, head-to-tail, or the distance is still unresolved and will have to be proved through the experimental improvements described above. Minimization of the crowding effect can also be achieved through the addition of plasmids encoding WT BtuB to dilute the labeled proteins on the surface, or through the introduction of the WT gene into the same pAG1 plasmid for direct coexpression. The DsbA-mutant also has been seen to suppress the size of the crowding peak and harvesting even earlier in the cell cycle may be sufficient to suppress the island formation. This will have to be in conjunction with the upgraded experimental setup, as many of the DsbA⁻ samples are at the lower end of the DEER concentration range.

Moving to the longer term, the method explored in this work should also be extensible from BtuB to other TBDTs and OM proteins. Ideal initial extensions would be previously studied TBDTs, such as FhuA, FecA, and ShuA, for which prior EPR data from the Cafiso lab is available (8, 9). FhuA could be used for comparisons in ton-box extension between the OM and whole cell environments, while ShuA is structurally highly similar to BtuB and may provide insights into the conservation of motions observed in the BtuB hatch domain (8, 10). From there, labels on OmpF could be used for comparison with the trimeric porin organization observed using AFM, and may provide a reference for comparison with BtuB organization as well (11, 12).

Eventually, work in the native system may progress to the point that the transport pathways can be identified, and work on BtuB can transition towards the development of targeted molecules or peptides that modulate its function for the maintenance of gut ecology or the development of novel antibiotics. This will require further novel extensions of experiment and methodology from those presented here, but the ability to create targeted control of not just *E. coli* but potentially the entire gut microbiota make this system a tantalizing target for future Research.

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